

Livro: Análise de circuitos em engenharia (capa marrom)

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Conceitos básicos

1.1. Sistema de Unidades

SI: Sistema Internacional de unidade

Comprimento, metro [m]

Tempo, segundo [s]

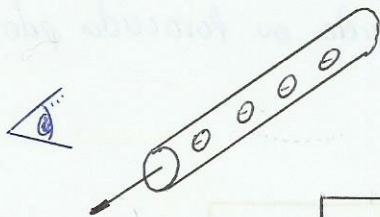
Corrente Elétrica, Ampere [A]

Prefixos

	T, Tera,	10^{12}
Múltiplos	G, Giga,	10^9
	M, Mega,	10^6
	k, Quilo,	10^3
<hr/>		
Sub-múltiplos	m, milo,	10^{-3}
	μ , micro,	10^{-6}
	n, nano,	10^{-9}
	p, piko,	10^{-12}

Quantidades básicas

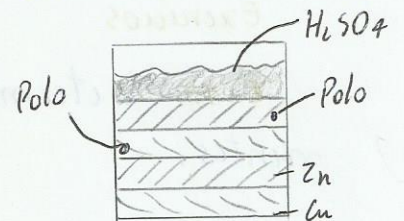
Carga elétrica, Coulomb [C]



$$\frac{1 [C]}{1 [s]} = 1 [A]$$

$$i(t) = \frac{dq}{dt}$$

tensão elétrica, Volt, [V]



Potência elétrica, watt [W]

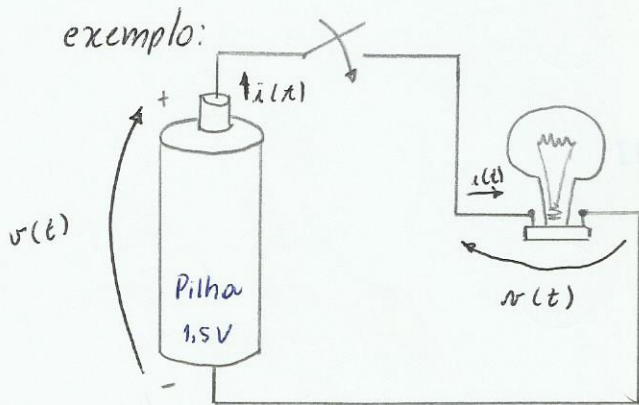
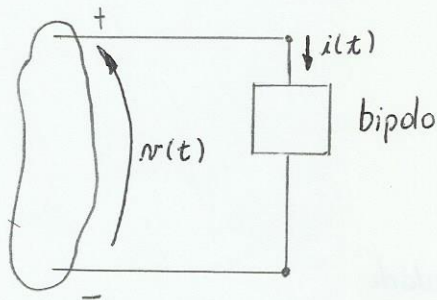
$$P = U \cdot I$$

Energia elétrica [J] = $\underline{W \cdot t}$

$$W = P \cdot t$$

Capítulo Potência em bipolos

Seja um circuito onde está ligado um bipolo.



(convenção)

Gerador: $v(t)$ e $i(t)$ tem o mesmo sentido

$p(t) = v(t) \cdot i(t)$ onde $p < 0$

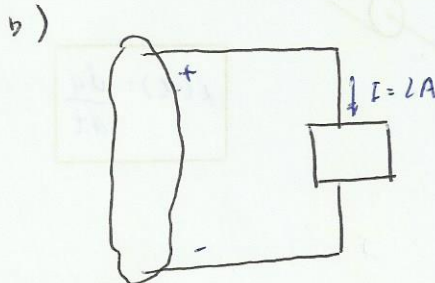
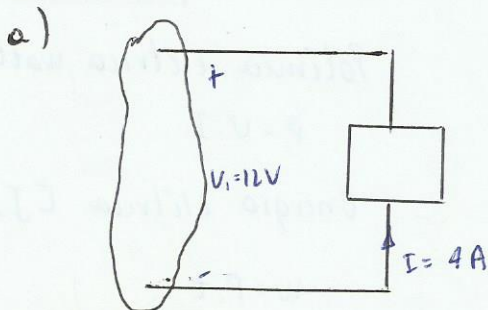
Receptor: $v(t)$ e $i(t)$ tem sentidos opostos

$p(t) = v(t) \cdot i(t)$ onde $p > 0$

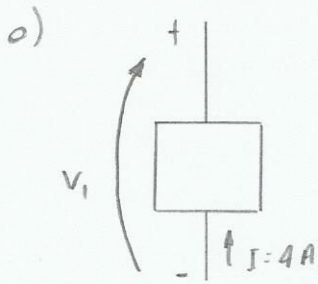
$\therefore -P_g + P_r = 0$ Balanço energético

Exercícios

E.11. Determine a potência absorvida ou fornecida pelos componentes.



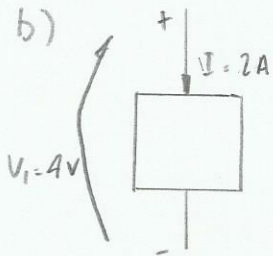
Solução



Gerador

$$P = v_1 \cdot I = 12 \cdot 4 = 48 \text{ W}$$

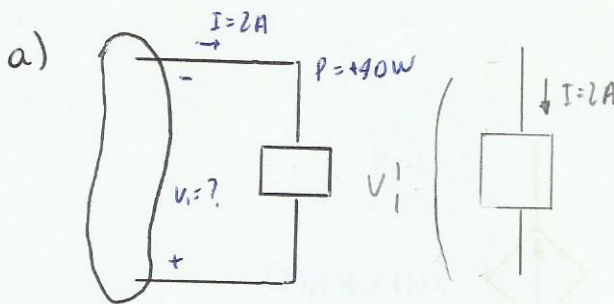
$$P = -48 \text{ W}$$



$$P = v_1 \cdot I = 4 \cdot 2 = 8 \text{ W}$$

∴ é um receptor, $P = 8 \text{ W}$

E 1.2 Determine as variáveis desconhecidas

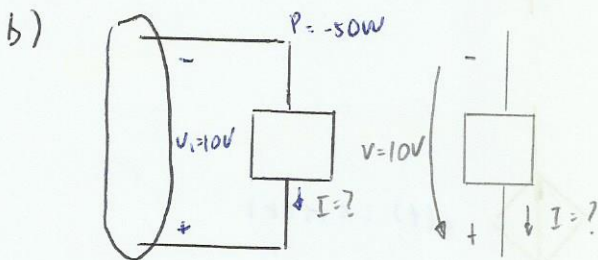


$$P = v_1' \cdot I$$

$$\therefore v_1' = \frac{P}{I} = \frac{40}{2} = 20 \text{ V}$$

(Receptor)

$$v_1 = -v_1' = -20 \text{ V}$$

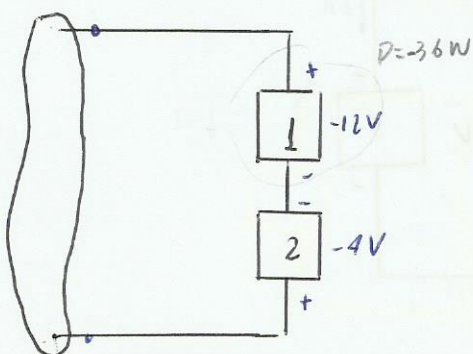


Gerador ($P < 0$)

$$I = \frac{P}{V} = \frac{50}{10} = 5 \text{ A}$$

1.12 pag 15

Dois bipolos estão conectados em série onde, o bipolo 1 fornece ao circuito 36 W, o bipolo 2 fornece ou consome potência? Quanto?



Gerador

$$I_1 = \frac{P}{V} = \frac{36}{12} = 3 \text{ A}$$

Receptor

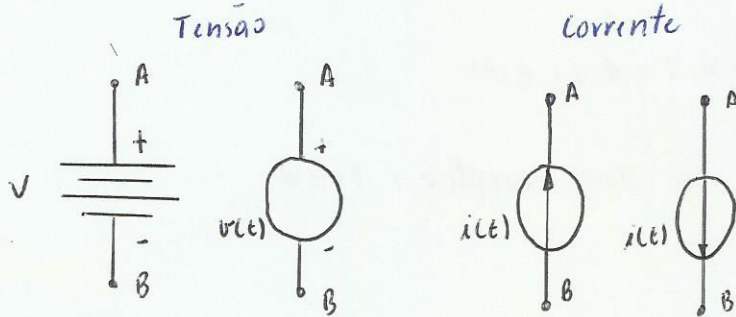
$$P = v \cdot I = 4 \cdot 3 = 12 \text{ W}$$

Sugestões: (HOMEWOR)

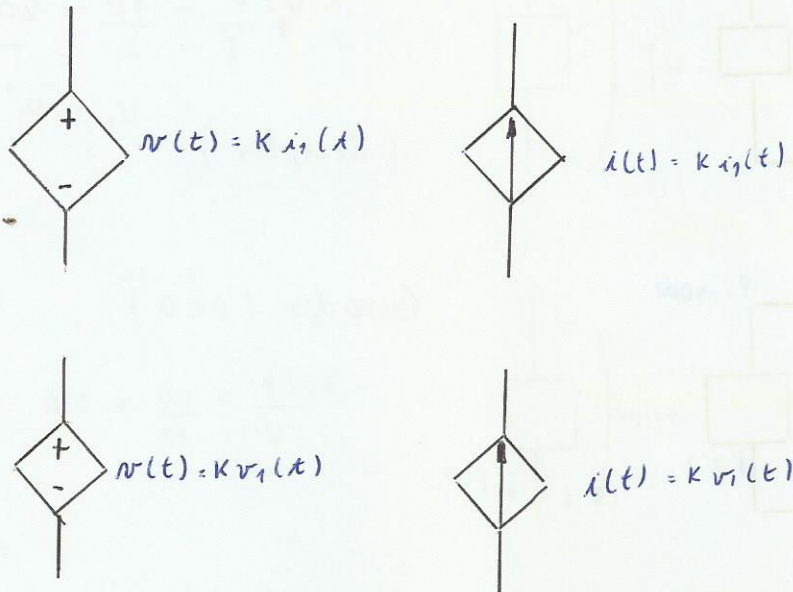
1.8 a 1.11 p:14

1.3. Componentes de circuitos

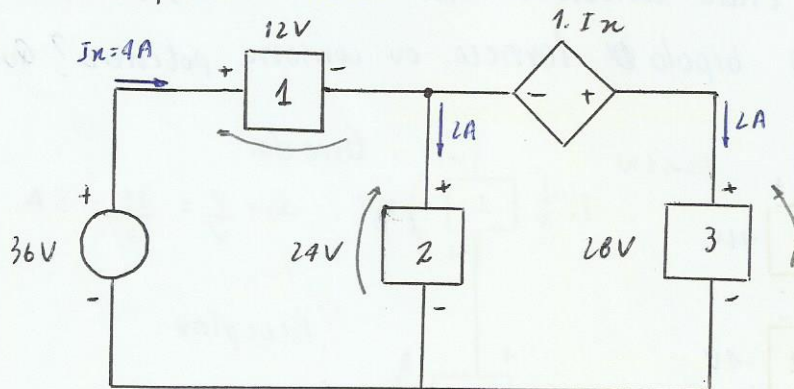
Fontes Independentes (c.c.)



Fontes dependentes ou vinculadas



Exemplo 1.7: Dado o circuito verifique o balanço energético.

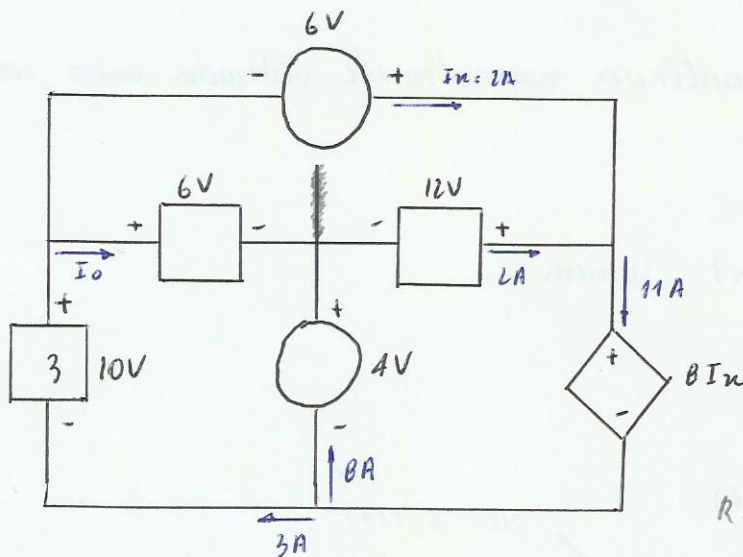


gerada	recebida
$36 \cdot 4 = 144W$	$12 \cdot 4 = 48W$
$1 \cdot I(x) = 4(2) = 8W$	$24 \cdot 2 = 48W$
<u>152W</u>	$-28 \cdot 2 = 56W$
$P_g = -152W$	<u>152W</u>
	$P_{rec} = 152W$

Balanco energético

$$-152 + 152 = 0$$

1.19 Calcule I_0 aplicando balanço energético



Sugestão (HOMEWORK)

1.8 a 1.11 pag 14

1.13 a 1.18 pag 15 116

e 1.20 pag 17

R: $I_0 = 1A$

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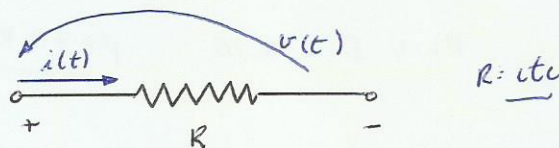
Capítulo 2

Circuitos resistivos

São constituídos de fontes (tensão ou corrente) e resistores

2.1. Lei de Ohm

No resistor existe uma proporcionalidade entre a tensão aplicada e a corrente

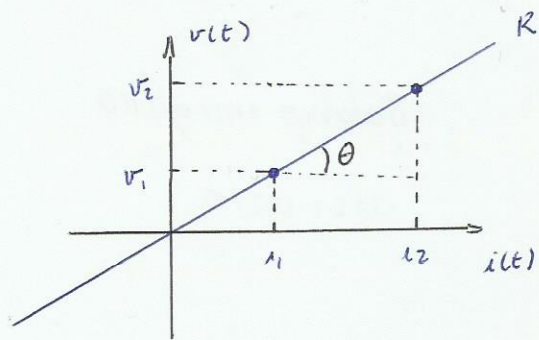


$$\frac{v_1(t)}{i_1(t)} = \frac{v_2(t)}{i_2(t)} = \frac{v_3(t)}{i_3(t)} = \dots = R$$

$$v(t) = R \cdot i(t) \quad \text{Lei de Ohm}$$

unidade, Ohm $[\Omega]$

gráfico de variação $v(t), i(t)$



$$\operatorname{tg} \alpha = \frac{v_2 - v_1}{i_2 - i_1}$$

$$\operatorname{tg} \alpha = R$$

2.1.1. Condutância G

É o inverso da resistência, normalmente utilizada como característica física de condutores.

$$G = \frac{1}{R} \quad [S] : \text{siemens}$$

Potência elétrica

$$p(t) = v(t) \cdot i(t)$$

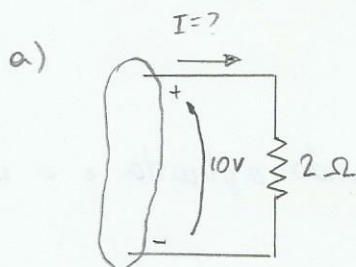
devido a lei de Ohm

$$p(t) = R \cdot i(t)^2$$

$$p(t) = \frac{v(t)^2}{R}$$

Exemplo 2.3 pg 20/21

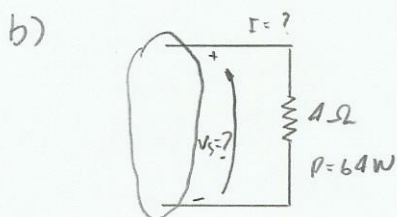
Determine em cada circuito a grandeza desconhecida



Calcule I e P

$$I = \frac{V}{R} = \frac{10}{2} \quad \therefore \quad \underline{I = 5 \text{ A}}$$

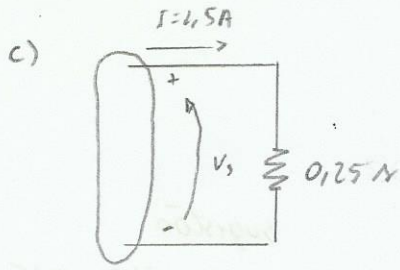
$$P = V \cdot I = 5 \cdot 10 \quad \therefore \quad \underline{P = 50 \text{ W}}$$



Calcule V_s e I

$$P = R \cdot i^2 \quad \therefore \quad i = \sqrt{\frac{P}{R}} = \sqrt{\frac{64}{4}} \quad \therefore \quad \underline{i = 4 \text{ A}}$$

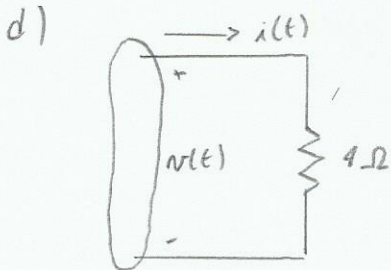
$$V = R \cdot I = 4 \cdot 4 \quad \therefore \quad \underline{V = 16 \text{ V}}$$



Calcular V, P

$$V = 2,5 \cdot \frac{1}{0,25} \quad \therefore V = 10 \text{ V}$$

$$P = 10 \cdot 2,5 = 25 \text{ W}$$



$$v(t) = 16 \sin 377 t \text{ [V]}$$

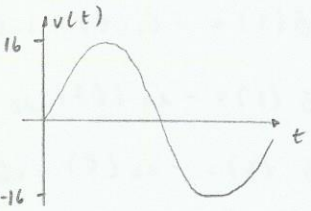
$$i(t) = \frac{v(t)}{R} \Rightarrow i(t) = \frac{16 \sin 377 t}{4}$$

$$\therefore i(t) = 4 \sin 377 t \text{ [A]}$$

$$p(t) = v(t) \cdot i(t)$$

$$= 16 \sin 377 t \cdot 4 \sin 377 t$$

$$\therefore p(t) = 64 (\sin 377 t)^2 \text{ [W]}$$

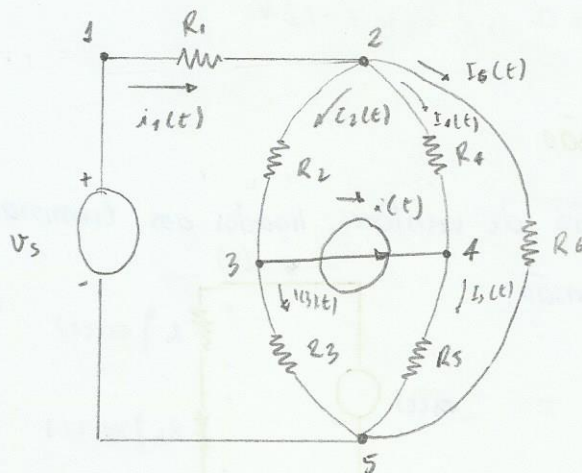
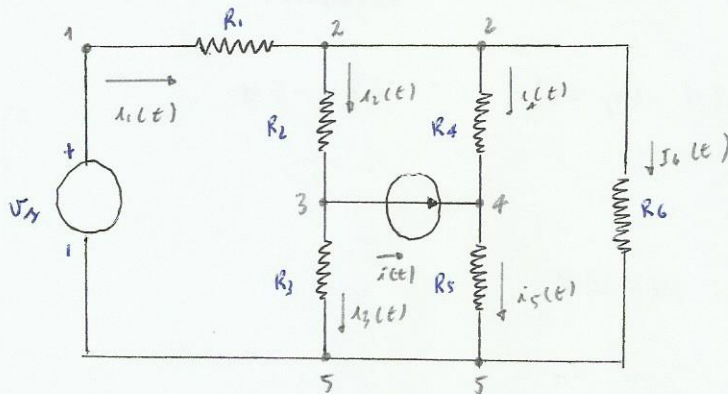


Sujectão E21. e E22
Pg 21/22

2.2 Leis de Kirchoff

Quando o circuito contiver várias conexões de bipolos (nós) e formar pequenos circuitos (laços ou malhas) pode aplicar as leis de Kirchoff.

Ex:



Lei dos nós

A soma algébrica das correntes em um nó é zero.

Convenção

Corrente entra no nó \oplus ela é negativa
 Corrente sai do nó \ominus ela é positiva

sugestão

E.23 EL4 pg 25

nó (1) = $-i_1(t) + i_1(t) = 0$

nó (2) = $-i_1(t) + i_2(t) + i_4(t) + i_6(t) = 0$

nó (3) = $-i_2(t) + i(t) + i_3(t) = 0$

nó (4) = $-i(t) - i_4(t) + i_5(t) = 0$

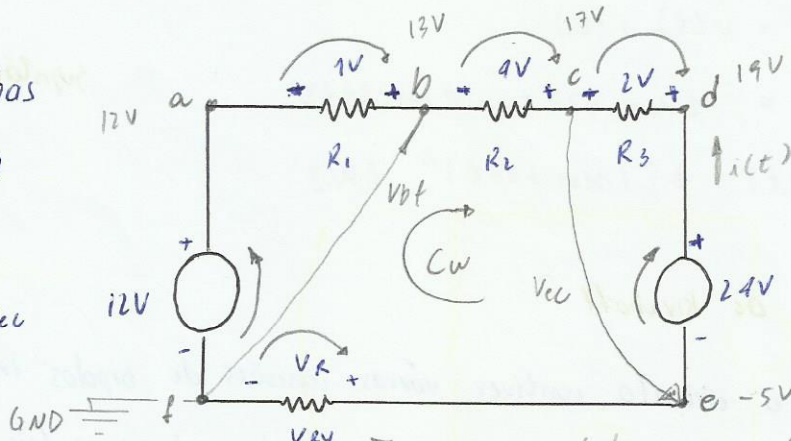
nó (5) = $-i_3(t) - i_5(t) - i_6(t) + i(t) = 0$

ZERO

Lei das malhas

E.26 pg 29

Calcule V_{R1}, V_{R2}, V_{R3}



- Aplicamos o sentido horário \odot CW \leftarrow Está invertido, pois a tensão deu negativa

$12 + 1 + 4 + 2 - 24 - V_{R4} = 0 \quad \therefore V_{R4} = -5V$

- $V_{R1} = ?$

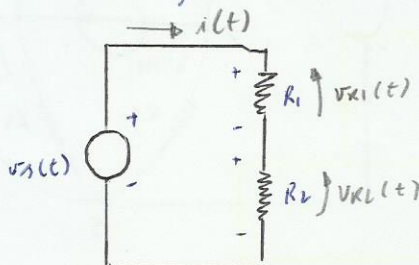
$12 + 1 - V_{R1} = 0 \quad \therefore V_{R1} = 13V$

- $V_{R2} = ?$

$2 - 24 - V_{R2} = 0 \quad \therefore V_{R2} = -12V$

23 Divisor de tensão

Através da utilização de resistores ligados aos terminais da fonte pode obter parte da sua tensão.



$i(t) = \frac{v_{R1}(t)}{R_1} = \frac{v_{R2}(t)}{R_2} = \frac{v(t)}{R_1 + R_2}$

I II III

(I) e (II)

$$\frac{V_{R_1}(t)}{R_1} = \frac{V(t)}{R_1 + R_2} \Rightarrow \boxed{V_{R_1}(t) = \frac{R_1}{R_1 + R_2} \cdot v(t)}$$

(II) = (III)

$$\Rightarrow \boxed{V_{R_2}(t) = \frac{R_2}{R_1 + R_2} \cdot v(t)}$$

Exercício
E 2.5
6V
1A

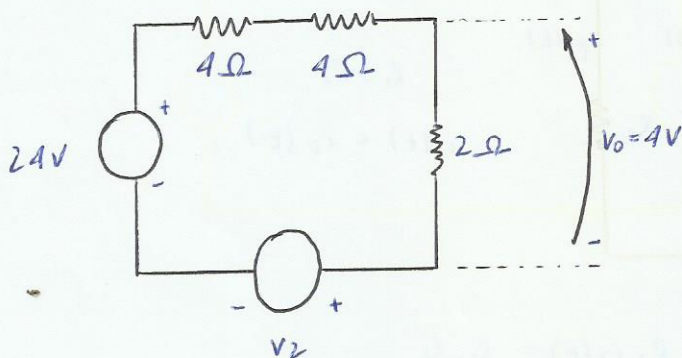
ex: dado $R_1 = 2\Omega$; $R_2 = 3\Omega$ e $v(t) = 12V$

teremos: $V_{R_1}(t) = 4.8V$

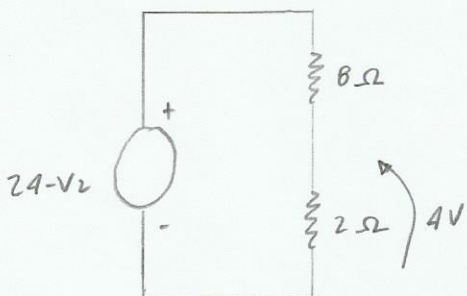
$$V_{R_2}(t) = \frac{7.2V}{12.0}$$

E 2.10 pg 37

Sabe-se que $v_0 = 4V$. Determine por divisor de tensão o valor de v_2



Solução



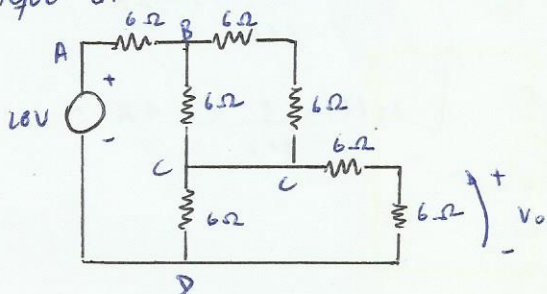
$$V_{R_2}(t) = \frac{R_2}{R_1 + R_2} \cdot v(t)$$

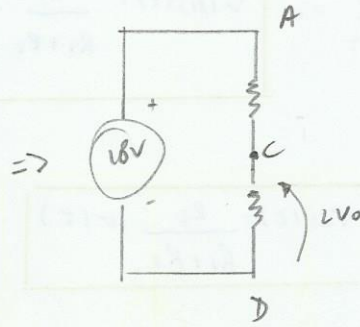
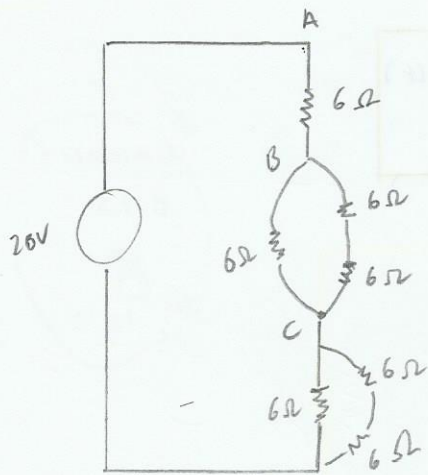
$$4 = \frac{2}{2 + 6} \cdot (24 - v_2)$$

$$\therefore \underline{v_2 = 4V}$$

E 2.11 pg 63

Aplique divisor de tensão e ~~topologie~~ calcule v_0



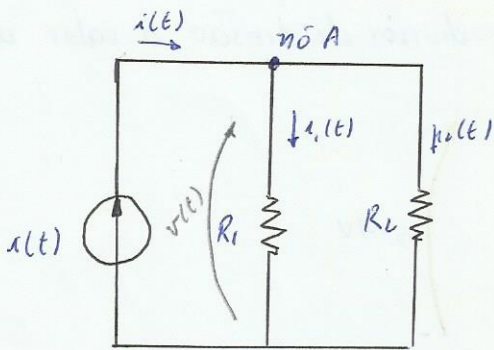


$$E: \begin{matrix} 2.7 \\ 2.6 \\ 2.9 \end{matrix} \left. \vphantom{\begin{matrix} 2.7 \\ 2.6 \\ 2.9 \end{matrix}} \right\} P. 3.137$$

$$2V_0 = \frac{4}{10+4} \cdot 20 \quad \therefore V_0 = 4V$$

Divisor de corrente

Seja o seguinte circuito



$$R_1 > R_2$$

$$i_1(t) < i_2(t)$$

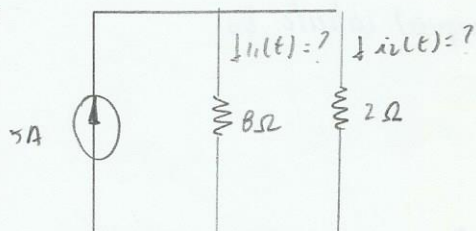
$$v(t) = R_1 i_1(t) = R_2 i_2(t) = \frac{R_1 \cdot R_2}{R_1 + R_2} \cdot i(t)$$

$$\textcircled{I} \quad \textcircled{II} \quad \textcircled{III}$$

$$\textcircled{I} \equiv \textcircled{III} \quad i_1(t) = \frac{R_2}{R_1 + R_2} i(t)$$

$$\textcircled{II} \equiv \textcircled{III} \quad i_2(t) = \frac{R_1}{R_1 + R_2} i(t)$$

Exemplo



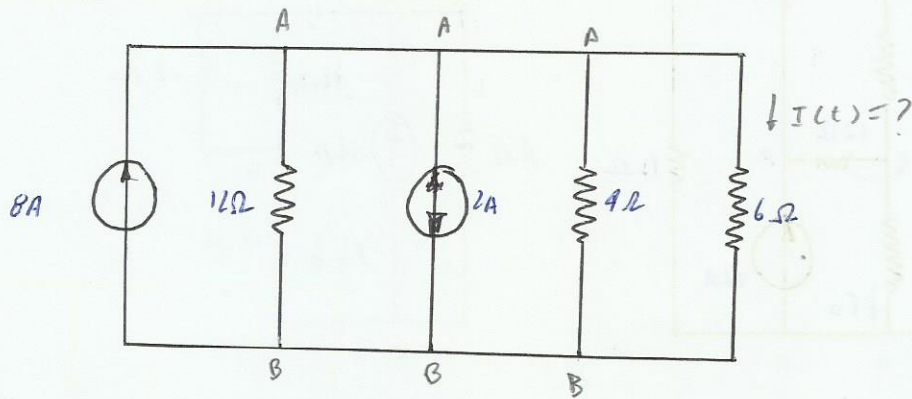
$$i_1(t) = \frac{2}{8+2} \cdot 5 = 1A$$

$$i_2(t) = \frac{8}{8+2} \cdot 5 = 4A$$

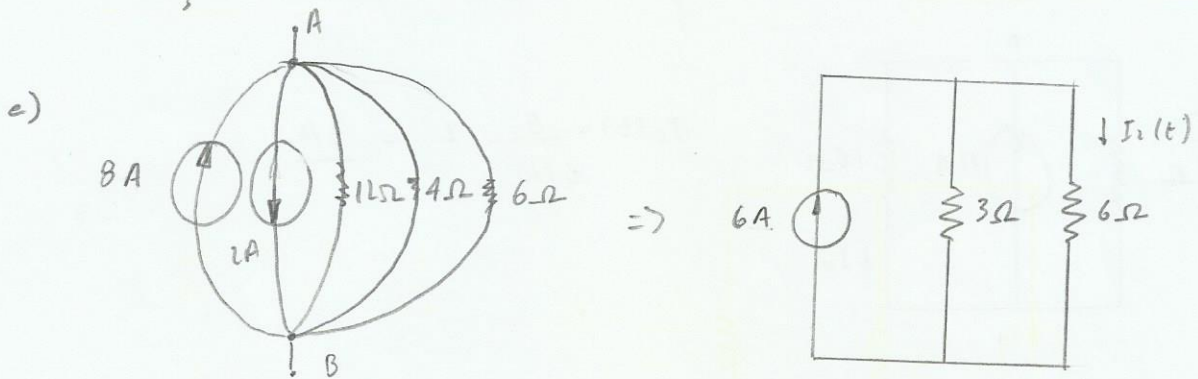
E2.11 Dado o circuito, determine:

a) A intensidade de corrente em 6Ω

b) A potência dissipada em 6Ω



Solução:



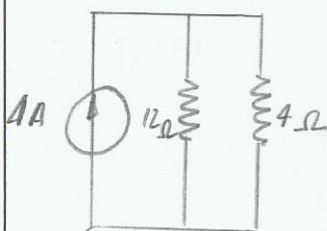
$$I_2(t) = \frac{3}{3+6} \cdot 6 = \underline{2A}$$

b) $P = R \cdot I^2(t)$

$$P = 6 \cdot 2^2 = \underline{24W}$$

c) Qual a intensidade de corrente em 12Ω e 4Ω

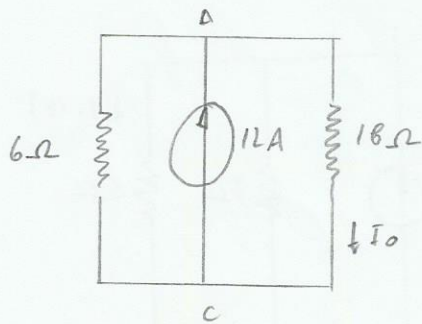
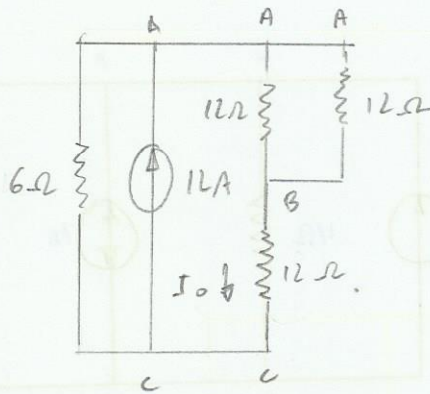
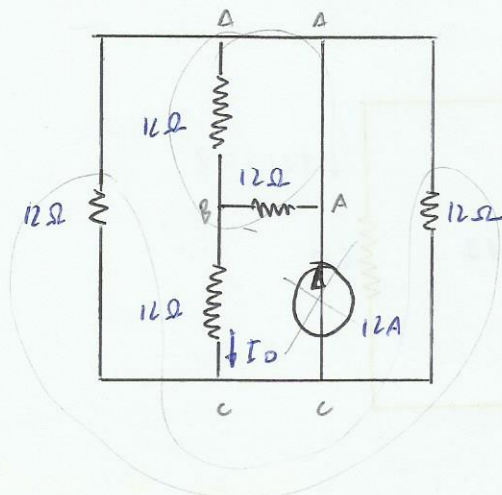
$$I_1(t) = \frac{6}{3+6} \cdot 6 = 4A$$



$$I_1(t) = \frac{4}{12+4} \cdot 4 = \underline{1A}$$

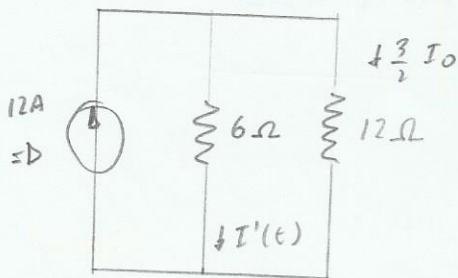
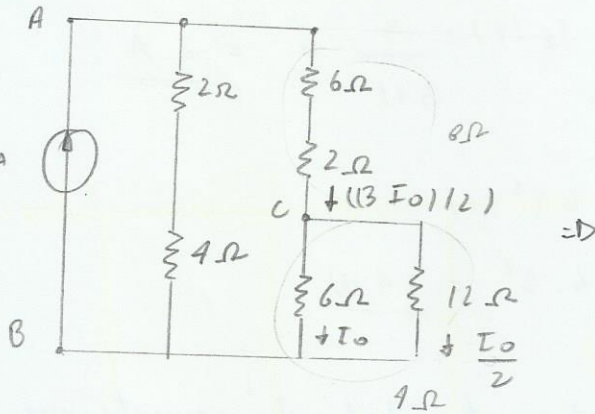
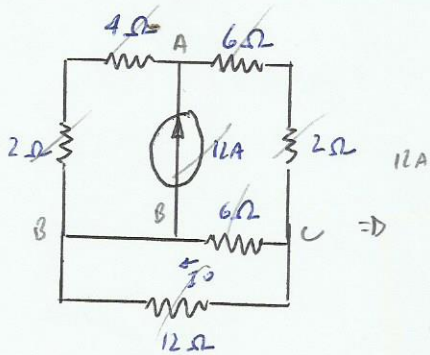
$$I_2(t) = \frac{12}{12+4} \cdot 4 = \underline{3A}$$

Aplique divisor de corrente e calcule I_0 :

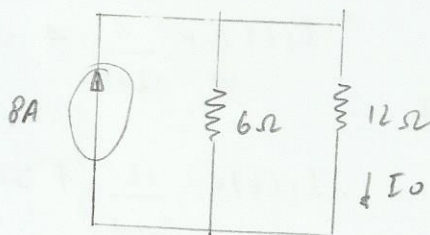


$$I_0(t) = \frac{6}{6+12} \cdot 12 = \underline{3A}$$

2.23 pg 66 sem do 30



$$I'(t) = \frac{12}{6+12} \cdot 12 = 8A$$



$$\frac{3}{2} I_0 = \frac{6}{12+6} \cdot 12$$

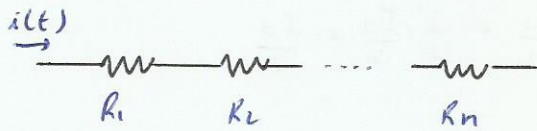
$$\therefore I_0 = \frac{8}{3} A$$

Versão do professor

$$I_0 = \frac{6}{6+12} \cdot 8 = \frac{48}{18} = \frac{24}{9} = \underline{\underline{\frac{8}{3} A}}$$

Combinação de resistores

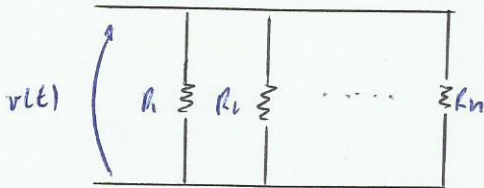
Série



$i(t)$ é a mesma

$$R_T = \sum_{i=1}^n R_i$$

Paralelo



$v(t)$ é a mesma

$$\frac{1}{R_T} = \frac{1}{R_1} + \frac{1}{R_2} + \dots + \frac{1}{R_n}$$

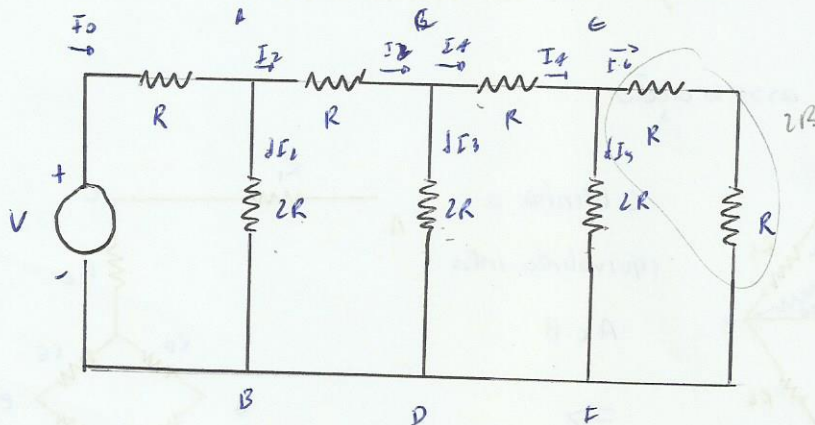
Caso particular (2 resistores em paralelo)

$$\frac{1}{R_T} = \frac{1}{R_1} + \frac{1}{R_2}$$

$$R_T = \frac{R_2 \cdot R_1}{R_2 + R_1}$$

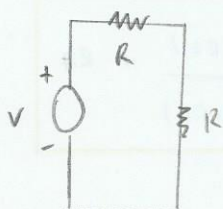
$$\frac{1}{R_T} = \frac{R_2 + R_1}{R_1 \cdot R_2}$$

2.24 Dado o circuito obtenha V_{AB} , V_{CD} , e V_{EF} em função de V



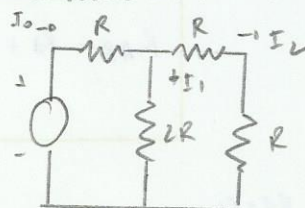
Solução

Cálculo de I_0



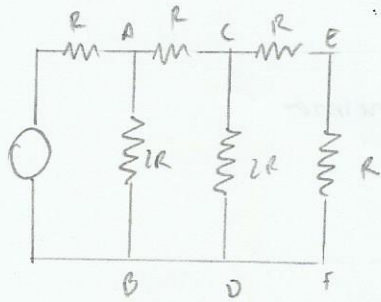
$$I_0 = \frac{V}{2R}$$

Cálculo de I_1 e I_2



$$I_1 = I_2 = \frac{I_0}{2}$$

Calculo I_3 e I_4



$$I_3 = I_4 = \frac{I_2}{2} = \frac{1}{2} \frac{I_0}{2} = \frac{I_0}{4}$$

$$I_5 = I_6 = \frac{I_0}{4} \cdot 2 = \frac{I_0}{2}$$

$$V_{AB} = 2R \cdot \frac{I_0}{4} = R \cdot I_0 = R \cdot \frac{V}{2R} = \frac{V}{2}$$

$$V_{CD} = 2R \cdot \frac{I_0}{4} = \frac{R \cdot I_0}{2} = \left(R \cdot \frac{V}{2R} \right) \cdot 2 = \frac{V}{2}$$

$$V_{CE} = R \cdot \frac{I_0}{2} = \left(R \cdot \frac{V}{2R} \right) \cdot 2 = \frac{V}{2}$$

Sugestões

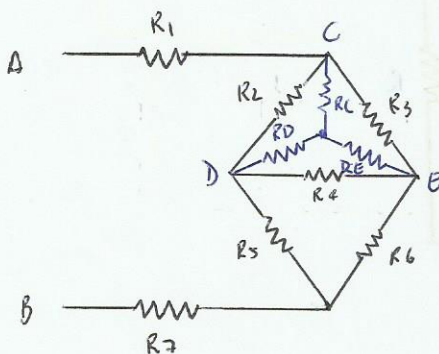
E 2.12 e E 2.13 pg 44

E 2.14 e 2.15 pr 46/47

E 2.16 e E 2.17 pg 32/53

2.7. Transformação triângulo (Δ) em estrela (Y)

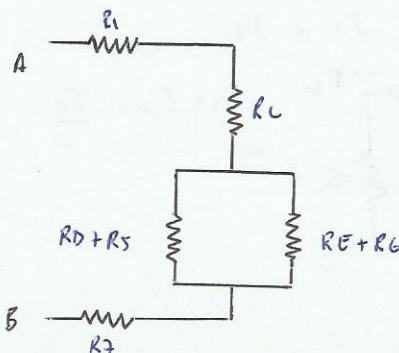
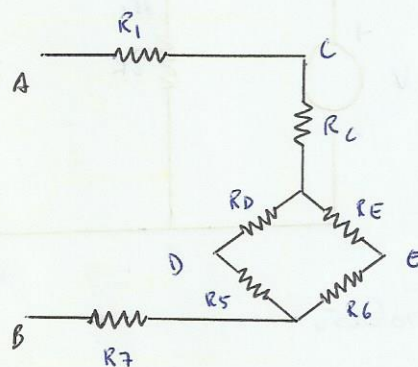
Seja a seguinte associação



Obtenha o equivalente entre

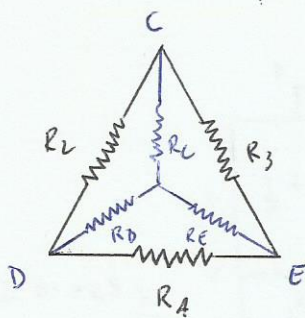
A e B

\Rightarrow



$$R_{AB} = R_1 + R_2 + \frac{(R_3 + R_5) \cdot (R_4 + R_6)}{(R_3 + R_5) + (R_4 + R_6)} + R_7$$

Fórmulas de transformação



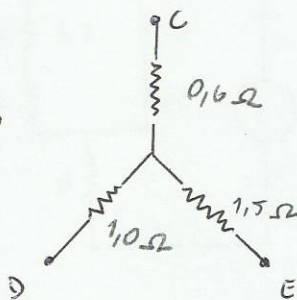
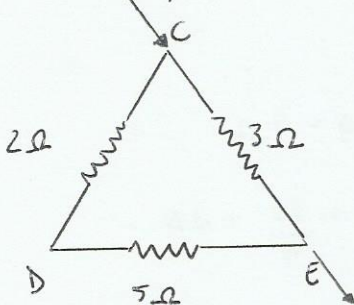
$$R_C = \frac{R_2 \cdot R_3}{R_2 + R_3 + R_4}$$

$$R_D = \frac{R_2 \cdot R_4}{R_2 + R_3 + R_4}$$

$$R_E = \frac{R_3 \cdot R_4}{R_2 + R_3 + R_4}$$



Exemplo



Dedução literal, está na página 53 e 54.

$$R_{CE\Delta} = \frac{3 \cdot 7}{3+7} = 2,1 \Omega$$

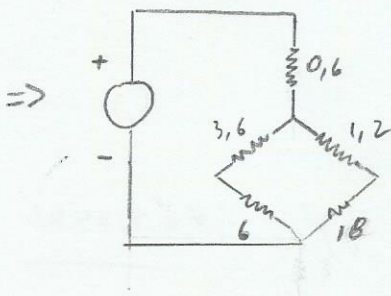
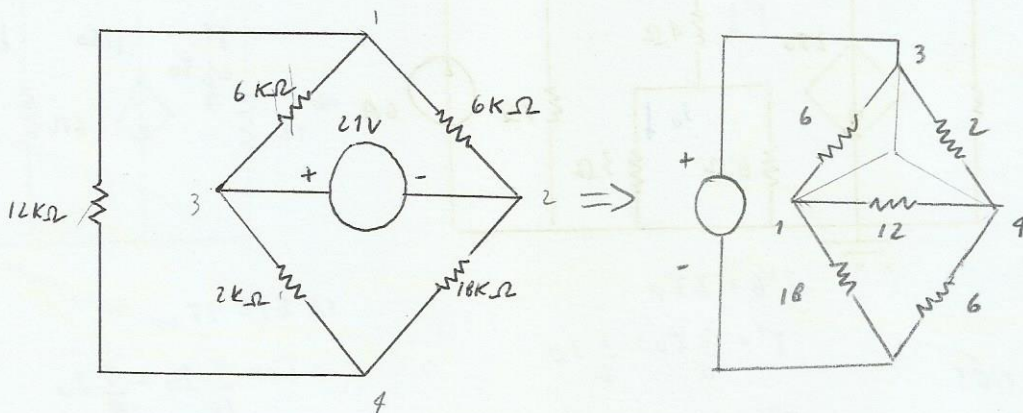
$$R_{CEY} = 0,6 + 1,5 = 2,1 \Omega$$

$$R_{ED\Delta} = \frac{5 \cdot 5}{5+5} = 2,5 \Omega$$

$$R_{EDY} = 1,0 + 1,5 = 2,5 \Omega$$

2.58 pg 74

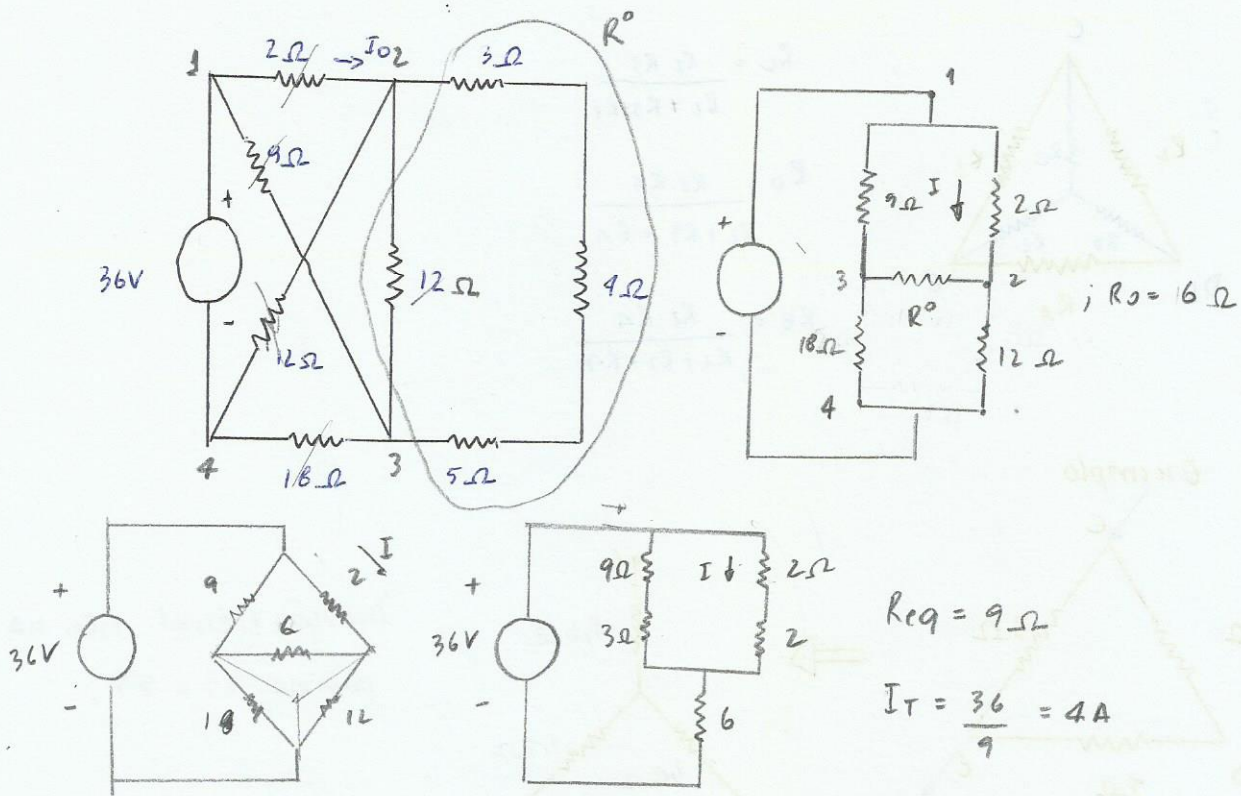
Encontre o valor da potência dissipada pelo circuito



$$R_{eq} = 0,6 + \frac{(3,6+6)(1,2+18)}{3,6+6+1,2+18} = 7$$

$$P = V \cdot I = V \cdot \frac{V}{R} \quad \therefore \quad P = \frac{V^2}{R} = \frac{21^2}{7} \quad \therefore \quad P = 63 \cdot 10^{-3} \text{ W}$$

2.59 Calcule I_0



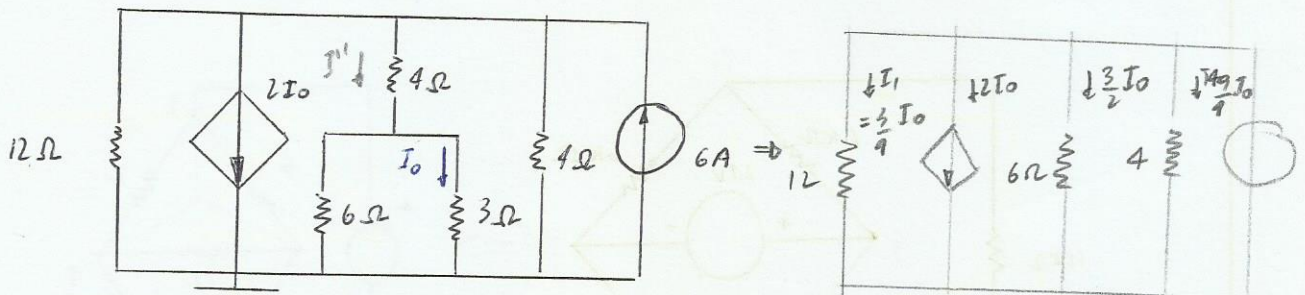
$$R_{eq} = 9\Omega$$

$$I_T = \frac{36}{9} = 4A$$

$$\therefore I = \frac{12}{12+4} \cdot 4 \quad \therefore \underline{I = 3A}$$

28. Circuitos com fontes dependentes

2.7. Dado o circuito calcule a potência dissipada em 12Ω



$$I'6 = 3I_0$$

$$I' = \frac{3}{6}I_0 = \frac{1}{2}I_0$$

$$I'' = \frac{1}{2}I_0 + I_0 = \frac{3}{2}I_0$$

Lei dos nós

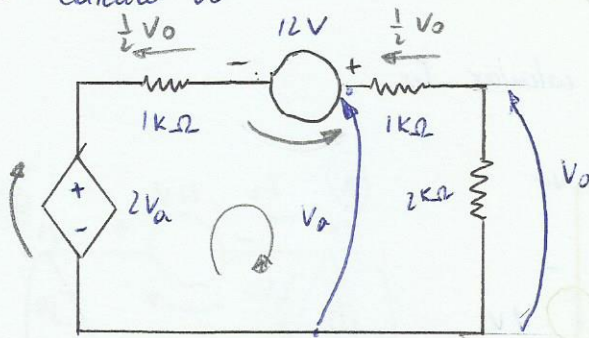
$$\frac{3}{4}I_0 + 12I_0 + \frac{3}{2}I_0 + \frac{19}{4}I_0 = 6$$

$$\frac{13}{2}I_0 = 6 \quad \therefore I_0 = \frac{12}{13} = 0,923A$$

$$P = V \cdot I$$

$$= R \cdot I^2 = 12 \cdot \left(\frac{3}{4} \cdot \frac{12}{13}\right)^2 \quad \therefore \underline{P = 5,75W}$$

2.68 Calcule V_0



Sugestões
 E 2.18 pg 55/56
 E 2.19 } pg 58/59
 E 2.20 }
 2.67 pg 76 resp 6 Ω
 2.69 pg 77 resp 2V

$$2V_a - \frac{1}{2}V_0 - \frac{1}{2}V_0 - V_0 + 12 = 0$$

$$V_a - \frac{1}{2}V_0 - V_0 = 0$$

$$2V_a - 2V_0 = -12$$

$$V_a = \frac{3}{2}V_0$$

$$V_a - V_0 = -6$$

$$\begin{cases} V_a - V_0 = -6 \\ V_a = \frac{3}{2}V_0 \end{cases}$$

$$\frac{3}{2}V_0 - V_0 = -6 \quad \therefore V_0 = \underline{\underline{-12V}}$$

Materia de Prova

Cap. I, II, III (até análise modal)

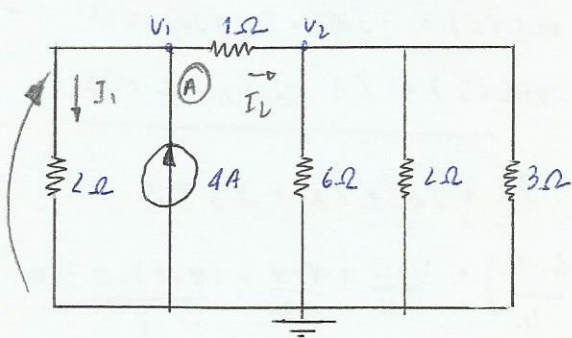
3 e 4 (exercícios conjuntos)

Análise modal

Para a resolução de circuitos

- 1º) Escrevemos as equações modais (lei dos nós) necessários
- 2º) Nominamos a ddp nos terminais de cada bipolo
- 3º) transformamos para lei de Ohm.

Determine V_1 e V_2 aplicando análise modal



Soluções

Nó A : $-4 + I_1 + I_2 = 0$

$$I_1 + I_2 = 4$$

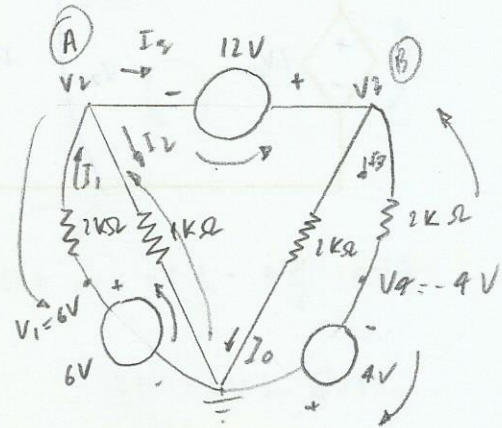
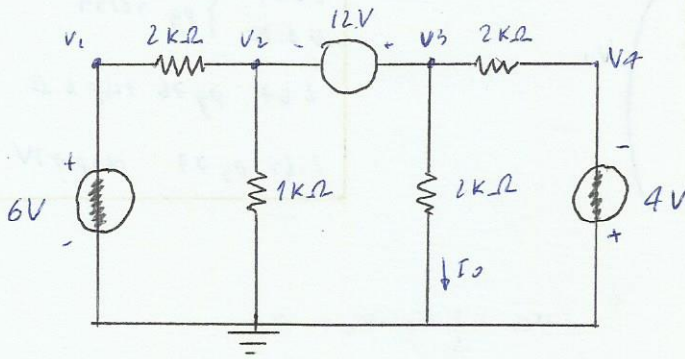
$$\frac{V_1 - 0}{2} + \frac{V_1 - 0}{2} = 4$$

$$V_1 = 4V$$

$$V_2 = \frac{1}{2}V_1 = 2V$$

Exercício com fonte de tensão

Utilize análise nodal para calcular I_0



Lei dos nós

nó A: $-I_1 + I_2 + I_3 = 0$

nó B: $-I_3 + I_0 + I_4 = 0 \Rightarrow -I_1 + I_2 + I_0 + I_3 = 0$

Lei de Ohm

$$-\left[\frac{6-V_2}{2k}\right] + \frac{V_2-0}{1k} + \frac{V_3-(-4)}{2k} + \frac{V_3-0}{2k} = 0$$

$$-6 + V_2 + 2V_2 + V_3 + 4 + V_3 = 0$$

$$3V_2 + 2V_3 = 2$$

onde $V_3 - 12 = V_2$

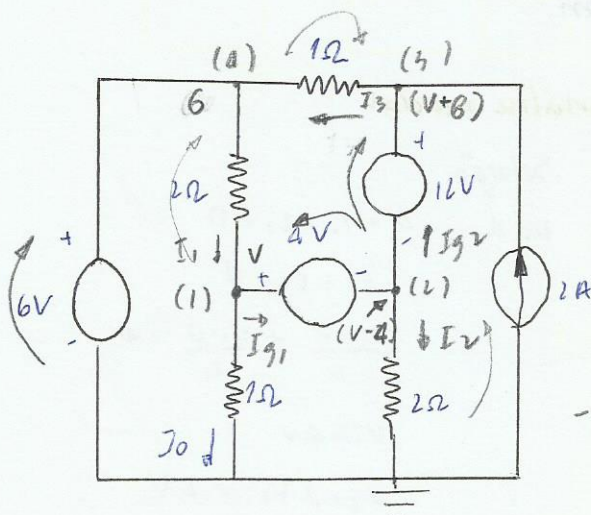
$$3(V_3 - 12) + 2V_3 = 2$$

$$3V_3 - 36 + 2V_3 = 2$$

$$5V_3 = 38 \Rightarrow V_3 = \frac{38}{5}$$

$$\frac{V_3 + 4}{2k} = I_0 \Rightarrow I_0 = \left(\frac{38}{5} + 4\right) \cdot 10^{-3} \Rightarrow I_0 = ?$$

3.28 Utilize a análise nodal para determinar I_0 na rede



nó (1) $= -I_1 + I_0 + I_{g1} = 0$

nó (2) $= -I_{g1} + I_2 + I_{g2} = 0$

nó (3) $= I_3 - I_{g2} - 2 = 0$

$$-I_1 + I_0 + I_2 + I_3 = 2$$

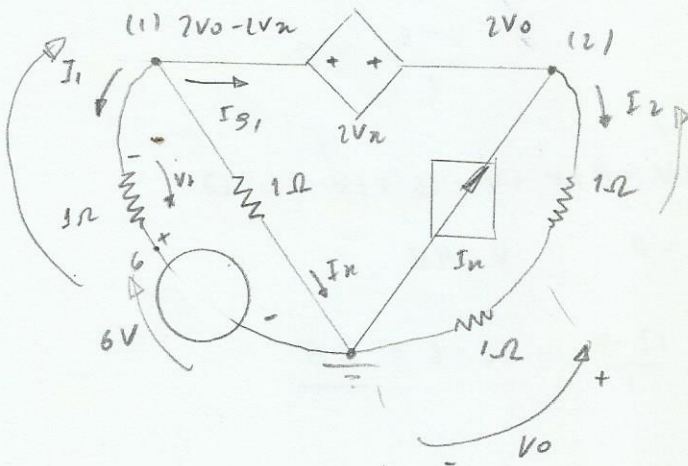
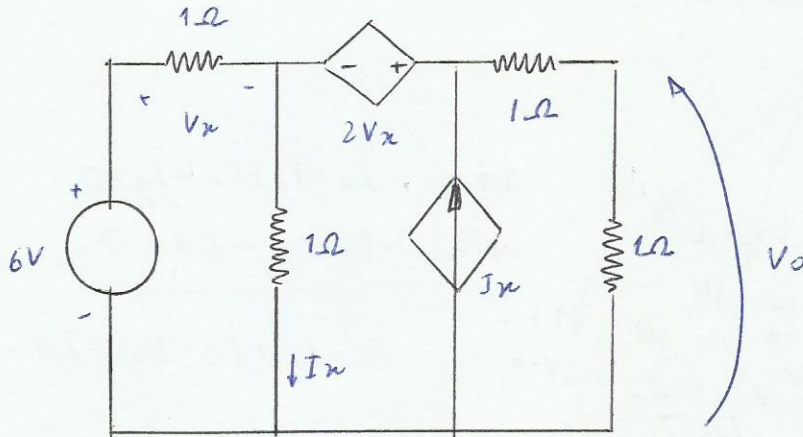
$$-\left(\frac{6-V}{2}\right) + \frac{V-0}{1} + \frac{V-4}{2} + \frac{(V+8)-6}{1} = 2$$

$$-6 + V + 2V + V - 4 + 2V + 4 = 4$$

$$6V = 10 \quad \therefore V = \frac{10}{6} = \frac{5}{3}$$

$$I_0 = \frac{V}{1} \quad \therefore I_0 = \frac{5}{3} \text{ A}$$

3.36 pg. 134 Determine v_0 por análise nodal



$$\text{nó (1): } I_1 + I_{g1} + I_x = 0$$

$$\text{nó (2): } -I_{g1} - I_x + I_2 = 0 \quad +$$

$$I_1 + I_2 = 0$$

$$\frac{2v_0 - 2v_x - 6}{1} + \frac{2v_0 - 0}{1} = 0$$

$$3v_0 - 2v_x = 6$$

$$\hookrightarrow 3v_0 - 2(2v_0 - 6) = 6$$

$$3v_0 - 4v_0 + 12 = 6$$

$$-v_0 = -6 \quad \therefore v_0 = 6 \text{ V}$$

Sugestões

3.30 pg. 133 (R: 3 A) (Adotar 1 sentido para I_0)

3.31 "

3.29 "

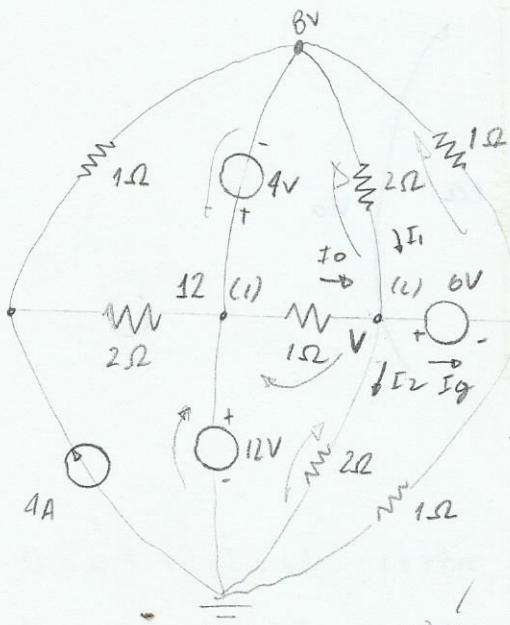
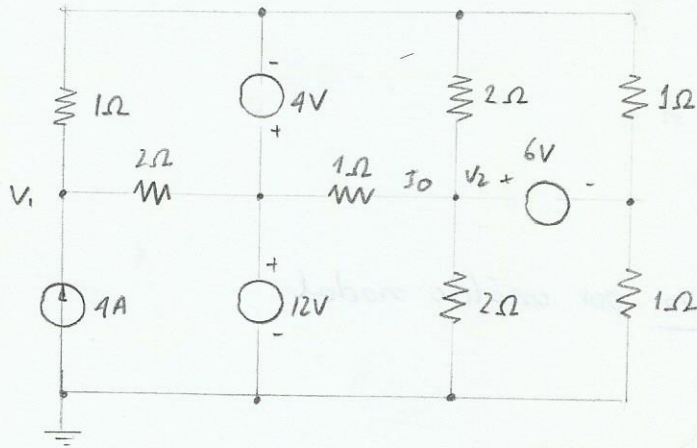
3.33 pg 134

Exercício 3.30

Estrela triângulo

↳ Estudou

triângulo → estrela



nó 2: $-I_0 - I_1 + I_2 + I_3 = 0$

nó 3: $-I_3 - I_4 + I_1 = 0$

$-I_0 - I_1 + I_2 - I_3 + I_4 = 0$

$-\left(\frac{12-V}{1}\right) - \left(\frac{8-V}{2}\right) + \frac{V}{2} - \left(\frac{8-(V-6)}{1}\right)$

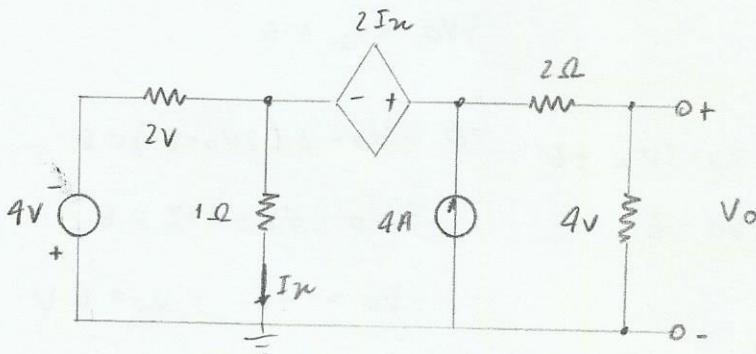
$+ \frac{V-6}{1} = 0$

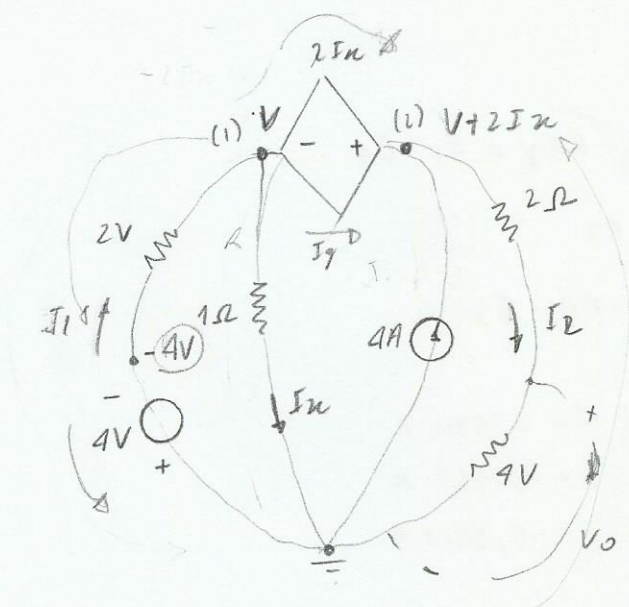
$-24 + 2V - 8 + V + V - 16 + 2V - 12 = 0$

$6V - 64 = 0 \quad \therefore V = 9V$

$I_0 = \frac{12-V}{1} = 12-6 = \underline{3A}$

Exercício 3.31





$$(1) \Rightarrow -I_1 + I_2 + I_x = 0$$

$$(2) \Rightarrow -I_2 - 4 + I_x = 0$$

$$-I_1 + I_2 + I_x = 4$$

$$-\left[-\frac{4-V}{2}\right] + \left[\frac{V-0}{1}\right] + \left[\frac{V+2I_x-0}{6}\right] = 4$$

$$12 + 3V + 6V + V + 2I_x = 24$$

$$10V + 2I_x = 12 \quad ; \quad I_x = \frac{V}{1}$$

$$12V = 12$$

$$V = 1V \quad \therefore \quad I_x = 1A$$

$$V_0 = \frac{4}{4+2} \cdot (V + 2I_x)$$

$$= \frac{4}{6} (1+2)$$

$$\therefore V_0 = 2V$$

Capítulo 3

Análise de laço

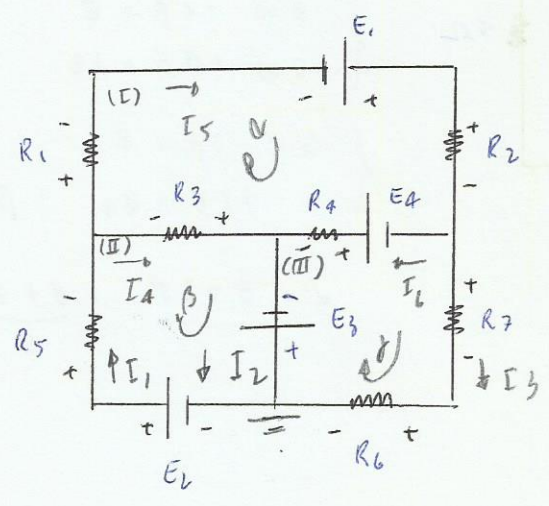
Adotamos uma corrente fictícia para cada laço,

($\alpha, \beta, \gamma, \dots$)

uma vez obtido o seu valor partimos as respostas do circuito

Ex p 999

Circuito de três malhas



- Dados:
- $R_1 = 2\Omega$
 - $R_2 = R_4 = R_7 = 1\Omega$
 - $R_3 = 3\Omega$
 - $R_5 = 4\Omega$
 - $R_6 = 2\Omega$

- $E_1 = 12V$
- $E_2 = 6V$
- $E_3 = 18V$
- $E_4 = 24V$

equações de laço

$$(I) \quad (R_2 + R_3 + R_4 + R_1) \alpha - R_3 \beta - R_4 \gamma = E_1 + E_4$$

$$(II) \quad (R_3 + R_5) \beta - R_3 \alpha = E_2 + E_3$$

$$(III) \quad (R_4 + R_6 + R_7) \gamma - R_4 \alpha = -E_4 - E_3$$

$$\begin{cases} 7\alpha - 3\beta - \gamma = 36 \\ -3\alpha + 7\beta = 14 \\ -\alpha + 4\gamma = -42 \end{cases} \begin{matrix} \text{Resp} \\ \text{Linha} \end{matrix} \begin{cases} \alpha = 6,5490 \text{ A} \\ \beta = 6,2353 \text{ A} \\ \gamma = -0,8627 \text{ A} \end{cases}$$

$$I_1 = \beta = 6,2353 \text{ A}$$

$$I_2 = \beta - \gamma = 15,098 \text{ A}$$

$$I_3 = \gamma = -0,8627 \text{ A}$$

$$I_4 = \beta - \alpha = -0,3137 \text{ A}$$

$$I_5 = \alpha = 6,5490 \text{ A}$$

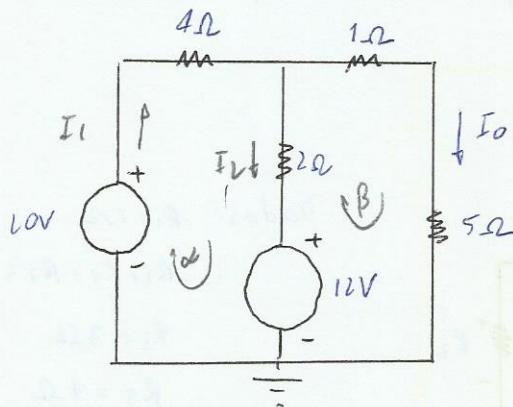
$$I_6 = \alpha - \gamma = 15,4117 \text{ A}$$

3.40 (Modificado) pg 135

Dado o circuito aplique análise e calcule:

a) I_0 ?

b) Potência dissipada em 5Ω



$$\begin{cases} (4+2)\alpha - 2\beta = 20 - 12 \\ (2+1+5)\beta - 2\alpha = 12 \\ 6\alpha - 2\beta = 8 \\ -2\alpha + 8\beta = 12 \\ 6\alpha - 3\beta = 8 \\ 22\beta = 44 \quad \beta = 2 \end{cases}$$

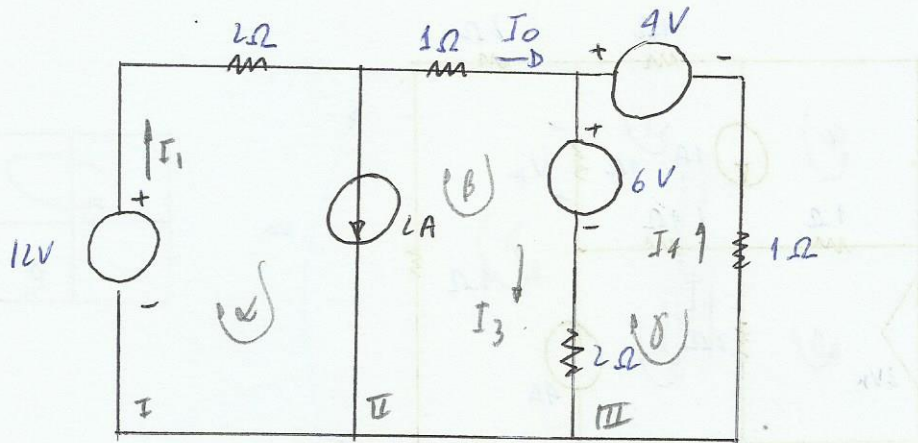
$$\alpha = \frac{8 + 2\beta}{6} = \frac{8 + 4}{6} = 2$$

$$\therefore I_0 = \beta = 2 \text{ A}$$

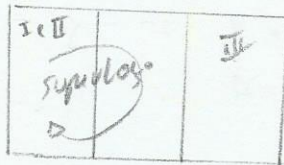
$$P = V \cdot I = R \cdot I^2 = 5 \cdot 2^2$$

$$\therefore P = 20 \text{ W}$$

3.42) Aplique a análise do laço e calcule I_0



Solução



$$2\alpha + 3\beta - 2\gamma = 12 - 6$$

$$3\gamma - 2\beta = 6 - 4$$

$$\begin{cases} 2\alpha + 3\beta - 2\gamma = 6 \\ -2\beta + 3\gamma = 2 \end{cases}$$

onde

$$\alpha - \beta = 2$$

$$\alpha = 2 + \beta$$

$$\gamma = \frac{2 + 2\beta}{3}$$

$$2(2 + \beta) + 3\beta - 2 \left(\frac{2 + 2\beta}{3} \right) = 6$$

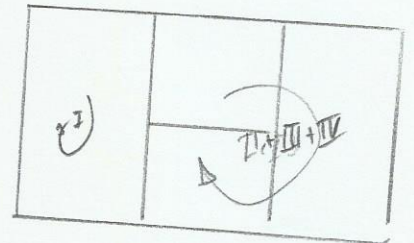
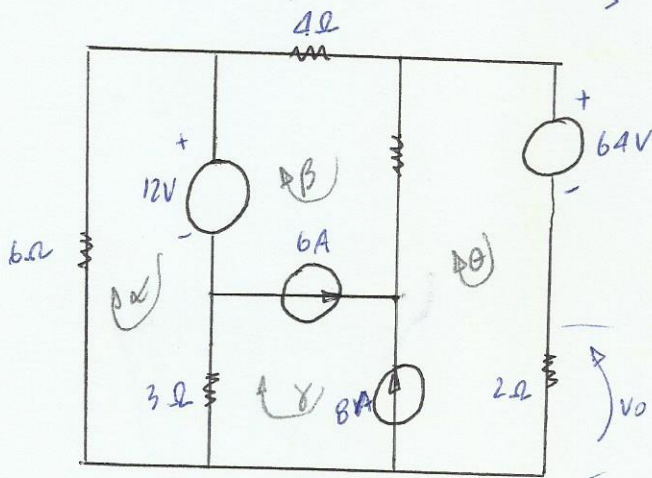
$$4 + 2\beta + 3\beta - \frac{4}{3} - \frac{4}{3}\beta = 6$$

$$\frac{11}{3}\beta = \frac{10}{3}$$

$$\beta = \frac{10}{11}$$

$$\therefore I_0 = \frac{10}{11} \text{ A}$$

3.58-) Determine V_0 por análise de laço



$$9\alpha - 3\gamma = -12$$

$$4\beta + 2\theta + 3\gamma - 3\alpha = 12 - 64$$

$$9\alpha - 3\gamma = -12$$

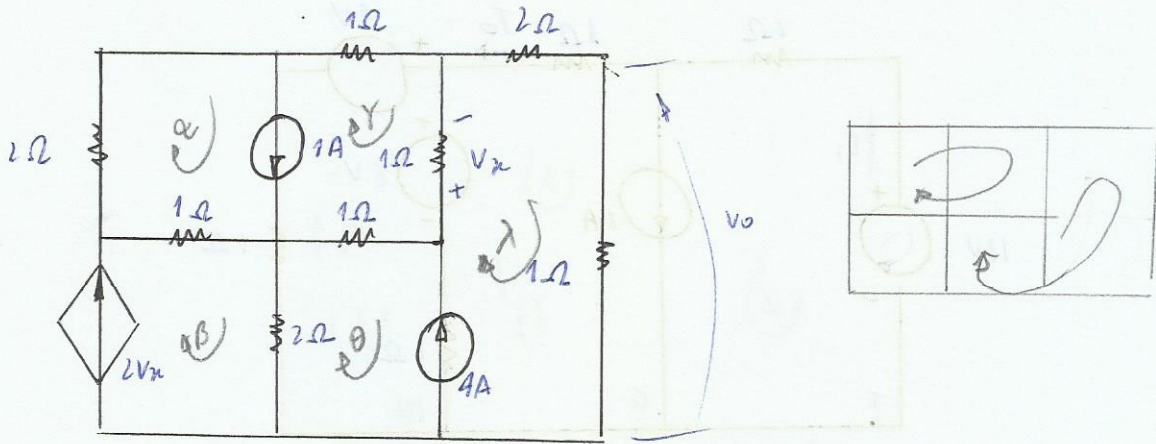
$$4\gamma - 24 + 16 + 2\gamma + 3\gamma - 3\alpha = -52$$

onde $\gamma - \beta = 6$ $\beta = \gamma - 6$

$\theta - \gamma = 8$ $\theta = 8 + \gamma$

$$9\alpha - 3\gamma = -12 \quad \therefore \theta = 1A$$

$$-3\alpha + 9\gamma = -44 \quad V_0 = 2\theta = 4V$$



$$\begin{cases} 3\alpha + 3\gamma - \beta - \theta - \lambda = 0 \\ 3\theta + 4\lambda - 2\beta - 2\gamma = 0 \end{cases} ; \text{ Onde } \beta = 2V_x \rightarrow V_x = 1(\lambda - \gamma)$$

$$\alpha - \gamma = 1$$

$$\lambda - \theta = 4$$

$$\lambda = 3,43 \text{ A}$$

$$V_0 = 1 \cdot \lambda = 3,43 \text{ V}$$

Sugestões

- 3.43 pg 136 resp) 17 A
- 3.55 - pg 139 resp) $\frac{3}{2}$ V
- 3.61 pg 141 resp) $\frac{90}{11}$ V
- 3.65 pg 142 resp) $\frac{36}{11}$ V

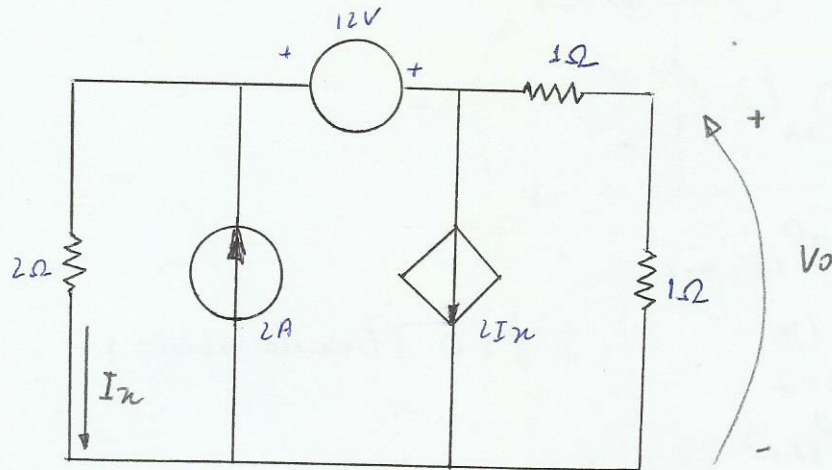


Capítulo 5 Teorema de Thévenin / Norton (continuação)

- Circuito com fonte dependente

5.46 pag 220

Aplique o teorema de Thévenin e calcule v_o

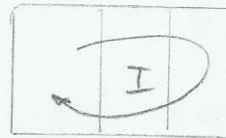
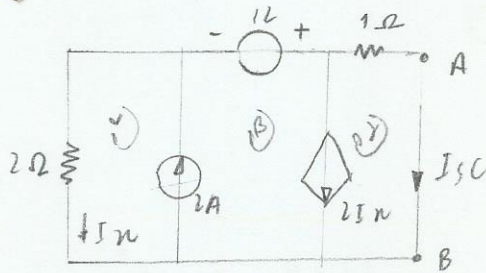


Solução

Fonte dependente \Rightarrow Método Indirecto

I_{SC} ?

$$R_{th} = \frac{V_{oc}}{I_{sc}}$$



equação de I : $2\alpha + \gamma = 12$

$$\beta - \alpha = 2 \Rightarrow \beta - (-I_x) = 2 \Rightarrow \beta + I_x = 2$$

$$\beta - \gamma = 2I_x$$

$$\beta = 2I_x + \gamma = 2 - I_x$$

$$3I_x = 2 - \gamma$$

$$\gamma = 2 - 3I_x$$

$$2\alpha + \gamma = 12$$

$$-2I_x + 2 - 3I_x = 12$$

$$-5I_x = 10$$

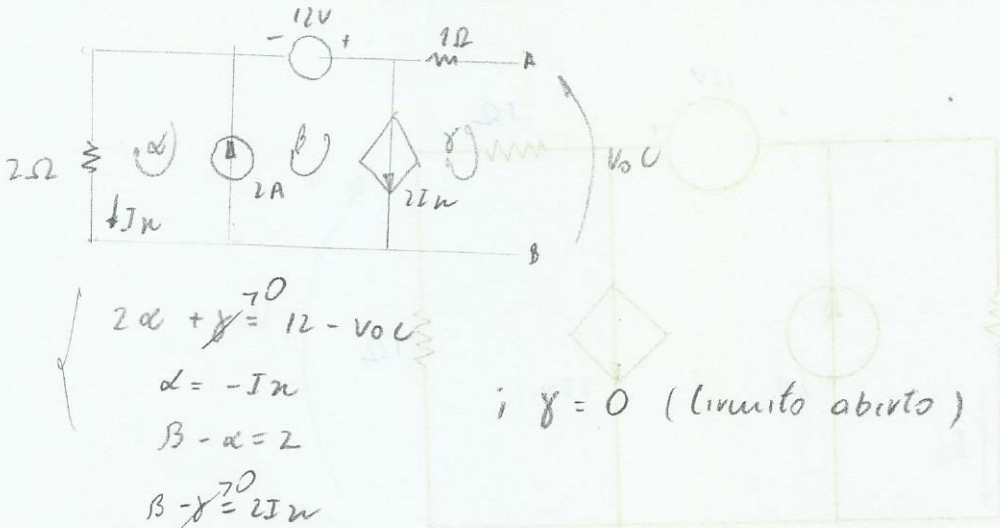
$$I_x = -2A$$

$$2\alpha + \gamma = 12 \quad ; \quad \alpha = -I_n = 2$$

$$\gamma = 12 - 2\alpha$$

$$= 12 - 2 \cdot 2 \quad \therefore \gamma = 8 \quad \therefore I_{sc} = 8A$$

V_{OC} :



$$2\alpha + \gamma = 12 - V_{OC}$$

$$\alpha = -I_n$$

$$\beta - \alpha = 2$$

$$\beta - \gamma = 2I_n$$

$$\alpha = -I_n$$

$$\beta - \alpha = 2$$

$$2I_n - (-I_n) = 2$$

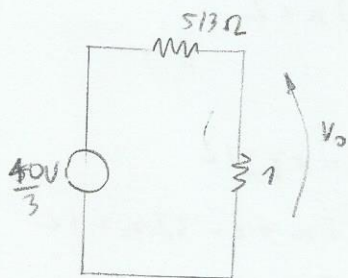
$$3I_n = 2 \quad \rightarrow \quad I_n = \frac{2}{3}$$

$$\alpha = -\frac{2}{3}$$

$$2\alpha = 12 - V_{OC}$$

$$V_{OC} = 12 - 2\alpha = 12 + 2 \cdot \frac{2}{3} = \frac{36 + 4}{3} = \frac{40}{3} V$$

$$R_{th} = \frac{V_{OC}}{I_{sc}} = \frac{\frac{40}{3}}{8} = \frac{5}{3} \Omega$$

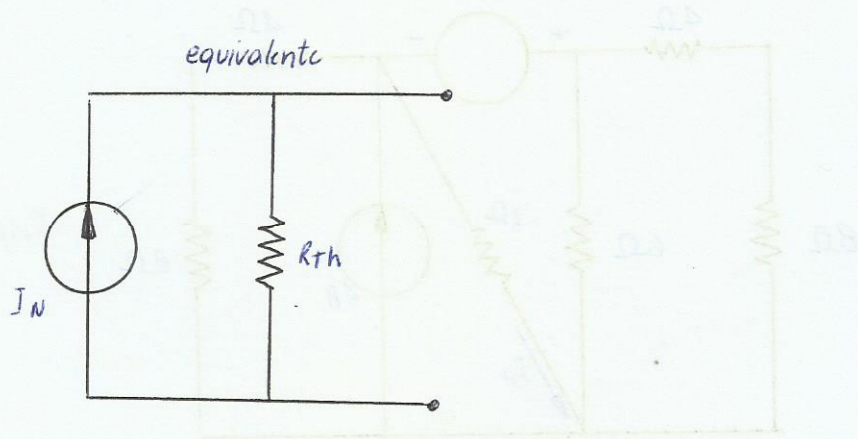


$$V_0 = \frac{1}{1 + \frac{5}{3}} \cdot \frac{40}{3}$$

$$V_0 = \frac{8}{8} \cdot \frac{40}{3}$$

$$V_0 = \underline{5V}$$

Teorema de Norton

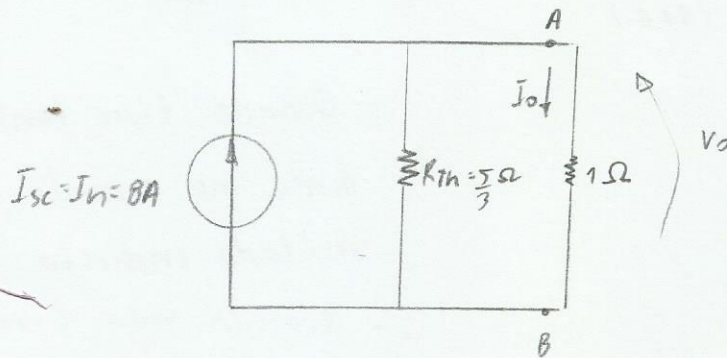


exercício anterior (5.46) e resolvemos por Norton

Como há ponto dependente $\left\{ \begin{array}{l} I_{sc} = 8A \\ V_{oc} = \frac{40}{3} V \end{array} \right.$

$$R_{Th} = \frac{V_{oc}}{I_{sc}} = \frac{40}{3} \div 8 = \frac{5}{3} \Omega$$

equivalente de Norton

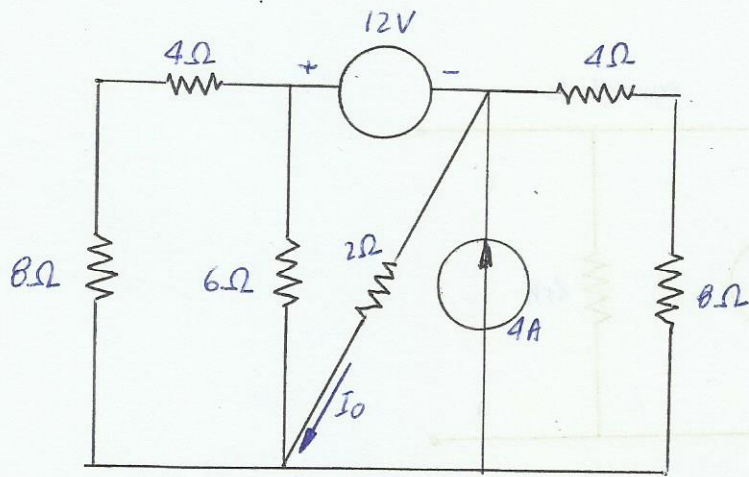


$$I_0 = \left(\frac{5}{3} : \left(\frac{5}{3} + 1 \right) \right) \times 8$$

$$\left(\frac{5}{3} : \frac{8}{3} \right) \cdot 8 = \frac{5}{8} \cdot 8 = 5 A$$

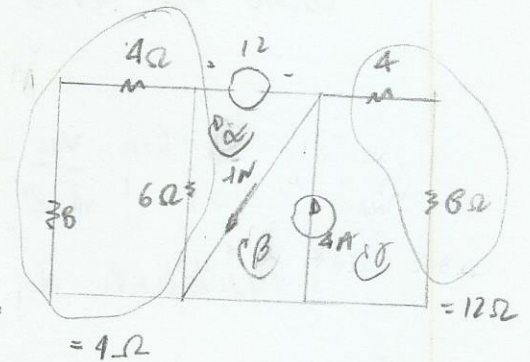
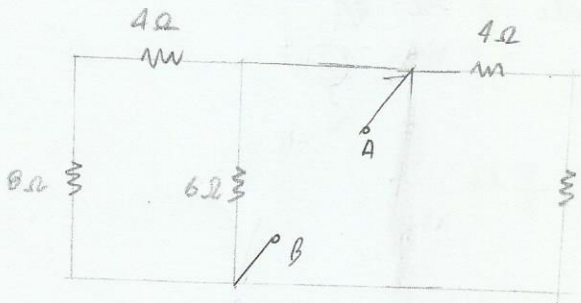
$$V_0 = 5 \cdot 1 = \underline{5V}$$

5.50 Determine I_0 aplicando Norton



Resp: $R_{th} = 3\Omega$
 $I_N = 1A$
 $I_0 = \frac{3}{5} A$

Solução



$$R_{th} = (4+8) \parallel 6 \parallel (4+8)$$

$$R_{th} = 3\Omega$$

- Quando tiver fonte dependente no circuito, usar método indiano
- Quando não tiver, abra as correntes e feche as tensões em curto

→ equações:

$$4\alpha + 12\gamma = -12 \quad \alpha + 3\gamma = -3$$

$$4\alpha = -12$$

$$\alpha = -3$$

$$\gamma - \beta = 4$$

$$I_N = \alpha - \beta$$

$$\gamma = \frac{-3 - \alpha}{3} = \frac{-3 - (-3)}{3} = 0$$

$$\beta = \gamma - 4 = 0 - 4 = -4$$

$$I_N = -3 - (-4) = 1A$$

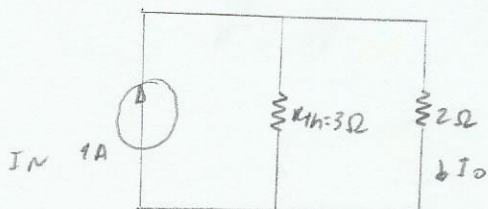
Supostos

U5.36 pg.218 $R_{th} = 4\Omega$
 $V_{th} = 16V$ $V_0 = 8V$

5.45 pg.220 $V_{0G} = 24V$ $V_0 = 6V$
 $I_N = 12A$

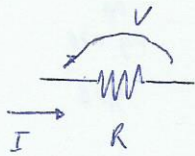
U5.53 pg.221 Resp: $R_{th} = \frac{11}{5}\Omega$
 $I_N = 6A$ $I_0 = 1A$

U5.52 pg.221 $R_{th} = \frac{18}{5}\Omega$ $I_0 = 3A$
 $I_N = 8A$



$$I_0 = \frac{3}{3+2} = \frac{3}{5} A$$

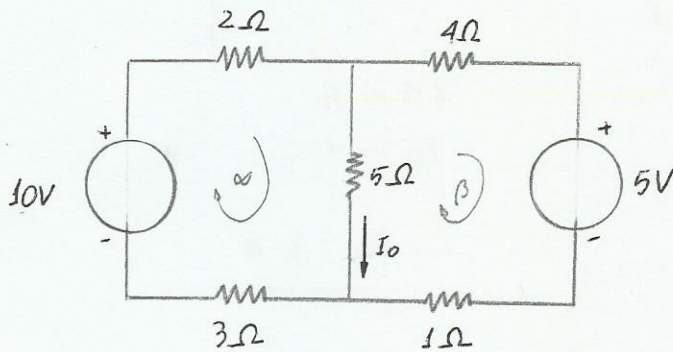
Linearidade



$$\frac{V}{I} = \frac{2V}{2I} = \frac{mV}{mI} = R$$

existe uma variação linear quando R é constante.

Ex:



$$\begin{cases} 10\alpha - 5\beta = 10 \\ 10\beta - 5\alpha = -5 \end{cases} \sim \begin{cases} 10\alpha - 5\beta = 10 \\ -10\alpha + 20\beta = -10 \end{cases} \quad \begin{matrix} 15\beta = 0 \\ \beta = 0 \end{matrix} \quad \therefore \alpha = 1$$

$$I_0 = \alpha - \beta = 1 - 0 \quad \therefore I_0 = 1A$$

Se dobrarmos o valor das fontes

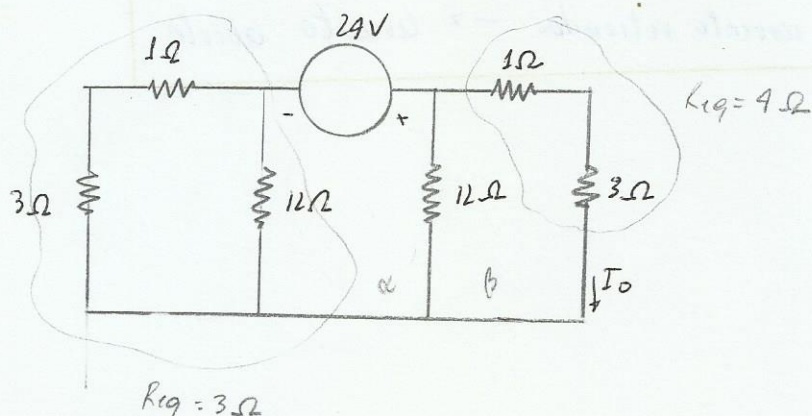
$$10V \rightarrow 20V$$

$$5V \rightarrow 10V$$

$$\begin{cases} 10\alpha - 5\beta = 20 \\ 10\beta - 5\alpha = -10 \end{cases} \sim \begin{cases} 10\alpha - 5\beta = 20 \\ -10\alpha + 20\beta = -10 \end{cases} \quad \therefore \beta = 0 \text{ e } \alpha = 2$$

$$I_0 = \alpha - \beta = 2 - 0 = 2 \quad \therefore I_0' = 2A$$

E. 5.3 Use a linearidade e a suposição que $I_0 = 1A$ e calcule o verdadeiro valor de I_0



Solução

$$12I = 4I_0$$

$$I = \frac{4I_0}{12} = \frac{I_0}{3}$$

$$I_T = \frac{I_0}{3} + I_0 = \frac{4I_0}{3}$$

$$R_{eq} = 3 + (12 \parallel 4) = 6$$

Admitindo $I_0 = 1$

$$I_T = \frac{4}{3}$$

$$V' = \frac{4}{3} \cdot 6 = 8V$$

$$24 - 8$$

$$I_0 = 1$$

$$\therefore I_0 = 3 \text{ A}$$

Sugestões

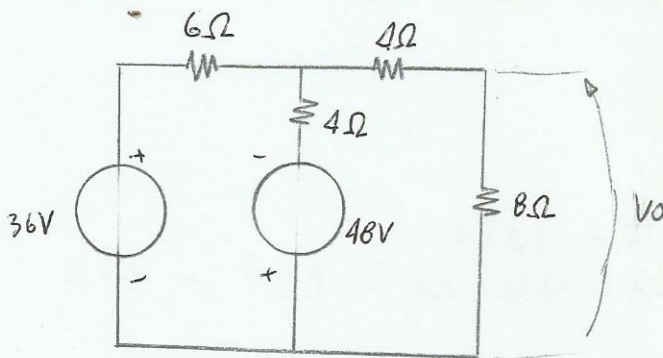
Linearidade:

Ex	Pg
E 5.1	Pg 176
5.2	178
5.4	210

Superposição de efeitos

Qualquer valor de tensão ou correntes nos resistores do circuito, pode ser obtido parcialmente a partir de cada fonte que o compõe.

Ex: E5.4 pg 184

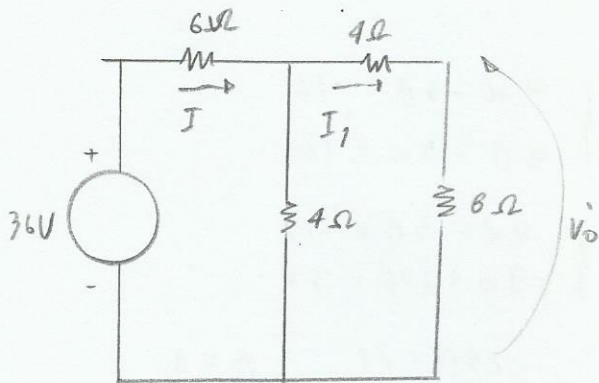


Método:

A fonte de tensão retirada \rightarrow curto circuito

A fonte de corrente retirada \rightarrow circuito aberto

Influência de 36V



$$R_{eq} = 6 + 4 \parallel (4 + 8)$$

$$= 6 + 3 = 9 \Omega$$

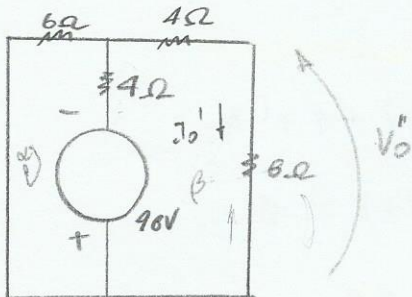
$$I = \frac{36}{9} = 4 \text{ A}$$

$$V_o = 8 \cdot I$$

$$I_1 = \frac{4}{4+8} \cdot 4 = 1 \text{ A}$$

$$V_o' = 8 \text{ V}$$

Influência de 48V



$$R_{eq} = 4 + 6 \parallel 12 = 8$$

$$I_T = \frac{48}{8} = 6 \text{ A}$$

$$V_o'' = 8 \cdot 2 = 16 \text{ V}$$

$$I_0' = \frac{6}{18} \cdot 6 = 2 \text{ A}$$

0V

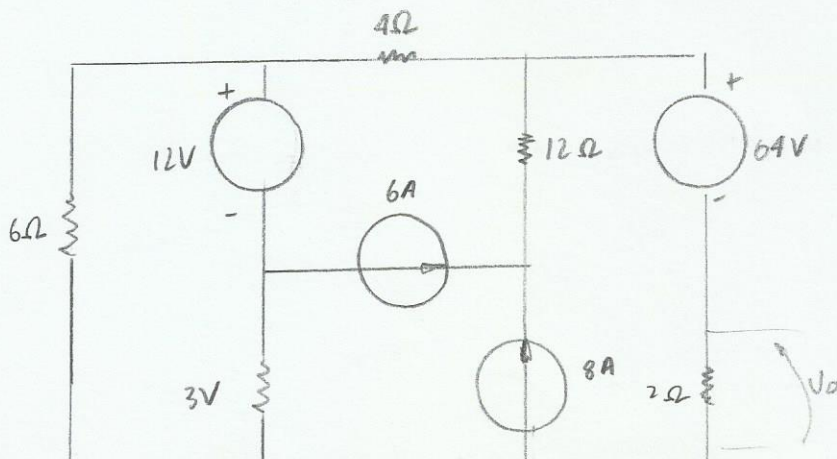
$$\begin{cases} 10\alpha - 4\beta = 98 \\ 16\beta - 4\alpha = -98 \end{cases} \sim \begin{cases} 40\alpha - 16\beta = 192 \\ -4\alpha + 16\beta = -98 \end{cases} \quad \begin{matrix} 36\alpha = 192 \\ \alpha = 4 \end{matrix}$$

$$\beta = \frac{10 \cdot 4 - 98}{4} = -2 \quad \therefore V'' = 8 \cdot (-2) = -16 \text{ V}$$

$$V_o = V_o' + V_o'' = 8 + (-16) = -8 \text{ V} \quad \therefore \underline{V_o = -8 \text{ V}}$$

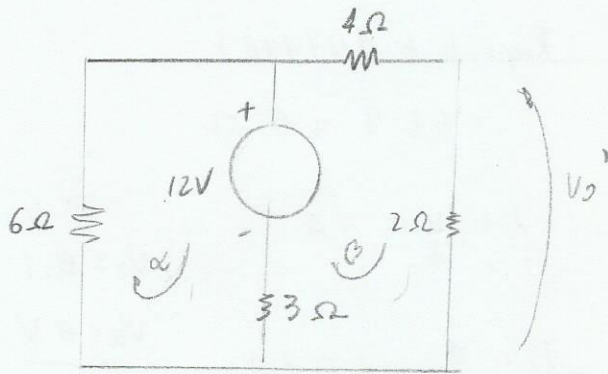
5.14 pg. 213

Aplique superposição de efeitos e calcule V_o



$$R: V_o = 4 \text{ V}$$

Influência de 12V



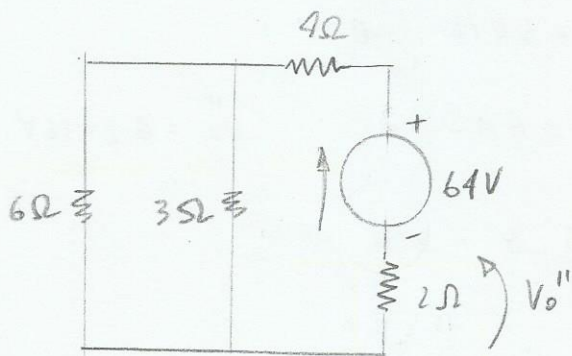
$$\begin{cases} 9\alpha - 3\beta = -12 \\ 9\beta - 3\alpha = 12 \end{cases}$$

$$\begin{cases} 9\alpha - 3\beta = -12 \\ -9\alpha + 27\beta = 36 \end{cases}$$

$$24\beta = 24 \quad \therefore \beta = 1$$

$$V_0' = 1 \cdot 2 = 2V$$

Influência de 64V



$$R_{eq} = (6 \parallel 3) + 4 + 2$$

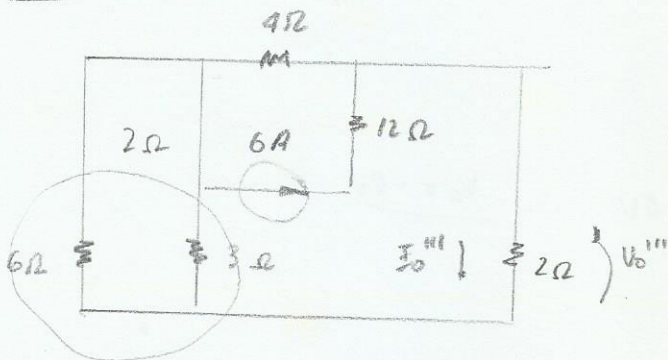
$$= 2 + 4 + 2 = 8$$

$$I_T = \frac{64}{8} = 8A$$

$$V_0'' = 8 \cdot 2 = -16V$$

Temos que calcular com as fontes de corrente

6A



6V

8A

$V_0 = 12$

$$V = V_0 + V_1 + V_2 + V_3 = 0V$$

Matéria de prova

3.54 = D 6V

- Capítulo 3

Análise de laços

- Capítulo 5

Linearidade

Superposição de Efeitos

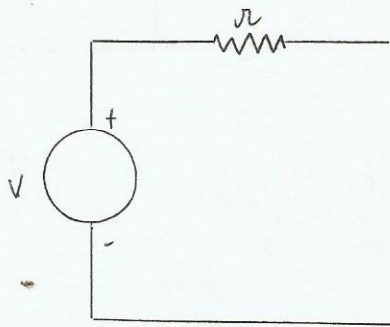
Transformação de fontes

Teorema de Thevenin e Norton

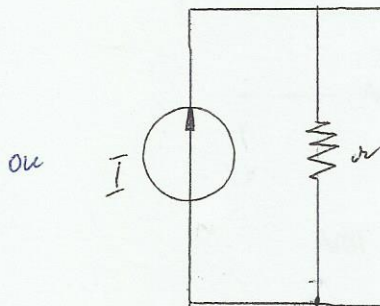
Transfêrência Max de Potência

Transformação de fontes

As fontes independentes chamadas de fontes reais são representadas com a sua resistência.

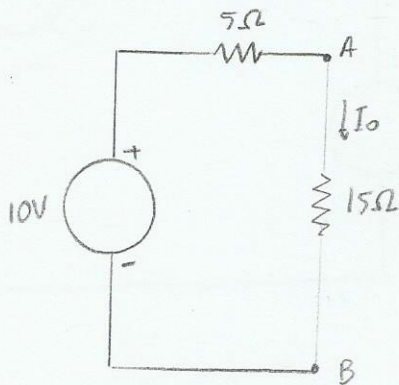


Fonte real de Tensão

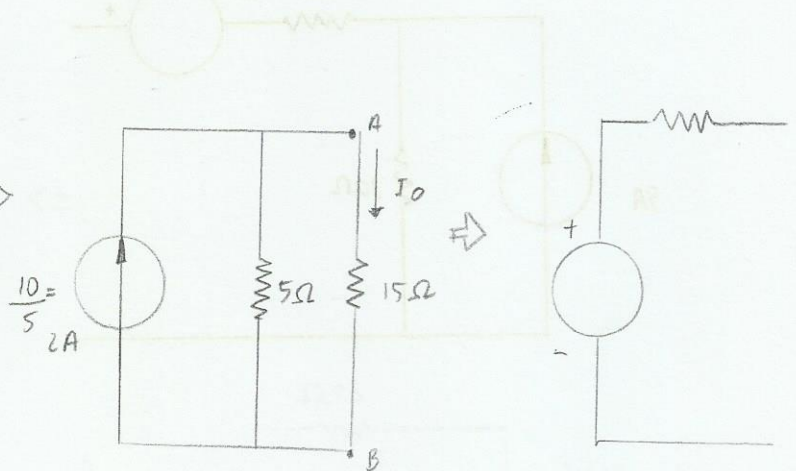


Fonte real de corrente

Conversão

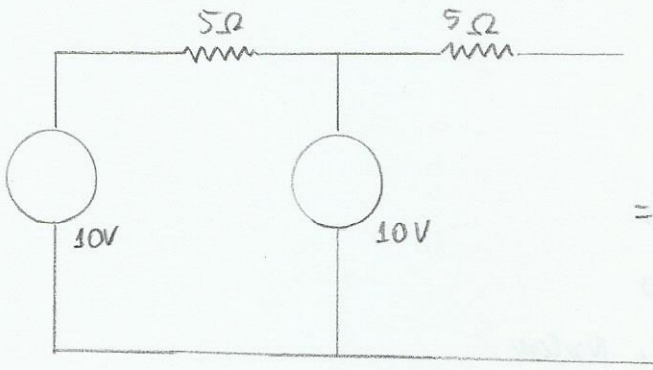


$$I_0 = \frac{10}{5+15} = 0,5 A$$

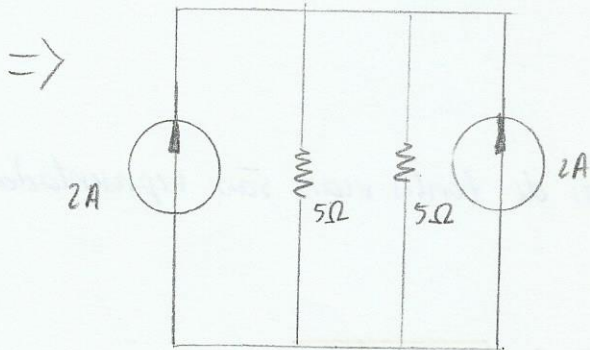


$$I_0 = \frac{5}{15+5} \cdot 2 = 0,5 A$$

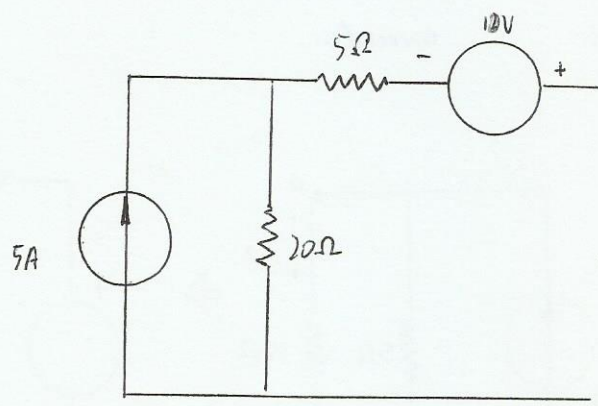
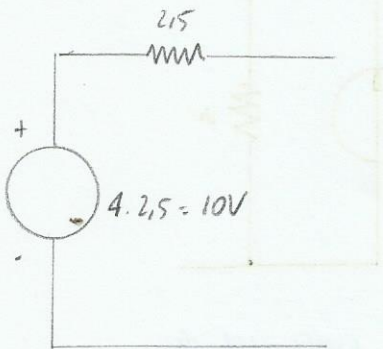
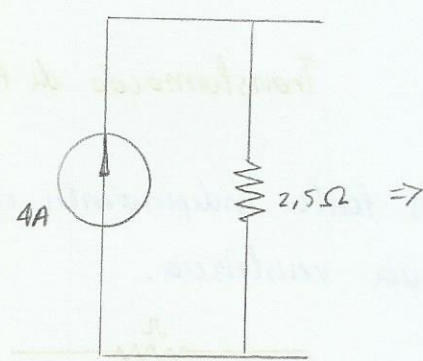
Vantagens da transformação



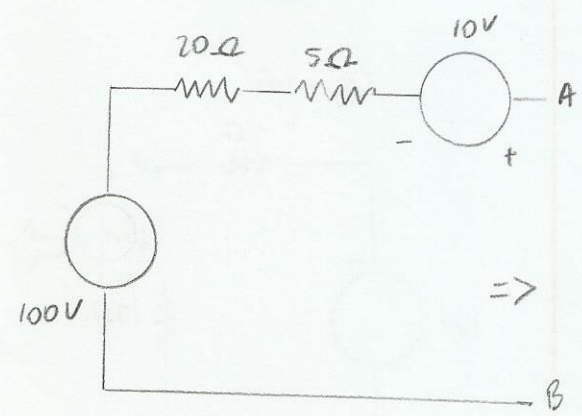
=>



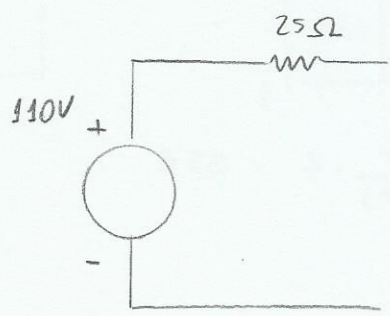
=>

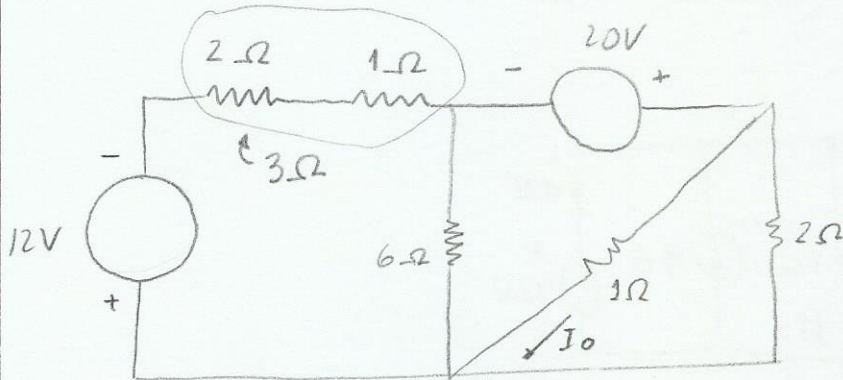
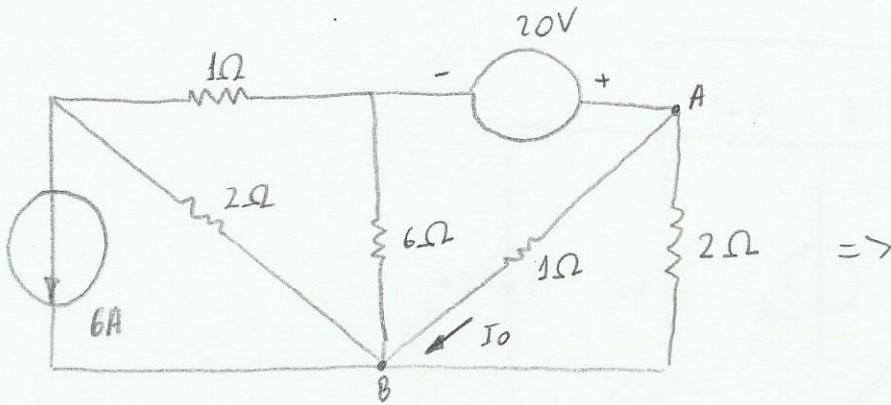


=>

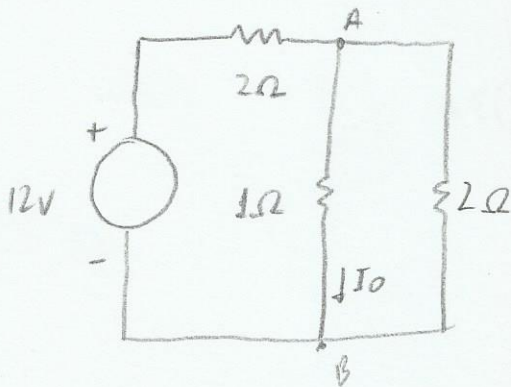
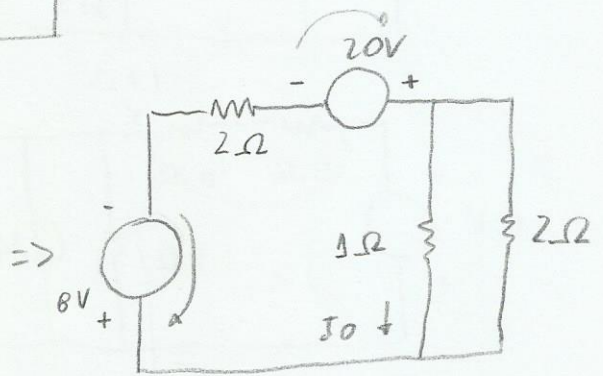
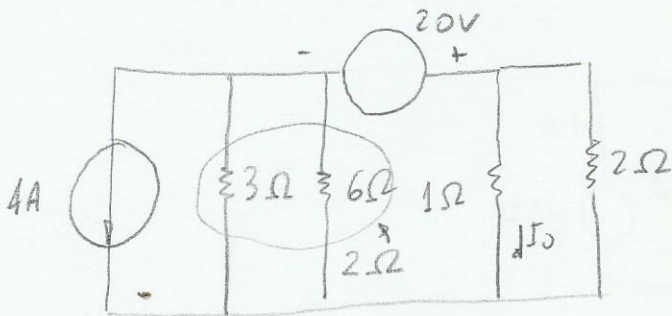


=>





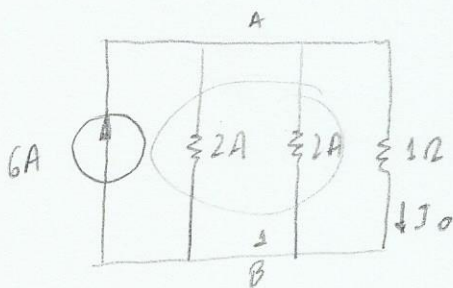
Para uma fonte de tensão
ou fonte de corrente,
ela tem que ter uma resistên-
cia em série



$$V_{AB} = \frac{2}{3} \div \left(\frac{2}{3} + 2\right) \cdot 12 = 3$$

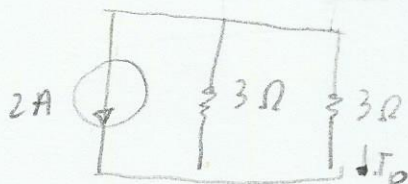
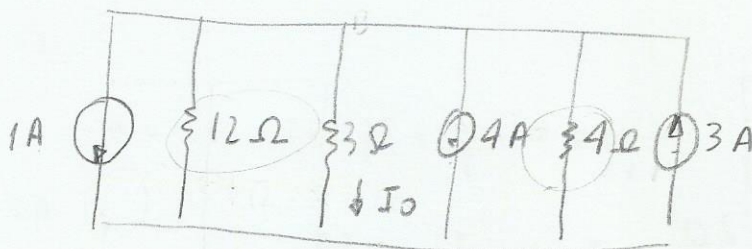
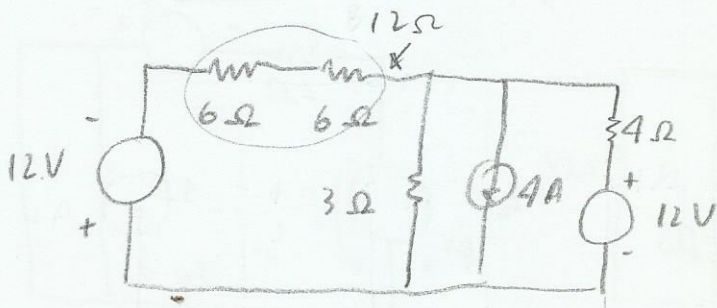
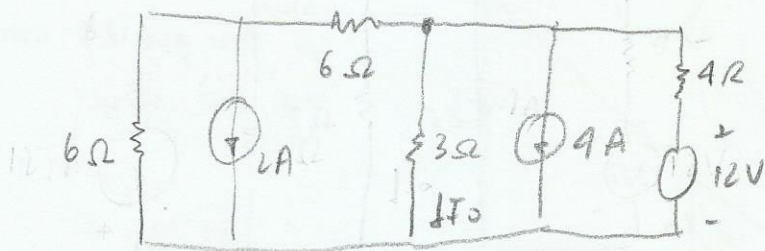
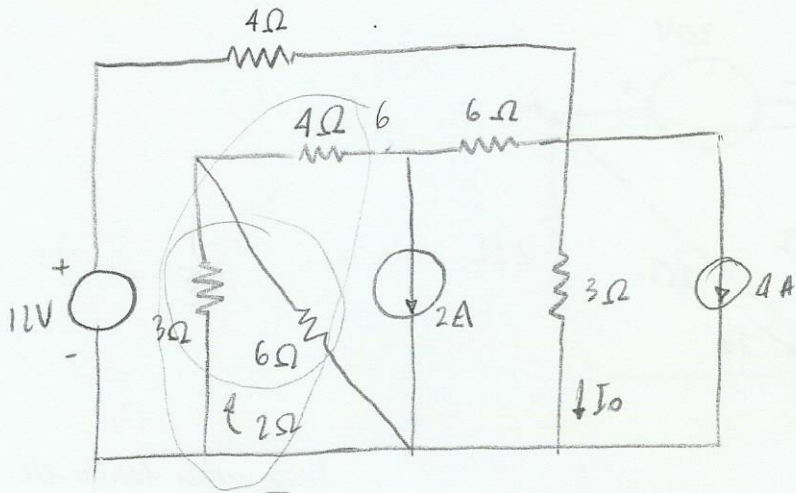
$$I_0 = \frac{3}{1} = \underline{\underline{3A}}$$

0V



$$I_0 = \frac{1}{1+1} \cdot 6 = \underline{\underline{3A}}$$

5.23 Aplique transformação de fonte para determinar I_0



$I_0 = -1A$

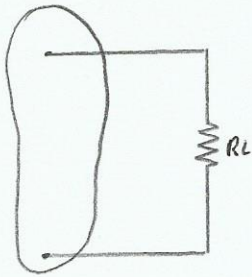
Sugestão de transformadas

5.20 pg 214 $V_0 = 10V$

5.22 " $I_0 = 2A$

Transferência Máxima de Potência

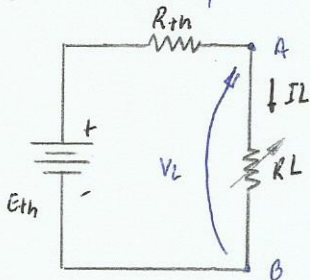
Seja um circuito qualquer



Qual o valor de R_L para que reciba a máxima potência transferida pelo circuito?

$$R_L = ? \Rightarrow R_L \text{ seja máxima}$$

O circuito pode ser representado por um equivalente de Thevenin



$$I_L = \frac{E_{th}}{R_{th} + R_L}$$

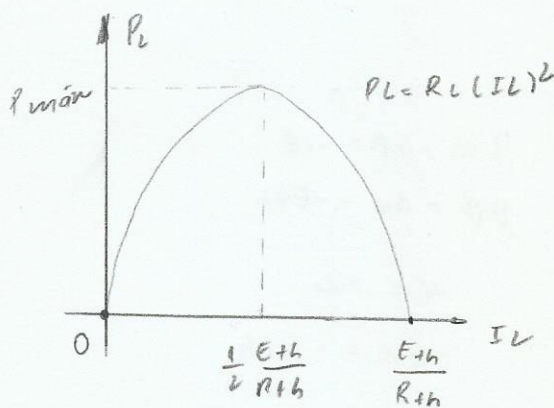
$$P_L = R_L \cdot (I_L)^2$$

R_L é variável

a) $R_L \gg R_{th} \rightarrow \infty$ logo $I_L \rightarrow 0$ e $P_L = 0$

b) $R_L \approx 0$ logo $I_L = \frac{E_{th}}{R_{th}}$ e $P_L = 0$

gráfico de $P_L \times I_L$



A potência máxima (P_{max}) acontece quando:

$$I_L = \frac{E_{th}}{2R_{th}} = \frac{E_{th}}{R_{th} + R_{th}} = R_L$$

Conclusão: R_L recebe a máxima potência transferida do circuito quando

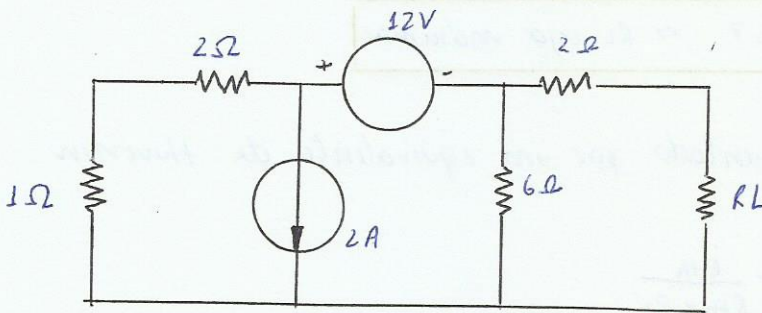
$$R_L = R_{th}$$

Exercícios

Dado o circuito. Pedem-se (15.59 pg 222)

a) o valor de R_L para que se tenha a máxima potência transferida pelo circuito.

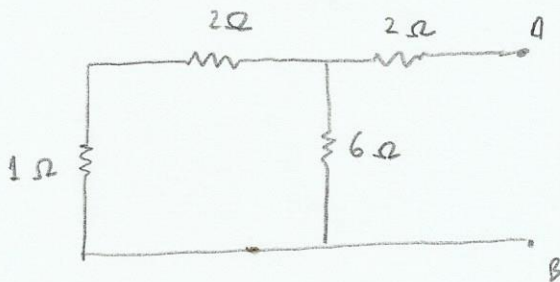
b) O valor dessa potência transferida



Solução:

(a)

$R_{th} = ?$

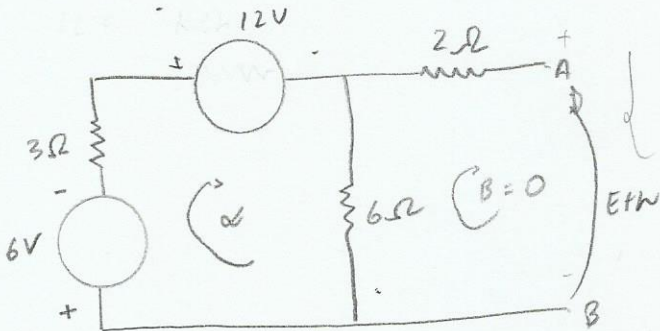


$R_{th} = 4 \Omega$

$R_L = R_{th} = 4 \Omega$

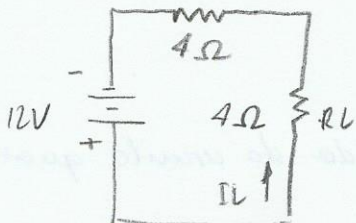
(b)

$E_{th} = ?$



$$\begin{aligned} 9\alpha - 6\beta &= -18 \\ 6\beta - 6\alpha &= -E_{th} \\ \alpha &= -2 \\ -6\alpha &= -E_{th} \\ \therefore E_{th} &= -12V \end{aligned}$$

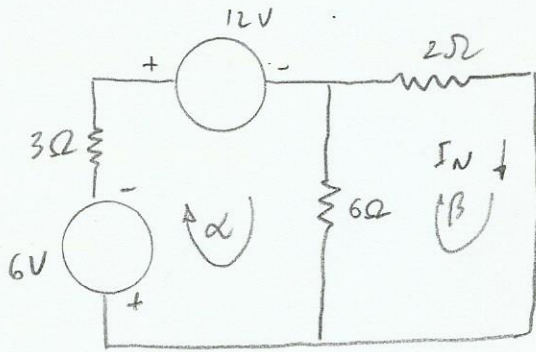
equivalente de thevenin



$P = R_L \cdot (I_L)^2 = 4 \cdot \left(\frac{12}{8}\right)^2$

$\therefore P = 9W$

Solução por Norton



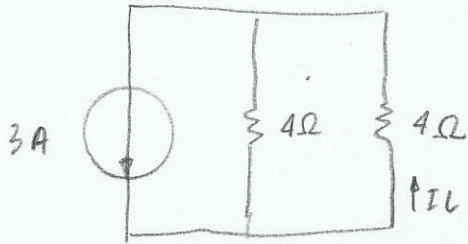
$$\begin{cases} 9\alpha - 6\beta = -18 \\ 8\beta - 6\alpha = 0 \end{cases}$$

$$\begin{cases} 9\alpha - 6\beta = -18 \\ -6\alpha + 8\beta = 0 \end{cases} \sim \begin{cases} 18\alpha - 12\beta = -36 \\ -18\alpha + 24\beta = 0 \end{cases}$$

$$12\beta = -36$$

$$\therefore \beta = -3$$

$\therefore I_N = \beta = -3A$



$\therefore Z_L = 1\Omega \quad \therefore P_L = \underline{9W}$

Sugestão:

- E. 5.19
 - E. 5.20
- pg 204

Circuitos eléctricos

Técnicas de Análisis Nodal de lazo

Análisis de lazo

Ejercicios

3.40 P no $R=5\Omega = ?$

$$\begin{cases} 6\alpha - 2\beta = 20 - 12 \\ 8\beta - 2\alpha = 12 \end{cases} \sim \begin{cases} 6\alpha - 2\beta = 8 \\ -2\alpha + 8\beta = 12 \end{cases} \sim \begin{cases} 6\alpha - 2\beta = 8 \\ 22\beta = 44 \end{cases}$$

$$\therefore \beta = 2 \quad \alpha = 2$$

$$I = 2 \quad \therefore P = V \cdot I = R \cdot I^2 = 5 \cdot 2^2 \quad \therefore \underline{P = 20W}$$

3.42 Determine I_0 :

$$\begin{cases} 2\alpha + 3\beta - 2\gamma = 12 - 6 \\ 3\gamma - 2\beta = 6 - 4 \end{cases} \sim \begin{cases} 2\alpha + 3\beta - 2\gamma = 6 \text{ (I)} \\ -2\beta + 3\gamma = 2 \end{cases} \quad \begin{cases} \alpha - \beta = 2 \\ \alpha = 2 + \beta \end{cases}$$

$$\text{(I)} \quad \begin{cases} 2(2 + \beta) + 3\beta - 2\gamma = 6 \\ 4 + 2\beta + 3\beta - 2\gamma = 6 \\ 5\beta - 2\gamma = 2 \end{cases} \quad \begin{cases} 5\beta - 2\gamma = 2 \text{ (x3)} \\ -2\beta + 3\gamma = 2 \text{ (x1)} \end{cases} \quad \begin{cases} 5\beta - 2\gamma = 2 \\ 11\beta = 10 \end{cases}$$

$$\therefore \beta = \frac{10}{11} \quad \therefore I_0 = \frac{10}{11} \text{ A}$$

3.50) Determine V_0

$$\begin{cases} 9\alpha - 3\gamma = -12 \\ 4\beta + 2\theta + 3\gamma - 3\alpha = 12 - 64 \end{cases} \quad \begin{cases} \gamma - \beta = 6 \\ \theta - \gamma = 8 \end{cases} \quad \begin{cases} \beta = \gamma - 6 \\ \theta = \theta + \gamma \end{cases}$$

$$4(\gamma - 6) + 2(\theta + \gamma) + 3\gamma - 3\alpha = -52$$

$$4\gamma - 24 + 16 + 2\gamma + 3\gamma - 3\alpha = -52$$

$$9\gamma - 3\alpha = -44$$

$$\begin{cases} 9\alpha - 3\gamma = -12 \\ -3\alpha + 9\gamma = -44 \end{cases} \sim \begin{cases} 9\alpha - 3\gamma = -12 \\ 24\gamma = -144 \end{cases}$$

$$\therefore \gamma = -6$$

$$\theta = \theta + \gamma = \theta + (-6) \quad \therefore \theta = 2 \quad \therefore \underline{V_0 = 4V}$$

3.64 Determine V_0

$$\begin{cases} 3\alpha + 3\gamma - \beta - \theta - \lambda = 0 \\ 3\theta + 4\lambda - 2\gamma - 2\beta = 0 \end{cases}$$

$$\begin{cases} \alpha - \gamma = 1 \rightarrow \alpha = 1 + \gamma \\ \beta = 2V_0 = 2 \cdot 1 \cdot (\lambda - \gamma) = 2\lambda - 2\gamma \\ \lambda - \theta = 4 \quad \theta = \lambda - 4 \end{cases}$$

$$3(1 + \gamma) + 3\gamma - 2(\lambda - \gamma) - (\lambda - 4) - \lambda = 0$$

$$3 + 3\gamma + 3\gamma - 2\lambda + 2\gamma - \lambda + 4 - \lambda = 0$$

$$6\gamma - 4\lambda = -7$$

$$\begin{cases} 6\gamma - 4\lambda = -7 \\ 2\gamma + 3\lambda = 12 \end{cases}$$

$$3(\lambda - 4) + 4\lambda - 2\gamma - 2(2(\lambda - \gamma)) = 0$$

$$3\lambda - 12 + 4\lambda - 2\gamma - 4\lambda + 4\gamma = 0$$

$$3\lambda + 2\gamma = 12$$

$$\begin{cases} 6\gamma - 4\lambda = -7 \\ -16\lambda = -55 \end{cases}$$

$$\lambda = \frac{55}{16}$$

$$V_0 = 1 \cdot \frac{55}{16} = \underline{\underline{3,4375 \text{ V}}}$$

3.43 Determine I_0

$$2\beta + 3\gamma = 12 \quad ; \quad \beta - \gamma = 4 \quad \alpha - \beta = 2 \quad \therefore \gamma = \alpha - 2 - 4$$

$$\gamma = \beta - 4 \quad \beta = \alpha - 2 \quad \gamma = \alpha - 6 \quad \text{e} \quad \beta = \alpha - 2$$

$$2(\alpha - 2) + 3(\alpha - 6) = 12$$

$$2\alpha - 4 + 3\alpha - 18 = 12$$

$$5\alpha = 34 \quad \therefore \alpha = \frac{34}{5} = 6,8 \quad \therefore \underline{\underline{I_0 = 6,8 \text{ A}}}$$

3.55 Determine V_0 :

$$3\alpha + \beta - \theta + \gamma = 24 \quad ; \quad \beta - \alpha = 4 \quad \therefore \beta = 4 + \alpha \quad ; \quad \theta = -2 \quad \text{e} \quad \gamma = -4$$

$$3\alpha + 4 + \alpha - (-2) - (-4) = 24$$

$$4\alpha = 14 \quad \therefore \alpha = \frac{14}{4} = \frac{7}{2}$$

$$I_0 = \alpha - \theta = \frac{7}{2} - (-2) = \underline{\underline{11 \text{ A}}}$$

3.61) Determina V_0

$$2\alpha + 4\beta = 12 \quad \beta - \alpha = 2V_0 = 2 \cdot (2\alpha)$$

$$\alpha + 2\beta = 6 \quad \beta - \alpha = 4\alpha \quad \alpha = \frac{1}{5}\beta$$

$$3\alpha - 3\beta = V_0$$

$$\left. \begin{array}{l} 2 \cdot \frac{1}{5}\beta + 4\beta = 12 \\ 2\beta + 20\beta = 60 \end{array} \right\} \begin{array}{l} 22\beta = 60 \\ \beta = \frac{60}{22} = \frac{30}{11} \end{array} \quad V_0 = 3 \frac{30}{11} = \frac{90}{11} V$$

Enunciados saltantes

3.41 Determinar V_0

$$\left. \begin{array}{l} 2\alpha - \beta = 4 \\ 2\gamma - \beta = -4 \end{array} \right\} \beta = 2 \quad \gamma = \frac{-4+2}{2} = -1 \quad V_0 = -1 \cdot 1 = \underline{-1V}$$

3.44 Determinar I_0

$$5\alpha - 2\beta - 2\gamma = 0 \quad ; \quad \beta = 2 \quad ; \quad \gamma = -4 \quad ; \quad \gamma - \beta = I_0$$

$$\gamma - \beta = I_0$$

$$I_0 = -4 - 2 = -6 \quad \therefore \quad \underline{I_0 = 6A}$$

3.45 Determinar I_0

$$3\gamma - \beta = 12 \quad ; \quad \beta = -2 \quad ; \quad \alpha = 4 \quad ; \quad I_0 = \beta - \gamma$$

$$\gamma = \frac{12 + \beta}{3} = \frac{12 - 2}{3} = \frac{10}{3}$$

$$I_0 = \beta - \gamma$$

$$= -2 - \frac{10}{3} = \frac{-16}{3} \quad \therefore \quad \underline{I_0 = \frac{-16}{3} A}$$

3.46 Determina V_0

$$2\alpha + 3\beta = 12 \quad ; \quad \beta - \alpha = 2 \quad \alpha = \beta - 2$$

$$2(\beta - 2) + 3\beta = 12$$

$$2\beta - 4 + 3\beta = 12$$

$$5\beta = 16 \quad \therefore \quad \beta = \frac{16}{5}$$

$$V_0 = \frac{16}{5} \cdot 2 = \frac{32}{5} V \quad \therefore \quad \underline{V_0 = \frac{32}{5} V}$$

3.47 Determina V_0

$$\left. \begin{array}{l} 12\alpha - 6\beta = 12 \\ 12\gamma - 6\beta = -12 \end{array} \right\} \sim \left. \begin{array}{l} 2\alpha - \beta = 2 \\ 2\gamma - \beta = -2 \end{array} \right\} \beta = 6 \quad ; \quad I_0 = \beta - \gamma$$

$$\gamma = \frac{-2 + 6}{2} = \frac{4}{2} = 2$$

$$I_0 = 6 - 2 \quad \therefore \quad \underline{I_0 = 4}$$

$$\underline{V_0 = 24V}$$

3.48 Determinar V_0

$$\begin{cases} 8I_1 - 2I_2 - 4I_3 = 0 \\ 5I_3 - 4I_1 - I_2 = 12 \end{cases} \quad I_2 = 4; \quad I_0 = I_2 - I_3$$

$$\begin{cases} 8I_1 - 4I_3 = 8 \\ -4I_1 + 5I_3 = 16 \end{cases} \sim \begin{cases} 8I_1 - 4I_3 = 8 \\ 6I_3 = 40 \end{cases} \quad \therefore I_3 = \frac{40}{6} = \frac{20}{3}$$

$$I_0 = 4 - \frac{20}{3} = \frac{-8}{3} \quad \therefore V_0 = \frac{-8}{3} \text{ V}$$

3.49 Determinar V_0

$$\begin{cases} 18\beta - 6\alpha - 6\gamma = 0 \\ 6\alpha - 6\beta - 6\gamma = 12 \end{cases} \sim \begin{cases} 3\beta - \alpha - \gamma = 0 \\ \alpha - \beta - \gamma = 2 \end{cases}; \quad \begin{cases} \gamma - \alpha = 6 \\ \gamma = 6 + \alpha \end{cases}$$

$$3\beta - \alpha - 6 + \alpha = 0$$

$$3\beta = 6 \quad \therefore \beta = 2 \quad V_0 = 6 \cdot 2 \quad \therefore V_0 = 12 \text{ V}$$

3.50 Determinar a potência dissipada no resistor de 2Ω

$$\begin{cases} 3\alpha - \gamma - 2\theta = 6 \\ 3\beta - \gamma - \theta = 0 \end{cases}; \quad \gamma = 2 \quad \theta = -2 \quad I = \theta - \alpha$$

$$3\alpha - 2 + 4 = 6$$

$$\alpha = \frac{4}{3}$$

$$I = -2 - \frac{4}{3} = \frac{-6-4}{3} = \frac{-10}{3}$$

$$P = V \cdot I = RI^2 = 2 \cdot \left(\frac{-10}{3}\right)^2 = \frac{200}{9} = \frac{200 \text{ W}}{9}$$

3.51 Determinar I_0

$$2\beta + 3\alpha - 3\gamma = 12$$

$$\beta - \gamma = I_0; \quad \gamma = -4 \quad \beta - \alpha = 2$$

$$2\beta + 3\alpha - 0 = 12 + 12 = 24$$

$$\beta + 4 = I_0 \quad \alpha = \beta - 2$$

$$15\beta + 3\alpha - 0 = 15 + 6 = 21$$

$$\beta = I_0 - 4 \quad \alpha = I_0 - 6$$

$$2(I_0 - 4) + 3(I_0 - 6) - 3(-4) = 12$$

$$2I_0 - 8 + 3I_0 - 18 + 12 = 12$$

$$5I_0 = 26$$

$$I_0 = \frac{26}{5}$$

3.52

$$3\alpha + 2\theta + 2\gamma - 3\beta = 0 \quad ; \quad \beta = 4$$

$$\theta - \alpha = 2 \quad \rightarrow \quad \alpha = \theta - 2$$

$$\gamma - \theta = 2 \quad \gamma = 2 + \theta$$

$$I_0 = \beta - \gamma = 4 - \gamma$$

$$3(\theta - 2) + 2\theta + 2(2 + \theta) - 3 \cdot 4 = 0$$

$$3\theta - 6 + 2\theta + 4 + 2\theta - 12 = 0$$

$$7\theta = 14 \quad \therefore \quad \theta = 2$$

$$I_0 = 4 - \gamma$$

$$I_0 = 4 - (2 + \theta)$$

$$I_0 = 4 - (2 + 2) = \underline{0}$$

3.53

$$2\alpha + \beta + 2\gamma - \theta - 2\lambda = 12 \quad ; \quad \beta - \alpha = 4 \quad I_0 = \gamma - \lambda$$

$$\gamma - \alpha = 2 \quad I_0 = \gamma + 3$$

$$\theta = -6$$

$$\lambda = -3$$

$$\beta = 4 + \alpha$$

$$\gamma = 2 + \alpha$$

$$2\alpha + 4 + \alpha + 2(2 + \alpha) - (-6) - 2(-3) = 12$$

$$2\alpha + 4 + \alpha + 4 + 2\alpha + 6 + 6 = 12$$

$$5\alpha = -8$$

$$\alpha = -\frac{8}{5}$$

$$I_0 = \gamma + 3$$

$$= 2 + \alpha + 3$$

$$= 2 - \frac{8}{5} + 3$$

$$\therefore \quad I_0 = \frac{17}{5} \text{ A}$$

3.54

$$2\alpha - \beta = -12 \quad ; \quad \beta = 4 \quad \theta - \gamma = 2$$

$$\gamma + 2\theta - \beta - \lambda = 12$$

$$\gamma = \theta - 2$$

$$\lambda - \theta = -V_0 \quad \therefore \quad V_0 = \theta$$

$$\theta - 2 + 2\theta - 4 = 12$$

$$3\theta = 18$$

$$\theta = 6$$

$$\therefore \quad \underline{V_0 = 6V}$$

3.56

$$\begin{cases} 3\alpha - \beta - \gamma = 0 \\ \gamma + 2\theta - \alpha - \beta - \cancel{\lambda^0} = -6 \\ \cancel{\lambda^0} - \theta = -V_0 \rightarrow V_0 = \theta \end{cases} ; \beta = -2$$

$$\theta - \gamma = 2 ; \gamma = \theta - 2$$

$$\theta - 2 + 2\theta - \alpha - (-2) = -6$$

$$3\theta - \alpha = -6$$

$$3\theta - \alpha = -6$$

$$3\theta - \left(\frac{\theta - 4}{3}\right) = -6$$

$$3\alpha - \beta - \gamma = 0$$

$$3\alpha - (-2) - (\theta - 2) = 0$$

$$\frac{9\theta - \theta + 4}{3} = -6$$

$$3\alpha + 2 - \theta + 2 = 0$$

$$8\theta = -18 - 4$$

$$\alpha = \frac{\theta - 4}{3}$$

$$\theta = \frac{-22}{8} = \frac{-11}{4}$$

3.57-)

$$\begin{cases} 4\alpha - 2\beta - 2\gamma = 12 \\ 4\gamma - 2\alpha - \theta = 0 \end{cases} ; \beta = 2 \quad \theta = -1 \quad I_0 = \alpha - \gamma$$

$$\begin{cases} 4\alpha - 2\gamma = 16 \\ -2\alpha + 4\gamma = -1 \end{cases} \sim \begin{cases} 4\alpha - 2\gamma = 16 \\ 6\gamma = 14 \end{cases} \quad \gamma = \frac{14}{6} = \frac{7}{3}$$

$$\alpha = \frac{16 + 2\gamma}{4} = \left(16 + \frac{14}{3}\right) \div 4 = \frac{48 + 14}{12} = \frac{62}{12} = \frac{31}{6}$$

$$I_0 = \frac{31}{6} - \frac{7}{3} = \frac{17}{6} \text{ A}$$

3.59-)

$$\begin{cases} 2\beta + 3\theta - \alpha - \gamma - \cancel{2\lambda^0} = 0 ; \alpha = 4 \quad \gamma = -2 \quad \theta - \beta = 1 \\ \cancel{2\lambda^0} - 2\theta = -V_0 \end{cases}$$

$$\beta = \theta - 1$$

$$2(\theta - 1) + 3\theta - 4 - (-2) = 0$$

$$2\theta - 2 + 3\theta - 4 + 2 = 0$$

$$V_0 = 2\theta$$

$$5\theta - 4 = 0$$

$$V_0 = \frac{8}{5} \text{ V}$$

$$\theta = \frac{4}{5}$$

3.60

$$\begin{cases} 4\beta - \alpha - 2\gamma - \theta = -4 \\ 2\alpha + 2\gamma + \theta - 4\beta = -6 \end{cases} \quad ; \quad \begin{cases} \gamma - \alpha = 2 \\ \gamma - \theta = 4 \end{cases} \quad ; \quad I_0 = \theta$$

$$\alpha = \gamma - 2$$

$$\theta = \gamma - 4$$

$$4\beta - (\gamma - 2) - 2\gamma - (\gamma - 4) = -4$$

$$4\beta - \gamma + 2 - 2\gamma - \gamma + 4 = -4$$

$$4\beta - 4\gamma = -10$$

$$\begin{cases} 4\beta - 4\gamma = -10 \\ -4\beta + 5\gamma = 0 \end{cases}$$

$$\gamma = -10$$

$$2(\gamma - 2) + 2\gamma + \gamma - 4 - 4\beta = -6$$

$$2\gamma - 4 + 2\gamma + \gamma - 4 - 4\beta = -6$$

$$-4\beta + 5\gamma = 0$$

$$I_0 = \theta = \gamma - 4 = -10 - 4$$

$$\therefore I_0 = -14 \text{ A}$$

3.62

$$\begin{cases} 6I_1 - 4I_2 = 12 \\ 10I_2 - 4I_1 - 6I_0 = 2V_a \\ 6I_0 - 6I_2 = -V_0 \end{cases} \quad ; \quad V_a = 2I_1$$

$$\begin{cases} 6I_1 - 4I_2 = 12 \\ -4I_1 + 10I_2 = 4I_1 \end{cases} \quad \sim \quad \begin{cases} 6I_1 - 4I_2 = 12 \\ -8I_1 + 10I_2 = 0 \end{cases} \quad \sim \quad \begin{cases} 15I_1 - 10I_2 = 30 \\ -8I_1 + 10I_2 = 0 \end{cases}$$

$$7I_1 = 30$$

$$I_1 = \frac{30}{7} \quad V_a = \frac{2 \cdot 30}{7} = \frac{60}{7}$$

Capítulo 5: Teorema Thevenin

5.46

* Obs.: Quando tiver fonte dependente usar método indireto.

$$R_{th} = \frac{V_{oc}}{I_{sc}}$$

Determinação do I_{sc}

$$2\alpha + \gamma = 12 \quad ; \quad \beta - \alpha = 2 \quad , \quad \alpha = -I_N \quad \therefore \quad \beta = 2 + \alpha = 2 - I_N$$

$$\beta - \gamma = 2I_N = 2 \cdot (-\alpha) \quad \therefore \quad \beta - \gamma = -2\alpha$$

$$\beta - \gamma = -2\alpha$$

$$\gamma = \beta + 2\alpha = 2 - I_N + 2(-I_N) \quad \gamma = 2 - 3I_N$$

$$2(-I_N) + 2 - 3I_N = 12$$

$$-2I_N - 3I_N = 12 - 2$$

$$-5I_N = 10 \quad \therefore \quad I_N = -2 \quad I_{sc} = \gamma$$

$$\beta - \gamma = -2\alpha$$

$$\gamma = \beta + 2\alpha = 2 - I_N + 2(-I_N)$$

$$= 2 + 2 + 2 \cdot (2) \quad \therefore \quad I_{sc} = 6A$$

Determinação do V_{oc}

$$2\alpha + \gamma = 12 - V_{oc} \quad ; \quad \beta - \alpha = 2$$

$$\beta - \gamma = 2I_N \quad ; \quad I_N = -\alpha$$

$$\beta = 2 + \alpha = 2I_N$$

$$2 + \alpha = -2\alpha$$

$$-3\alpha = 2 \quad \alpha = -\frac{2}{3}$$

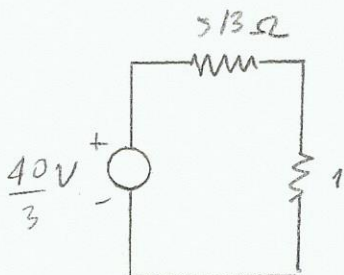
$$2\alpha = 12 - V_{oc}$$

$$V_{oc} = 12 - 2 \cdot \left(-\frac{2}{3}\right)$$

$$= 12 + \frac{4}{3} = \frac{40}{3}$$

$$R_{th} = \frac{40}{3} \div 6$$

$$R_{th} = \frac{40}{27} = \frac{20}{14} = \frac{10}{6} = \frac{5}{3}$$



$$V_o = \frac{1}{\frac{5}{3} + 1} \cdot \frac{40}{3} = 5V$$

● Determine I_0 , assuming $I_0 = 1A$

$$\begin{cases} 15\alpha - 12\beta = 24 \\ 16\beta - 12\alpha = 0 \end{cases} \quad \beta = I_0$$

$$\begin{cases} 5\alpha - 4\beta = 6 \\ -3\alpha + 4\beta = 0 \end{cases} \quad I_T = 4\Omega$$

$$\begin{aligned} 2\alpha &= 6 \\ \alpha &= 4 \end{aligned}$$

$$\begin{aligned} 4I_0 &= 12I' & I_T &= I_0 + \frac{I_0}{3} = \frac{4I_0}{3} \\ I' &= \frac{I_0}{3} \end{aligned}$$

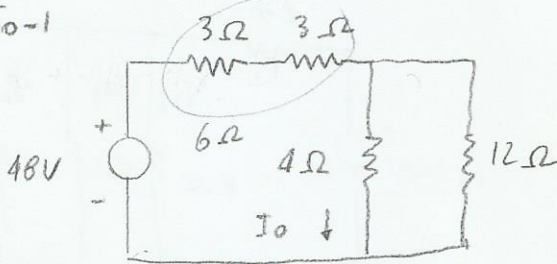
$$I_T' = \frac{4 \cdot 1}{3} = \frac{4}{3}$$

$$4 = 4/3$$

$$I_0 = 1$$

$$I_0 = 4 \cdot \frac{4}{3} = \frac{16}{3} = \underline{5.33A}$$

5.1 $I_0 = 1$



$$4I_0 = 12x$$

$$x = \frac{I_0}{3}$$

$$I_T = \frac{I_0}{3} + I_0 = \frac{4}{3}I_0$$

$$R_T = 6 + (4 \parallel 12) = 6 + 3 \quad \therefore R_T = 9$$

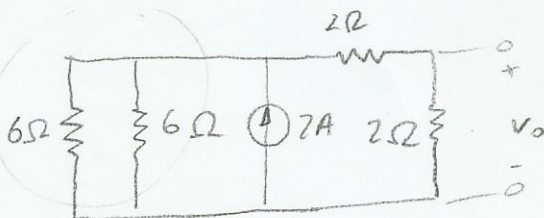
$$I_T = \frac{48}{9} = \frac{16}{3} \quad I_T' = \frac{4}{3}$$

$$\frac{16}{3} = \frac{4}{3}$$

$$I_0 = 1$$

$$I_0 = \frac{16}{3} \div \frac{4}{3} = 4 \quad \therefore \underline{I_0 = 4A}$$

5.2



$$; V_0 = 1V$$

$$I_0 = \frac{V_0}{2} \quad I_0' = \frac{1}{2}$$

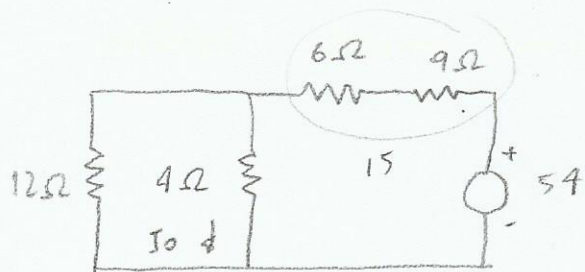
$$I_0 = \frac{6}{7}$$

$$\frac{6}{7} = \frac{1}{2}$$

$$V_0 = 1$$

$$\therefore V_0 = \frac{6}{7} \div \frac{1}{2}$$

$$\therefore \underline{V_0 = \frac{12}{7} V}$$



$$I_T = \frac{54}{(12 \parallel 4) + 15} = \frac{54}{3 + 15} = 3$$

$$\frac{4}{3} = 3$$

$$1 = I_0$$

$$12x = 4I_0$$

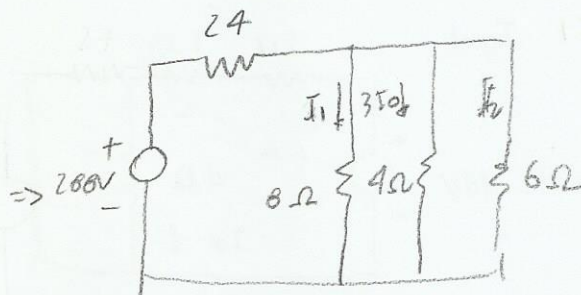
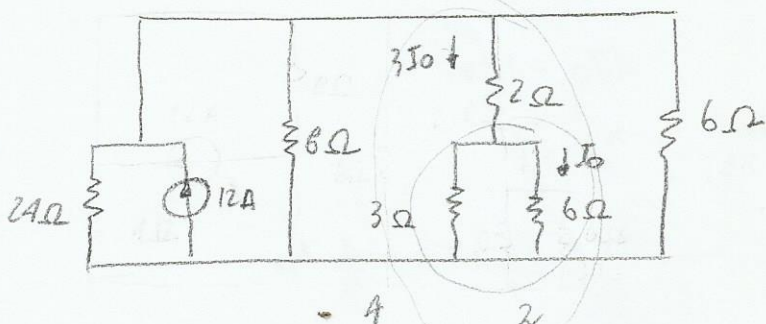
$$x = \frac{I_0}{3} \quad I_T = \frac{4I_0}{3} \quad I_T = \frac{4}{3}$$

$$I_0 = 3 \div \frac{4}{3} = \underline{\underline{\frac{9}{4} \text{ A}}}$$

5.4-1)

$$6I_0 = 3x \quad I = 2I_0 + I_0 = 3I_0$$

$$x = 2I_0$$



$$8I_1 = 12I_0$$

$$6I_2 = 12I_0$$

$$I_1 = \frac{12I_0}{8} = \frac{6I_0}{4} = \frac{3I_0}{2}$$

$$I_2 = 2I_0$$

$$I_T = \frac{3}{2}I_0 + 2I_0 + 3I_0 = \frac{13}{2}I_0$$

$$I_T' = \frac{13}{2}$$

$$R_T = 24 + (8 \parallel 4 \parallel 6) = \frac{336}{13}$$

$$I_T = 200 \div \frac{336}{13} = \frac{70}{7}$$

$$\frac{70}{7} = \frac{13}{2}$$

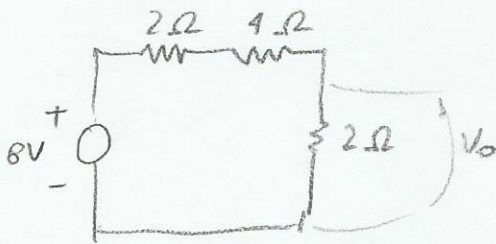
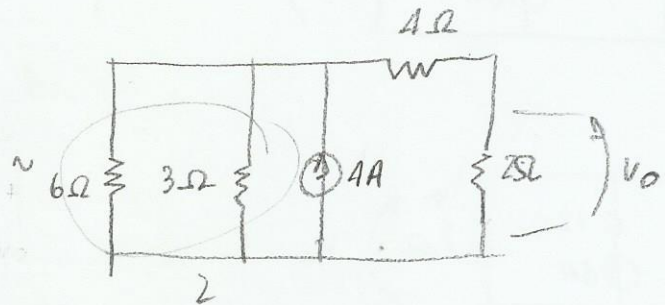
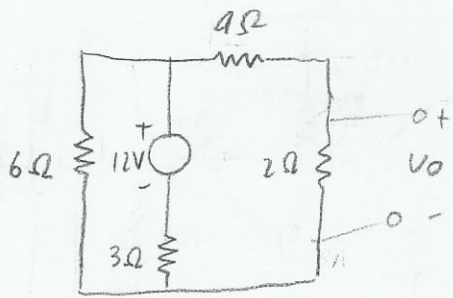
$$\therefore I_0 = \frac{70}{7} \div \frac{13}{2} = \frac{70 \cdot 2}{13 \cdot 7} = \underline{\underline{\frac{12}{7} \text{ A}}}$$

$$I_0 = 1$$

Superposição de efeitos

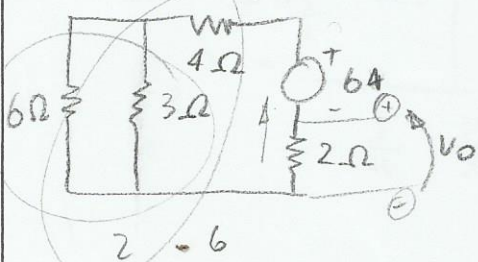
5.14)

Influência de 12V



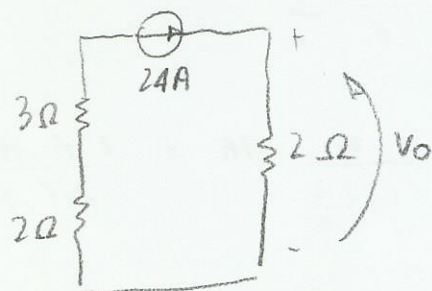
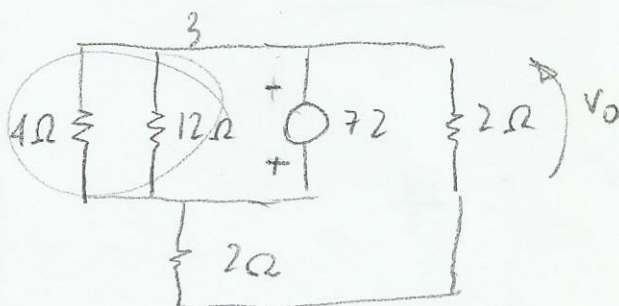
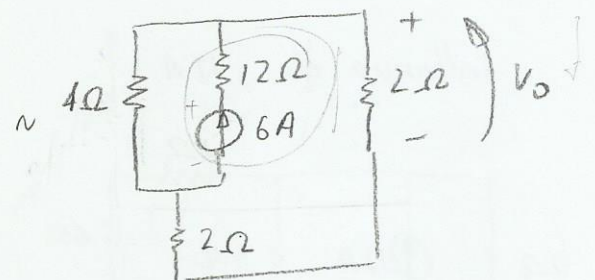
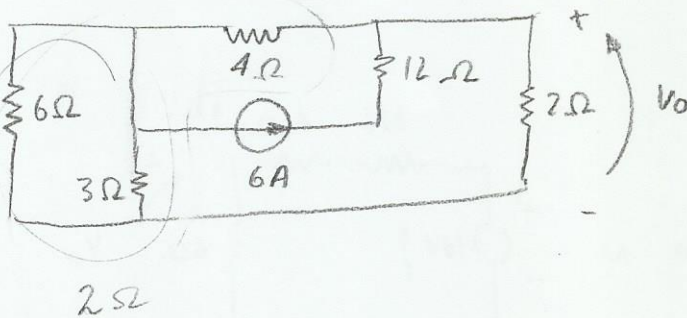
$$V_0' = \frac{2}{8} \cdot 8 = 2V \quad \checkmark$$

Influência de 6A



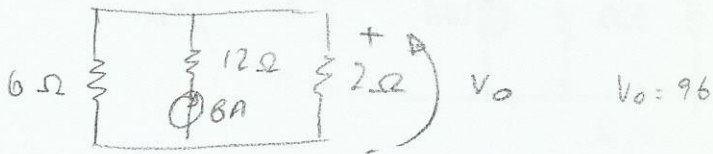
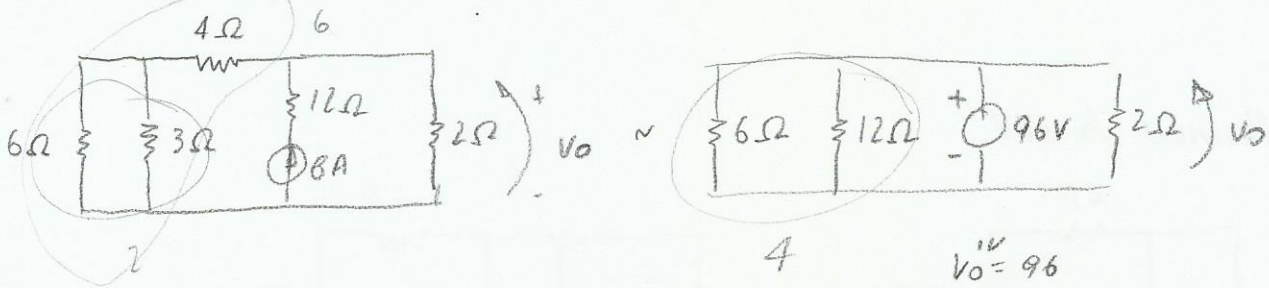
$$V_0'' = \frac{2}{8} \cdot 64 = -16V = -\frac{8}{2}V$$

Influência de 6A



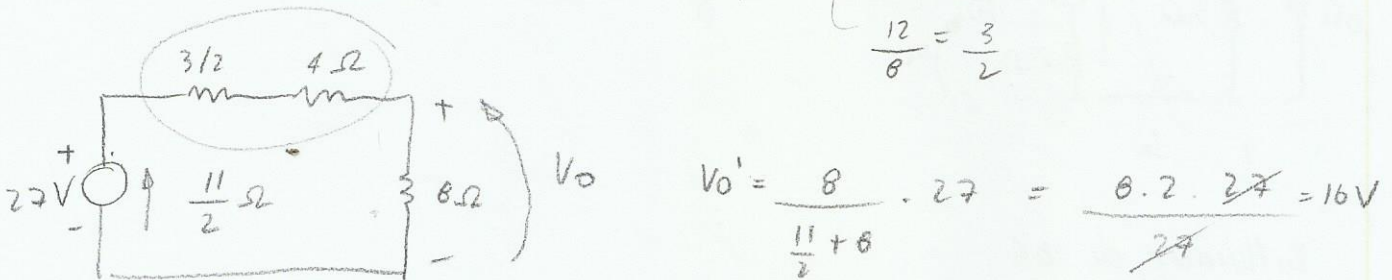
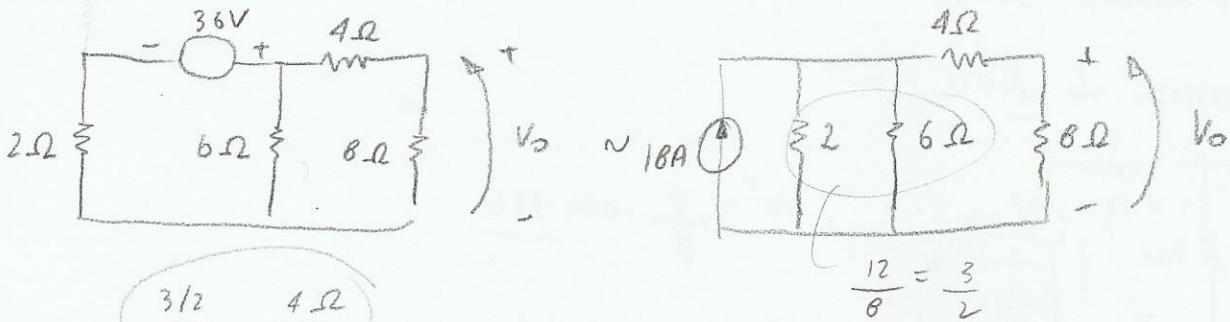
$$: V_0''' = 16V$$

Influenza de 8A

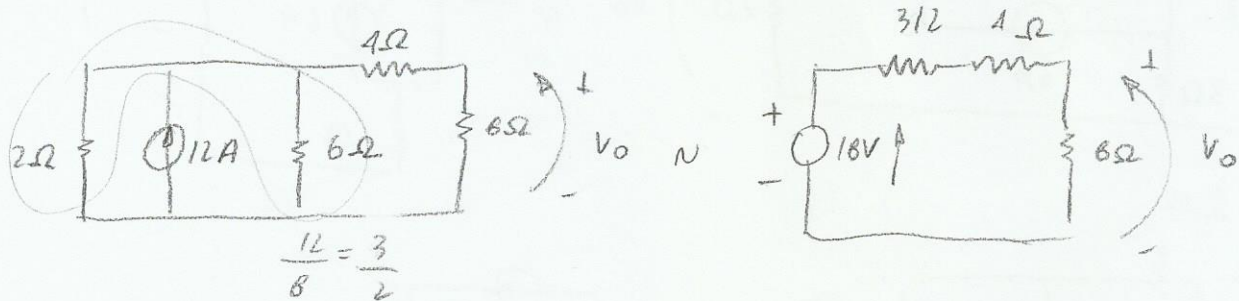


5.5

Influenza de 36V



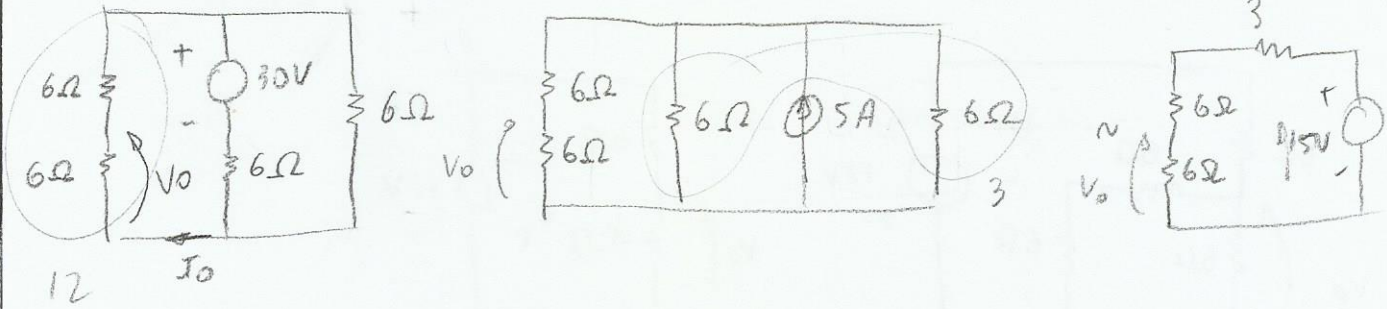
Influenza de 12A



$$V_0'' = \frac{8}{12 + \frac{3}{2}} \cdot 18 = \frac{2 \cdot 8 \cdot 18}{27 \cdot 3} = \frac{32}{3}$$

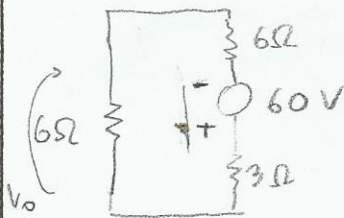
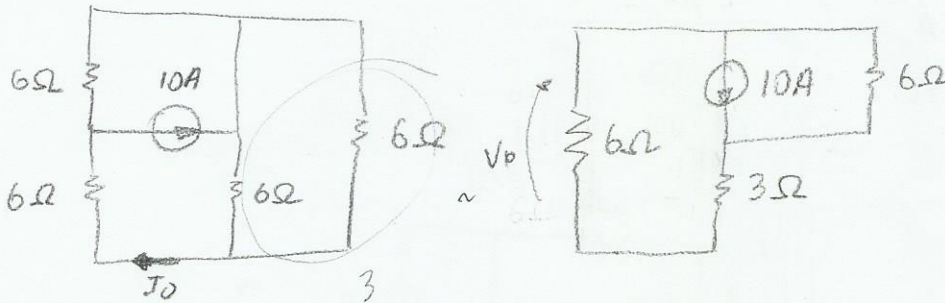
$$V = \frac{32}{3} + 16 = \frac{32 + 48}{3} = \frac{80}{3} \text{ V}$$

Influência de 30V



$$V_0' = \frac{6}{15} \cdot 15 = 6V$$

Influência de 10A



$$V_0'' = \frac{6}{15} \cdot 60 = -24$$

$$V = 6 - 24 = -18 \quad \therefore \underline{I = 3A}$$

$$\begin{cases} 18\alpha - 6\beta = -30 \\ 12\beta - 6\alpha = 30 \end{cases} \quad \sim \quad \begin{cases} 3\alpha - \beta = -10 \\ -3\alpha + 6\beta = 15 \end{cases}$$

$$\alpha = \frac{-10 + \beta}{3} = \frac{-10 + 1}{3} = -3$$

$$5\beta = 5 \quad \therefore \beta = 1$$

$$V_0' = 6V$$

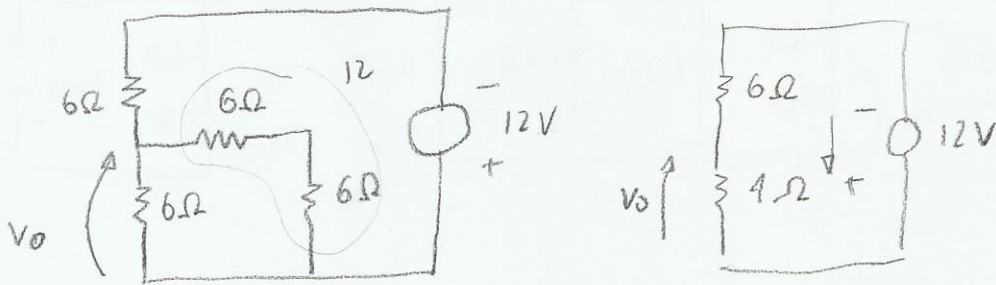
$$V_0'' = -24V$$

$$\therefore I = 3A$$

$$V = -18V$$

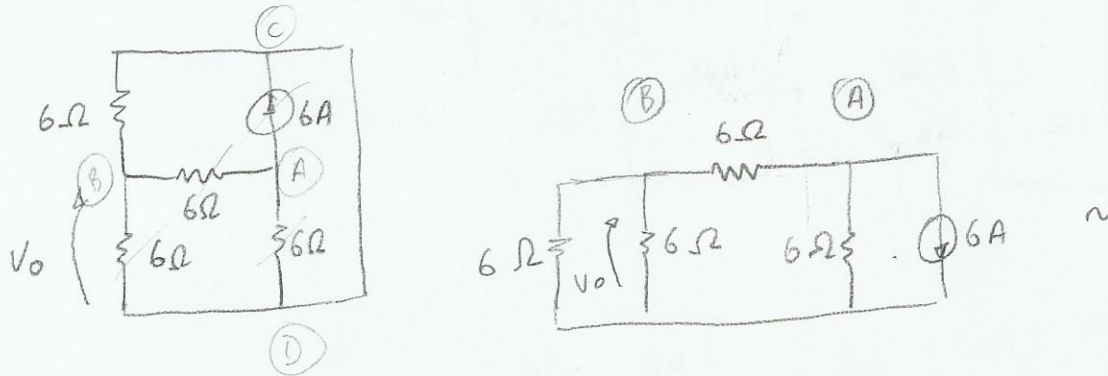
5.7.)

Influenza de 12V

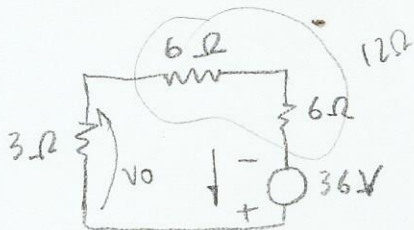


$$V_0' = \frac{-4}{4+6} \cdot 12 = -\frac{24}{5}$$

Influența de 6A



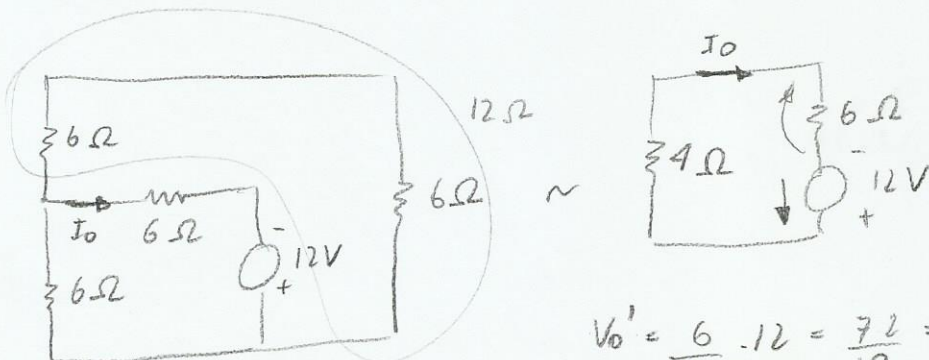
$$V_0'' = \frac{3}{15} \cdot 36 = \frac{-36}{5}$$



$$V = \frac{-36}{5} - \frac{24}{5} = -\frac{60}{5} = -12V$$

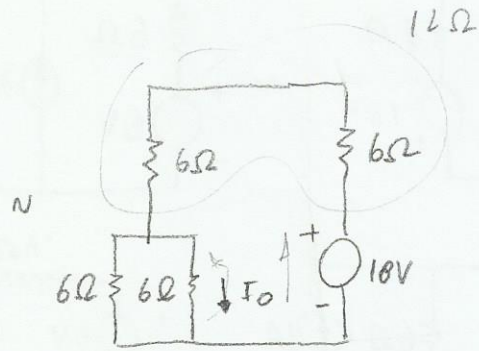
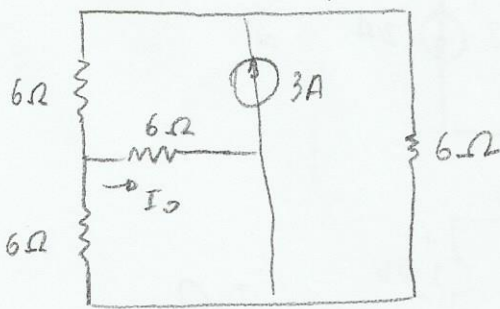
5.8.)

Influența de 12V



$$V_0' = \frac{6}{10} \cdot 12 = \frac{72}{10} = \frac{36}{5}$$

Influenza di 3A



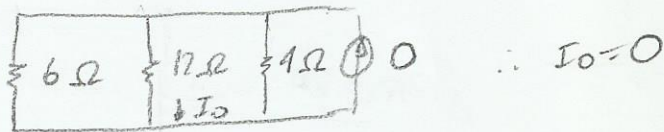
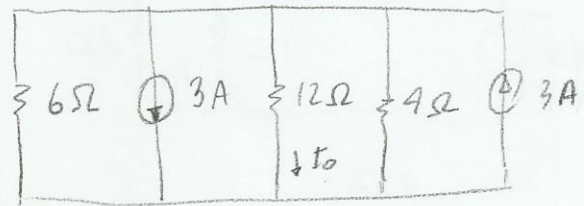
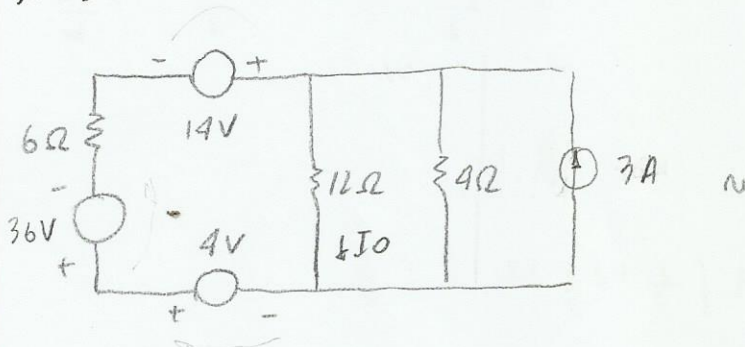
$$I_T = \frac{18}{12+3} = \frac{18}{15} = \frac{6}{5} = 2I_0 \quad \therefore I_0 = \frac{3}{5}$$

$$V_0'' = \frac{3}{5} \cdot 6 = \frac{18}{5}$$

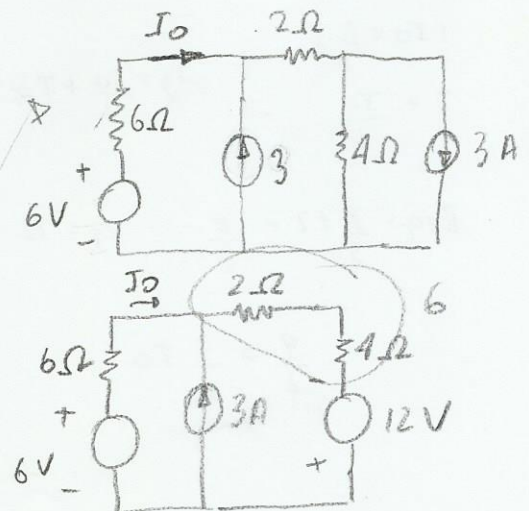
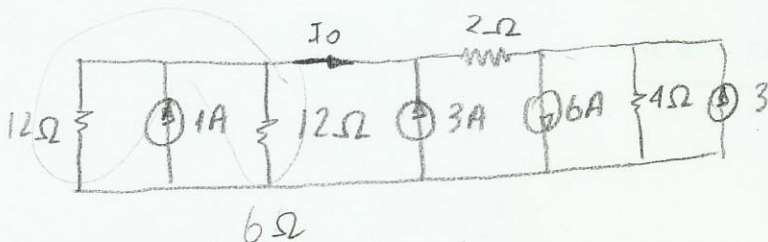
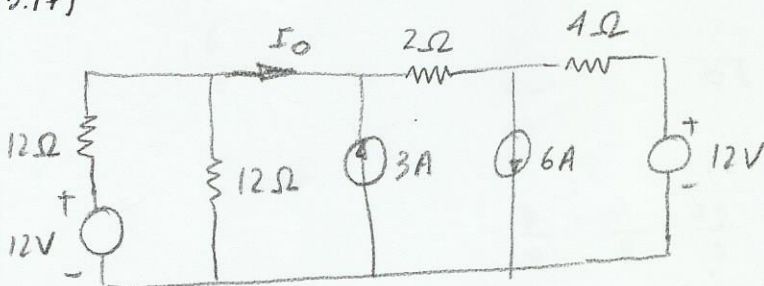
$$V = \frac{18}{5} + \frac{36}{5} = \frac{54}{5}$$

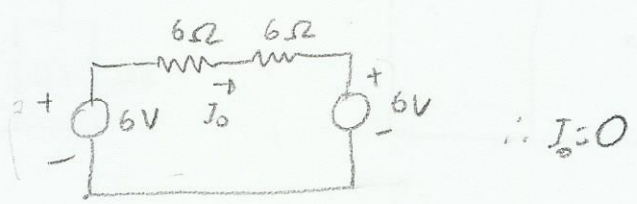
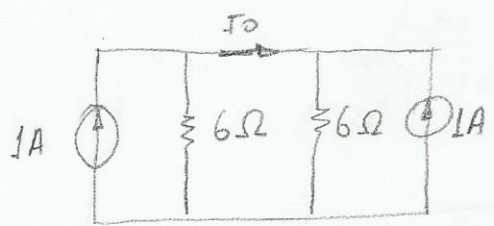
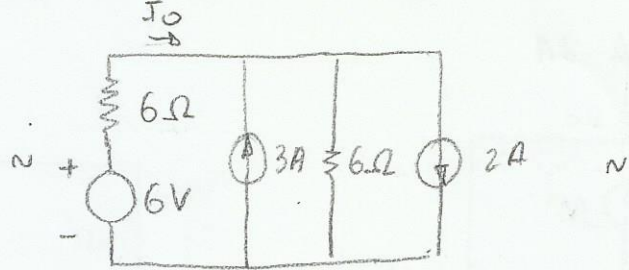
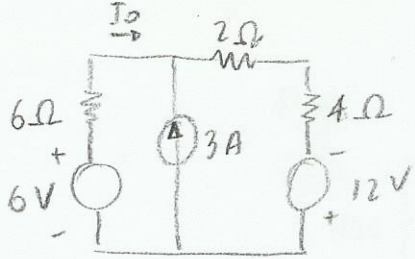
$$I_0 = \frac{54}{5} \div 6 = \frac{54}{30} = \frac{27}{15} = \frac{9}{5} \text{ A}$$

5.16.)

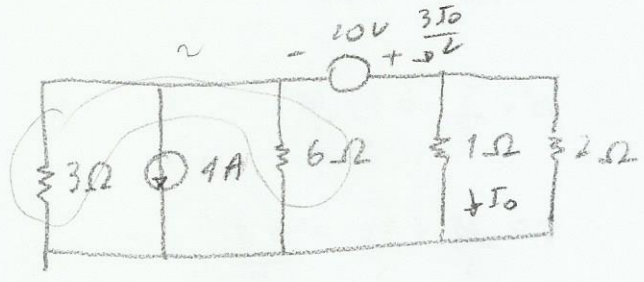
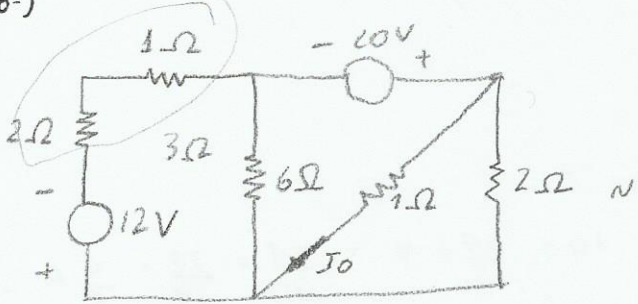


5.17)



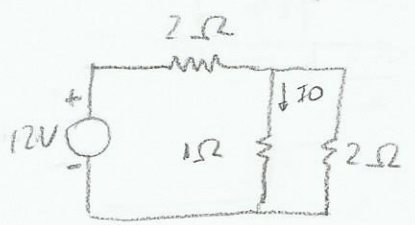
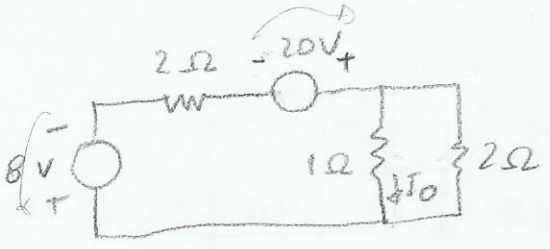


5.18.)



$I_0 = 2I$

$I = \frac{I_0}{2} \therefore I_0 + \frac{I_0}{2} = \frac{3I_0}{2}$



$V_0 = \frac{2}{3} \div \left(\frac{2}{3} + 2 \right) \cdot 12$

$= \frac{2}{3} \div \frac{8}{3} \cdot 12$

$= \frac{1}{4} \cdot 12 = 3$

$I_0 = 3A$

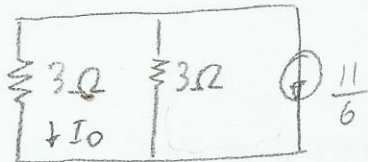
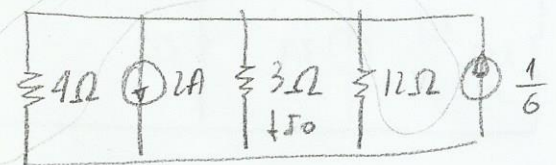
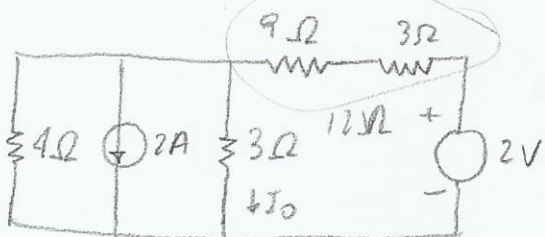
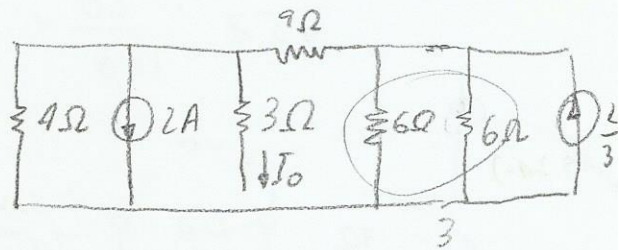
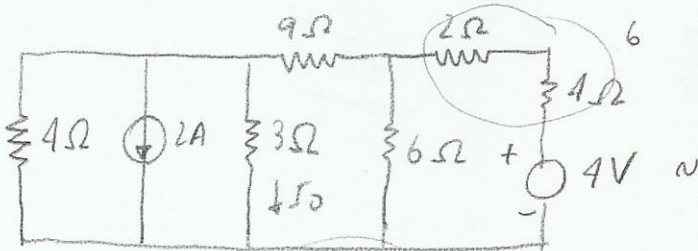
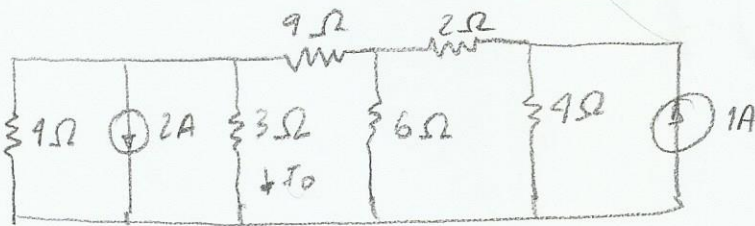
$1I_0 = 2I$

$I = \frac{I_0}{2} \therefore I_0 = \frac{I_0}{2} + I_0 = \frac{3}{2} I_0$

$R_{eq} = \frac{2}{3} + 2 = \frac{8}{3} \quad I_T = 12 \div \frac{8}{3} = \frac{36}{8} = \frac{18}{4} = \frac{9}{2}$

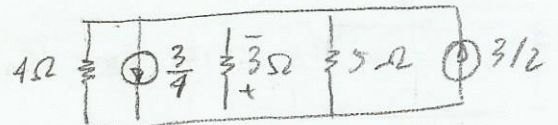
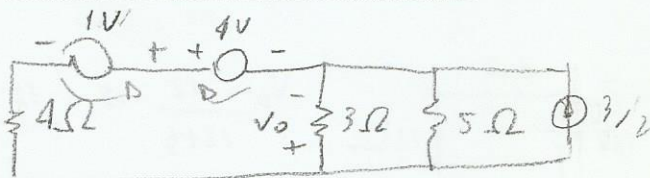
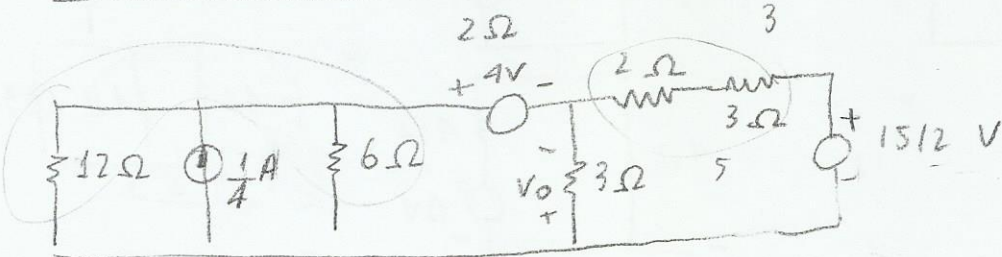
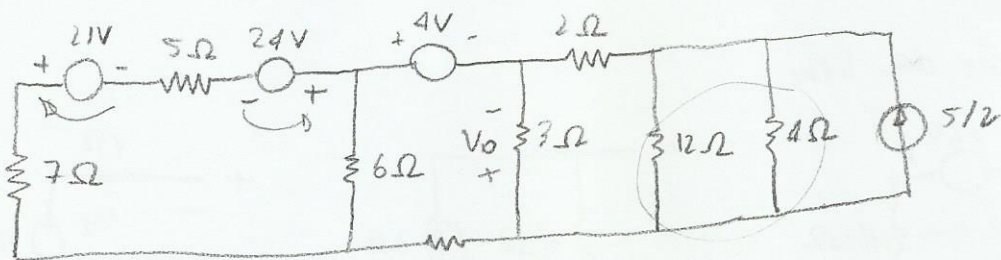
$\frac{9}{2} = \frac{3}{2} I_0 \therefore I_0 = 3A$

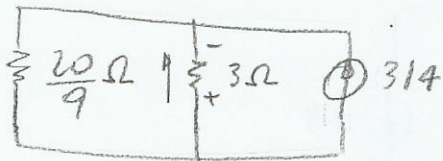
5.19.)



$$\therefore I_0 = \frac{11}{6} \div 2 = -\frac{11}{12} \text{ A}$$

5.20.)





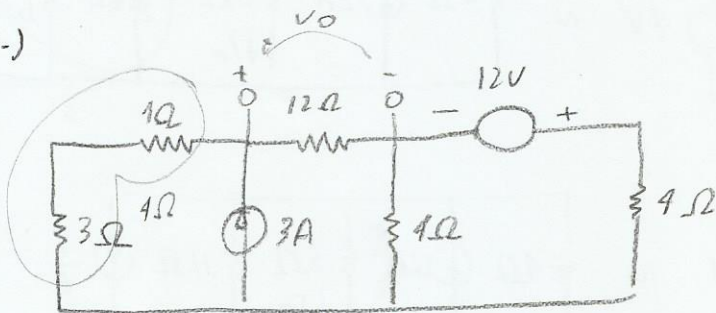
$$I_0 = \frac{20}{9} \div \left(\frac{20}{9} + 3 \right) \cdot \frac{3}{4}$$

$$= \frac{20}{9} \div \frac{47}{9} \cdot \frac{3}{4}$$

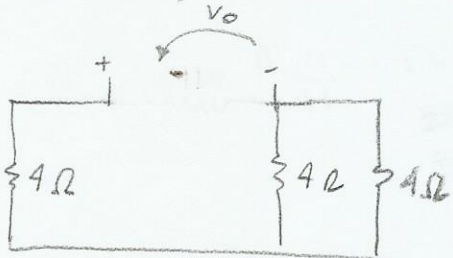
$$= \frac{20 \cdot 3}{47 \cdot 4} = \frac{60}{188} = \frac{15}{47}$$

$$\therefore V_0 = \frac{45}{47} \text{ V}$$

5.24-)

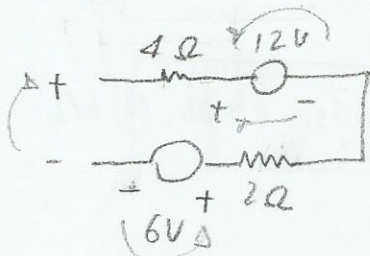
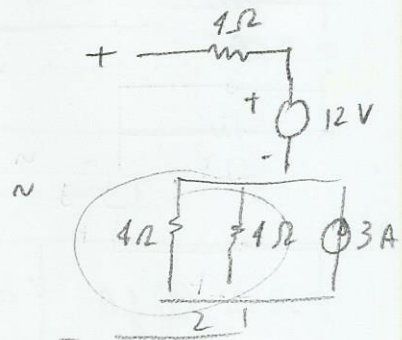
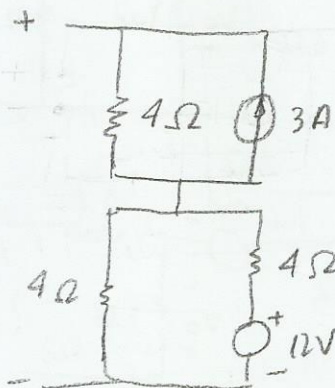
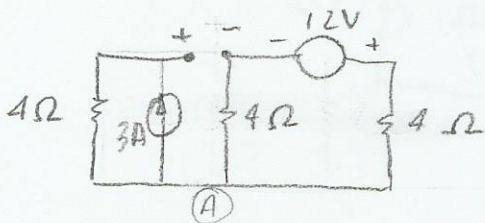


Determinação do R_{th}

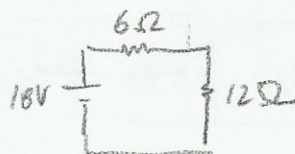


$$R_{eq} = 4 + (4 \parallel 4) = 6 \Omega$$

Determinação do E_{th}



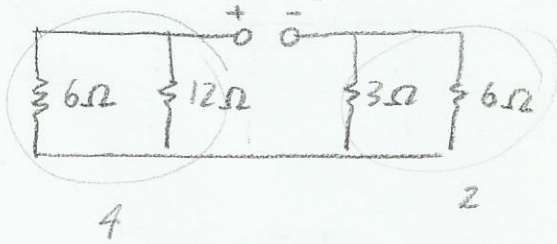
$$E_{th} = 18$$



$$V_0 = \frac{12}{12+6} \cdot 18 = 12 \text{ V}$$

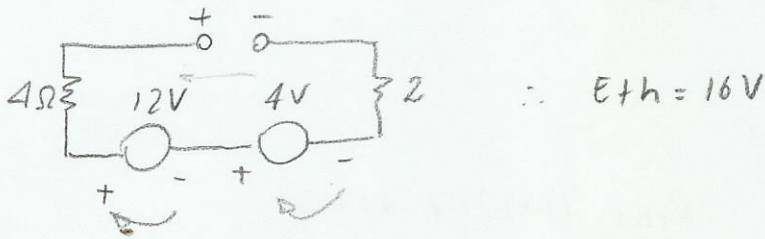
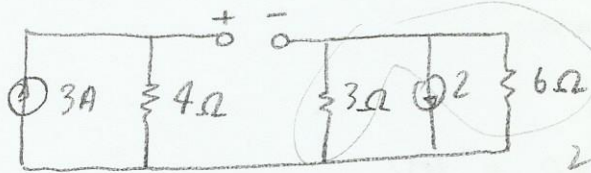
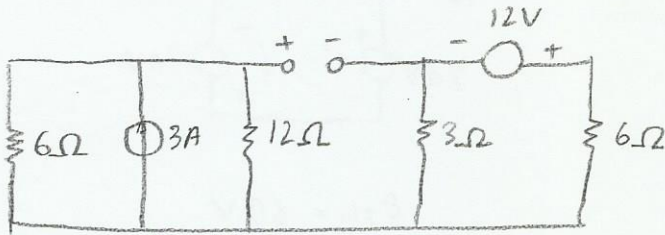
5.25

Para determinar R_{th}



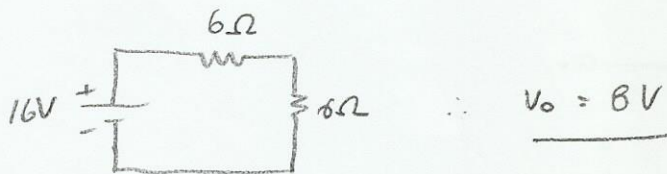
$\therefore R_{th} = 6 \Omega$

Para determinar E_{th}



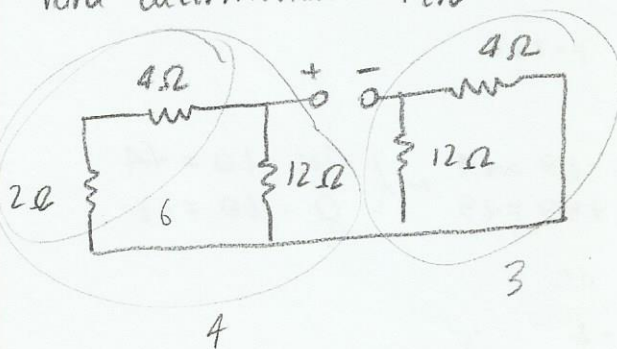
$\therefore E_{th} = 16V$

Gerador equivalente de thvenin



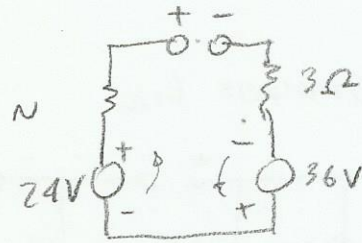
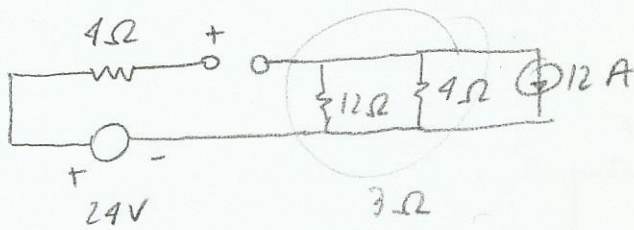
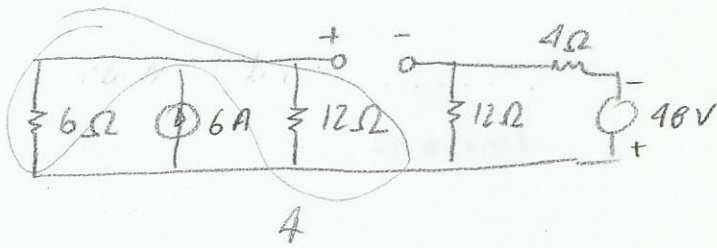
5.26

Para determinar R_{th}



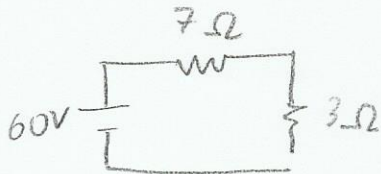
$\therefore R_{th} = 7 \Omega$

Para determinar E_{th}



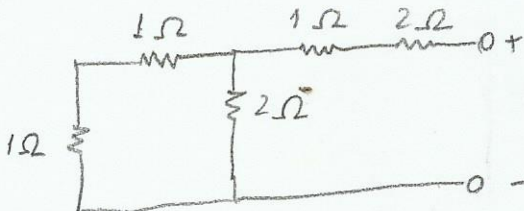
$\therefore E_{th} = 60V$

Gerador equivalente de Thevenin



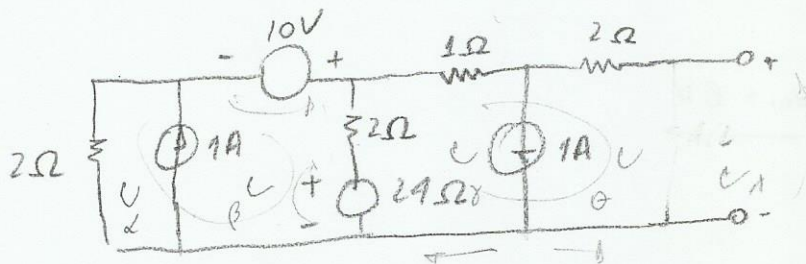
$V_0 = \frac{3}{3+7} 60 = 18V$

536



$R_{th} = (1+1) \parallel 2 + 1 + 2$

$\therefore R_{th} = 4\Omega$

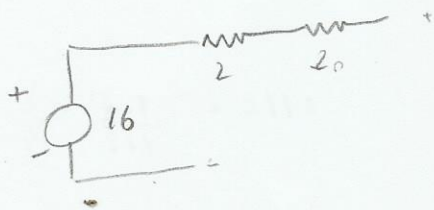
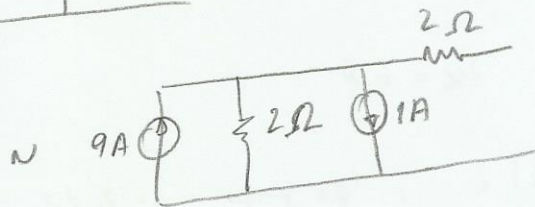
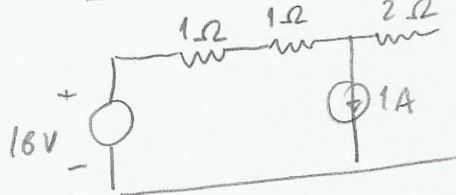
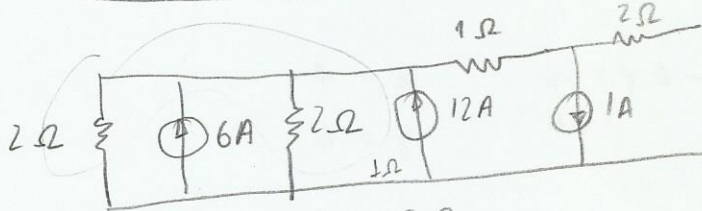
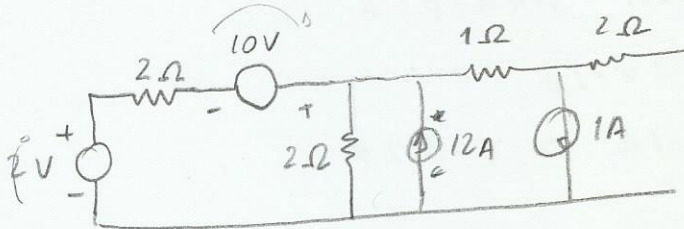
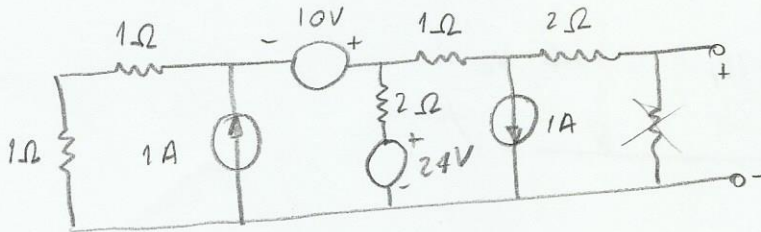


$$\begin{cases} 2\alpha + 2\beta - 2\gamma = -14 \\ 3\gamma + 6\theta - 2\beta = 24 \end{cases} \quad ; \quad \begin{cases} \beta - \alpha = 1 & \beta = 1 + \alpha \\ \gamma - \theta = 1 & \gamma = 1 + \theta \end{cases}$$

$$\begin{cases} 2\alpha + 2 + 2\alpha - 2 - 2\theta = -14 \\ 3 + 3\theta + 6\theta - 2 - 2\alpha = 24 \end{cases} \quad \sim \quad \begin{cases} 4\alpha - 2\theta = -14 \\ -2\alpha + 9\theta = 23 \end{cases} \quad \sim \quad \begin{cases} 4\alpha - 2\theta = -14 \\ 0 + 16\theta = 32 \end{cases}$$

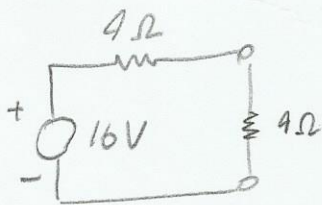
$\alpha = 2 \quad \gamma = 1 + 2 = 3 \quad \therefore I_{th} = 1 - 3 = -2$

Outra forma



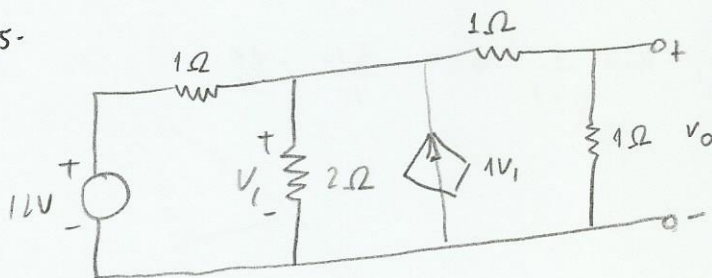
$\therefore V_{th} = 16V$

Gerador equivalente de thivnan

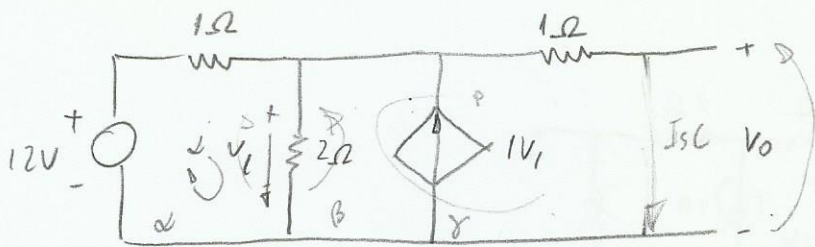


$\therefore V_0 = 8V$

5.45-



Utilizar método indutivo



$$\begin{cases} 3\alpha - 2\beta = 12 \\ 2\beta + \gamma - 2\alpha = 0 \end{cases}$$

$$\gamma - \beta = 1V_1 \quad V_1 = (\alpha - \beta) \cdot 2$$

$$\gamma - \beta = 2\alpha - 2\beta$$

$$\beta = \gamma - 2\alpha \rightarrow \gamma = \beta + 2\alpha$$

$$\begin{cases} 3\alpha - 2\gamma + 4\alpha = 12 \\ 2\gamma - 4\alpha + \gamma - 2\alpha = 0 \end{cases}$$

$$7\alpha - 2\gamma = 12$$

$$\begin{cases} 7\alpha - 2\gamma = 12 \\ -6\alpha + 3\gamma = 0 \end{cases}$$

$$21\alpha - 6\gamma = 36$$

$$9\alpha = 36$$

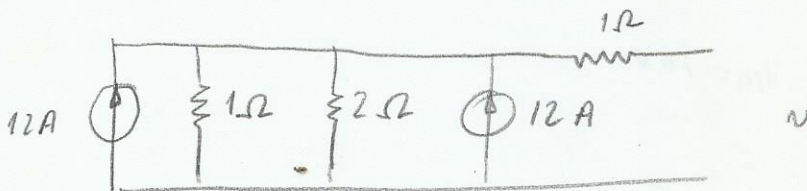
$$\therefore \alpha = 4$$

$$\gamma = 6$$

$$I_{sc} = 6 \text{ A}$$

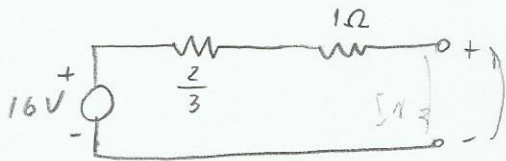
$$V_1 = (\alpha - \beta) \cdot 2 \quad ; \quad \beta = \gamma - 2\alpha = 6 - 2 \cdot 4 = -2$$

$$= (4 - (-2)) \cdot 2 = 12$$

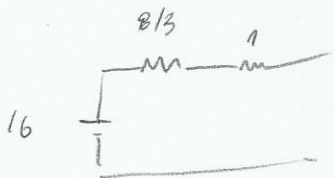


$$11/2 = \frac{1 \cdot 2}{1+2} = \frac{2}{3}$$

$$29 \cdot \frac{2}{3} = \frac{46}{3} = 16$$



$$\therefore V_{oc} = 16$$

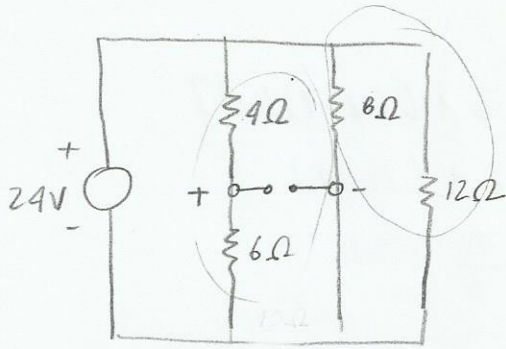


$$R_{th} = \frac{16}{6} = \frac{8}{3}$$

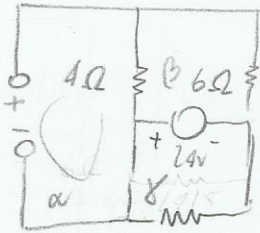
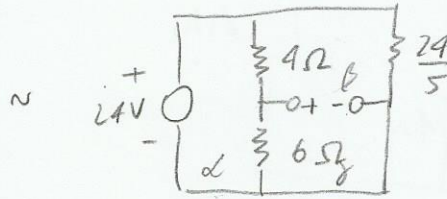
$$V_o = \frac{1}{\frac{8}{3} + 1} \cdot 16 = \frac{3 \cdot 16}{11} = \frac{48}{11}$$



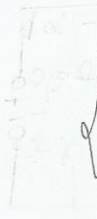
5.53



$$8 \parallel 12 = \frac{8 \cdot 12}{8+12} = \frac{96}{20} = \frac{48}{10} = \frac{24}{5}$$



24/5



$$10x - 4\beta - 6\gamma = 24$$

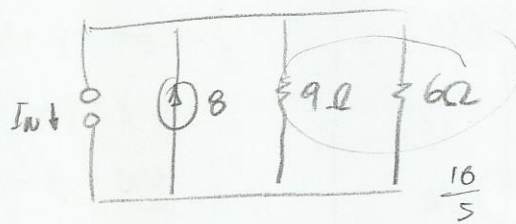
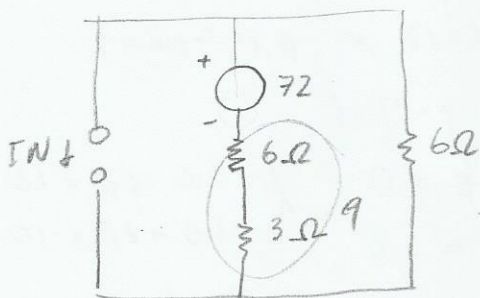
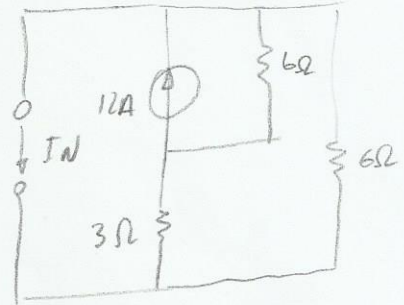
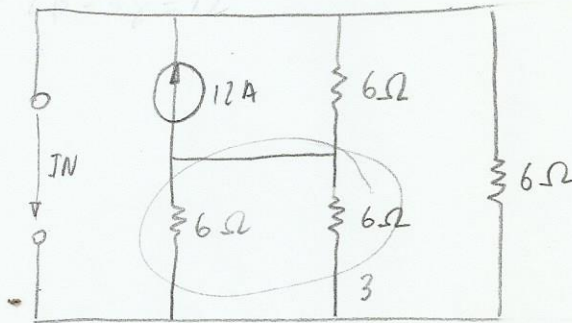
$$\frac{44}{5}\beta - 4\alpha = V_{OC}$$

$$6\gamma - 6\alpha = -V_{OC}$$

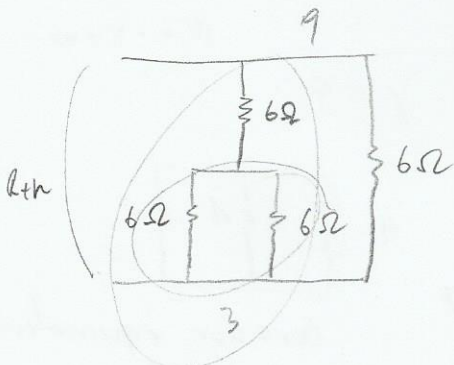
5.52

$$10x - 4\beta - 6\gamma = 24$$

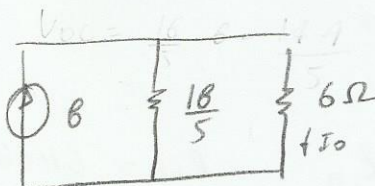
$$5x - 2\beta - 3\gamma = 12$$



$$I_N = 8$$



$$R_{th} = [(6 \parallel 6) + 6] \parallel 6 = \frac{18}{5}$$

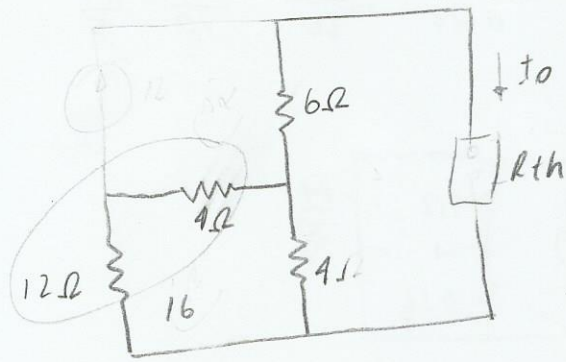


$$I_0 = \frac{18}{5} \div \left(\frac{18}{5} + 6 \right) \cdot 6$$

$$= \frac{18}{5} \cdot \frac{5}{48} \cdot 6 = \frac{18}{6} = 3$$

$$\therefore I_0 = 3A$$

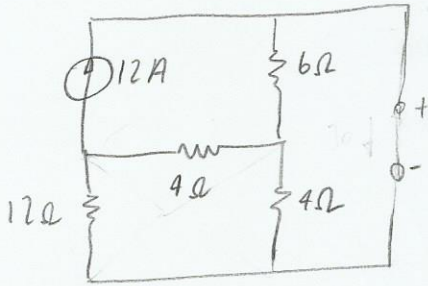
5.18



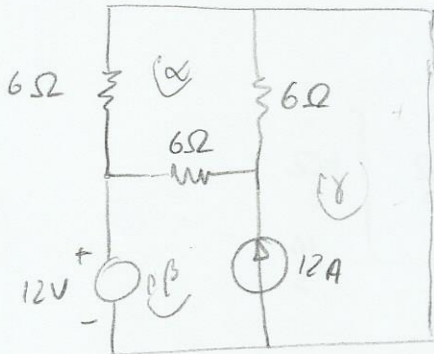
$$R_{th} = 6 + [(12+4) \parallel 4]$$

$$= 6 + (16 \parallel 4)$$

$$= \frac{46}{5} = 9,2$$



5.29



$$\begin{cases} 16\alpha - 6\beta - 6\gamma = 0 \sim 3\alpha - \beta - \gamma \\ 6\beta + 6\gamma - 12\alpha = 12 \sim \beta + \gamma - 2\alpha = 2 \\ \gamma - \beta = 12 \quad \gamma = 12 + \beta \end{cases}$$

$$\begin{cases} 3\alpha - \beta - 12 - \beta = 0 \\ \beta + 12 + \beta - 2\alpha = 2 \end{cases} \sim \begin{cases} 3\alpha - 2\beta = 12 \\ -2\alpha + 2\beta = -10 \\ \alpha - \beta = -5 \end{cases}$$

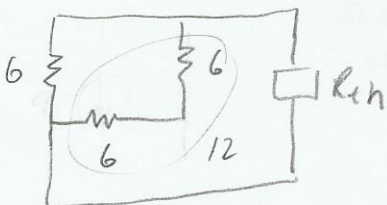
$$\begin{cases} 3\alpha - 2\beta = 12 \\ \alpha = 2 \end{cases}$$

$$\gamma = 12 + \beta$$

$$\gamma = 12 - 5 + \alpha = 12 - 5 + 2 \quad \therefore \gamma = 9$$

$$\beta = -5 + \alpha$$

$$I_N = 9$$

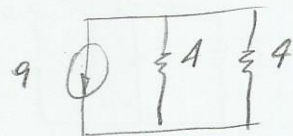


$$\therefore R_{th} = 6 \parallel (6+6) = 4$$

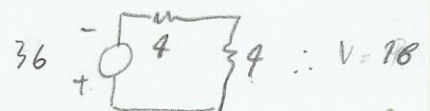
$$I_0 = \frac{18}{4} = \frac{9}{2}$$

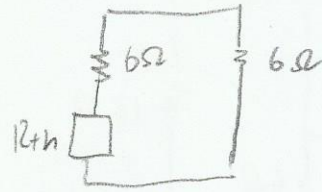
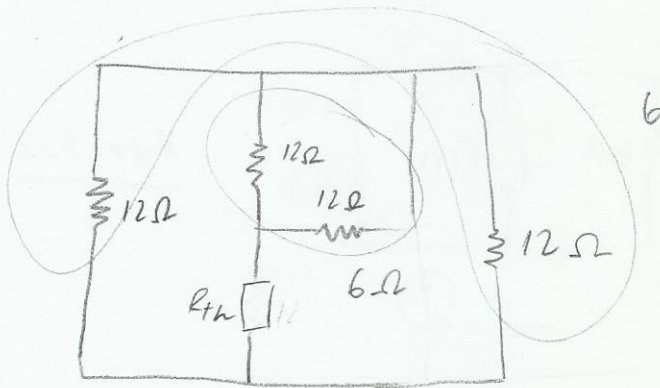
$$I_0 + 12 = \frac{9}{2}$$

$$\therefore I_0 = -7,5 \text{ A}$$

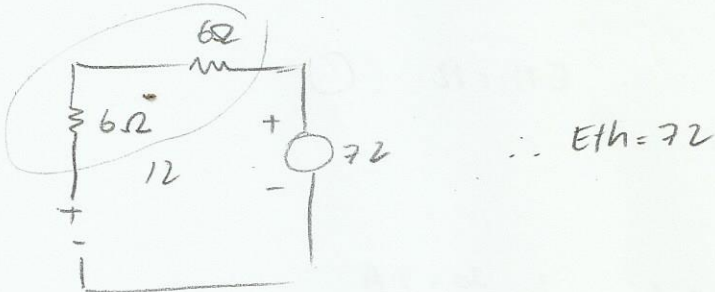
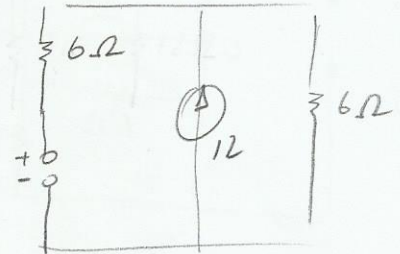
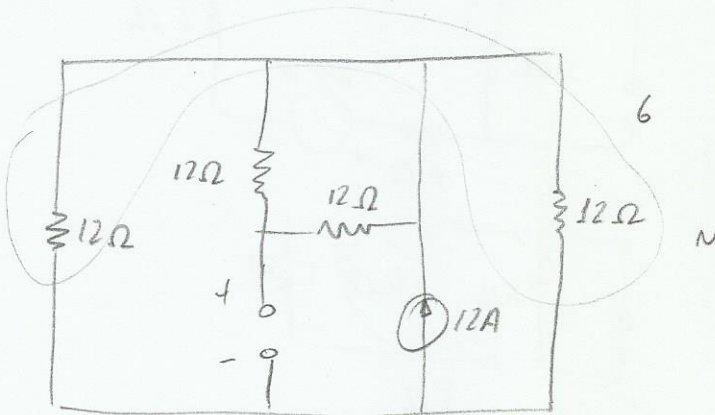


Gerador equivalente de thvenon



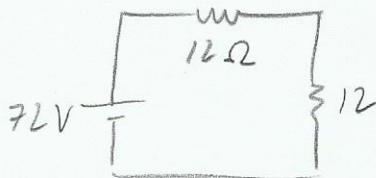
Determinação do R_{th} 

$$\therefore R_{th} = 12 \Omega$$

Para determinar E_{th} 

$$\therefore E_{th} = 72$$

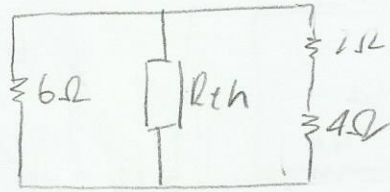
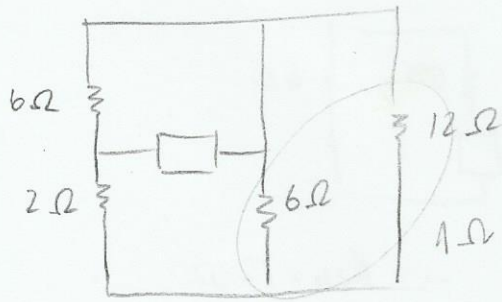
Circuito equivalente de Thevenin



$$\therefore V_0 = 36$$

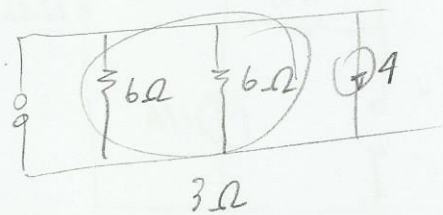
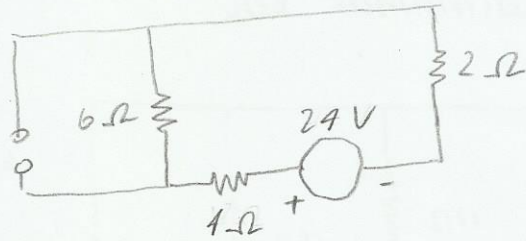
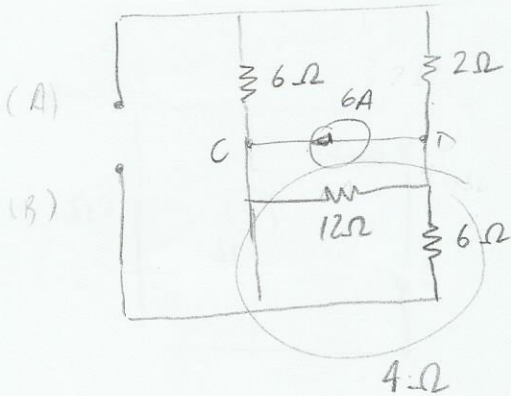
$$\therefore I_0 = \frac{36}{12} = \underline{\underline{3A}}$$

Determinação R_{th}



$\therefore R_{th} = 3\Omega$

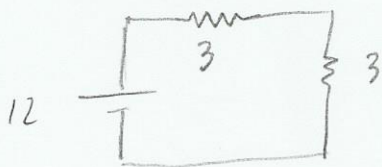
Determinação do E_{th}



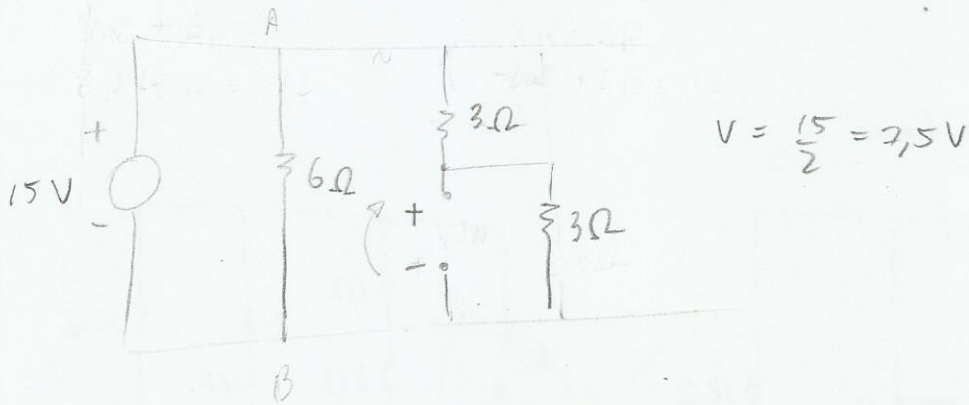
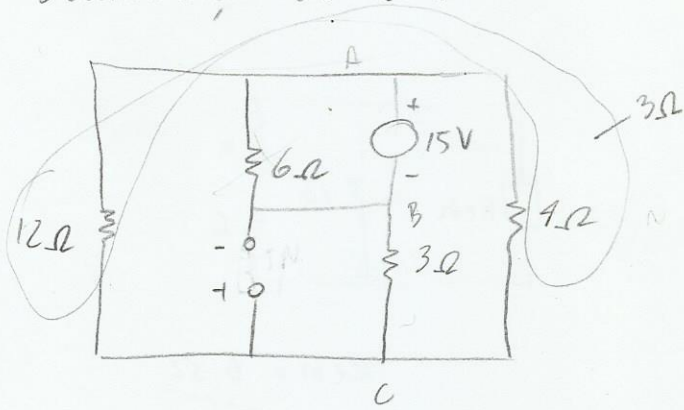
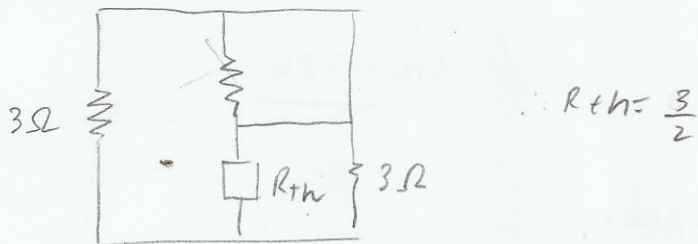
Gerador equivalente de

$\therefore E_{th} = 12$

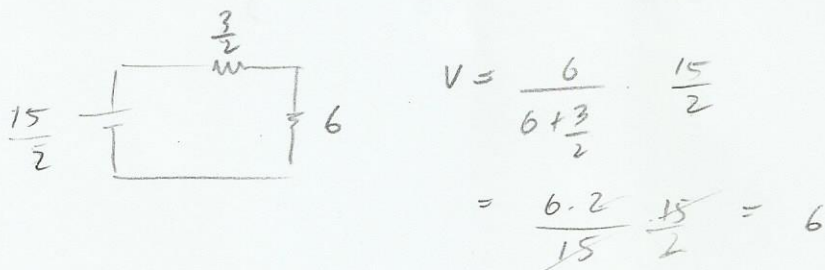
Thvenon



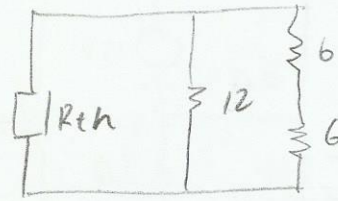
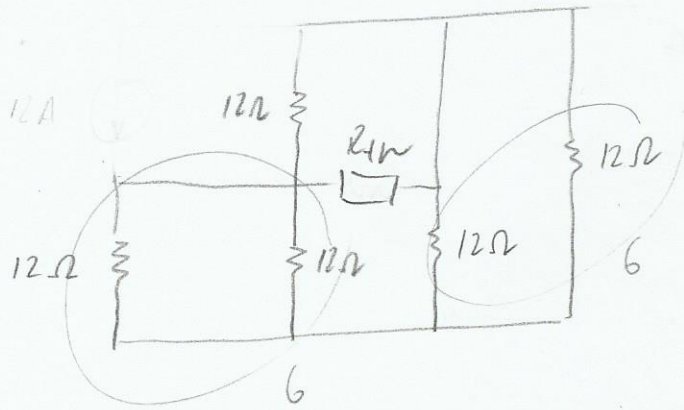
$\therefore V_0 = 6$ e $I_0 = 2A$

Determinação do E_{th} Determinação do R_{th} 

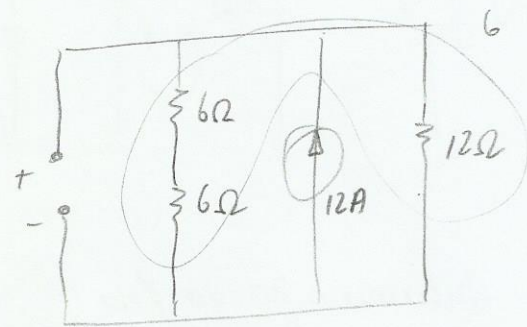
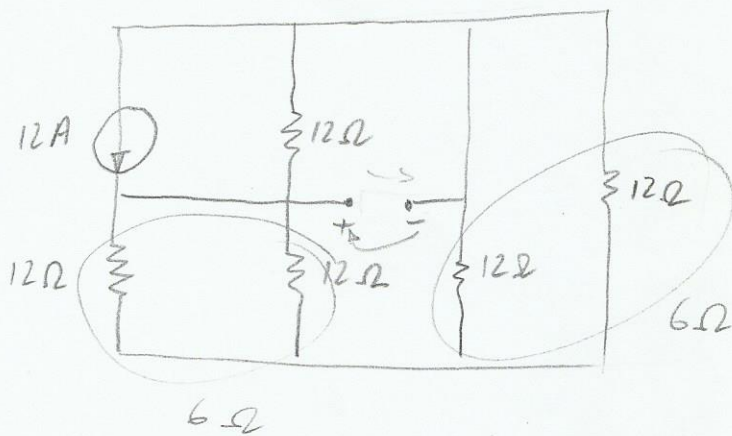
Gerador equivalente de Thevenin



$$I = \frac{6}{6} = 1A$$

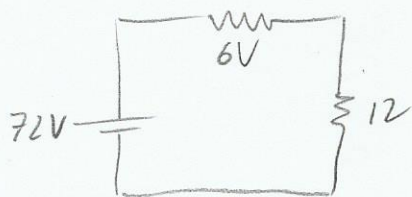
Determinação do R_{th} 

$$\therefore R_{th} = \underline{6 \Omega}$$

Determinação do E_{th} 

$$\therefore E_{th} = \underline{72V}$$

Gerador equivalente de Thevenin

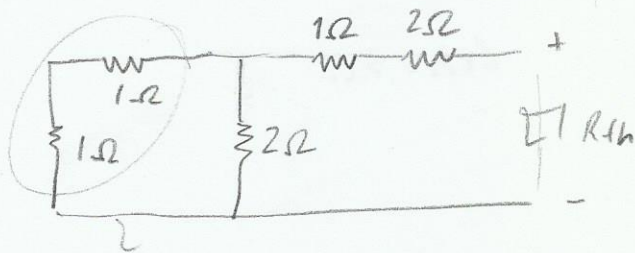


$$V = \frac{12}{12+6} \cdot 72 = \frac{12 \cdot 72}{18} = \frac{2 \cdot 72}{3} = 48$$

$$I_0 = \frac{48}{12} = \underline{4A}$$

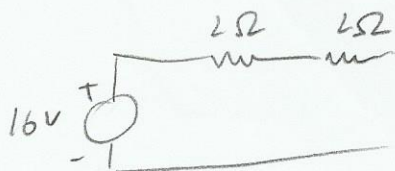
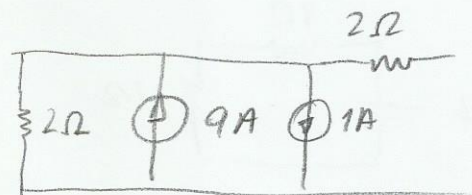
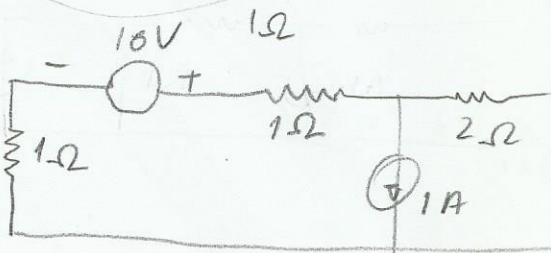
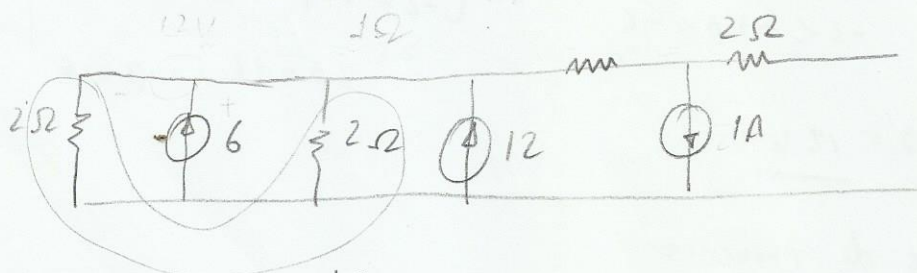
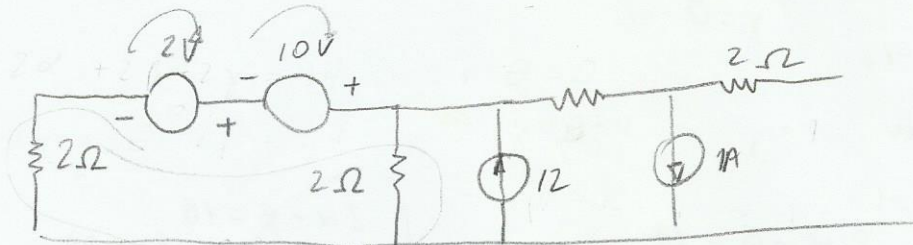
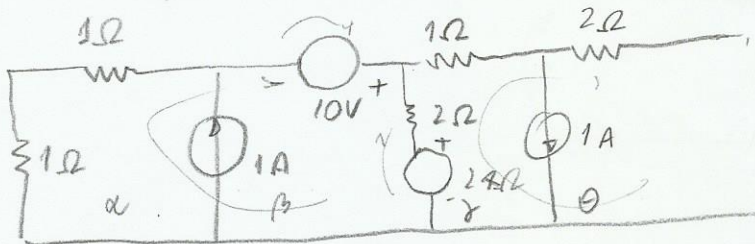
5.36)

Determinação do R_{th}



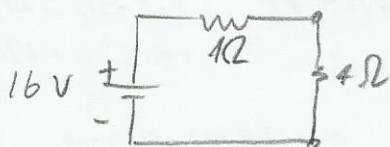
$\therefore R_{th} = 4\Omega$

Determinação do E_{th}



$\therefore E_{th} = 16V$

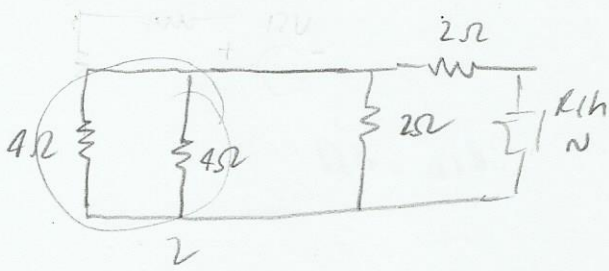
Gerador equivalente de Thevenin



$\therefore V_0 = 8V$

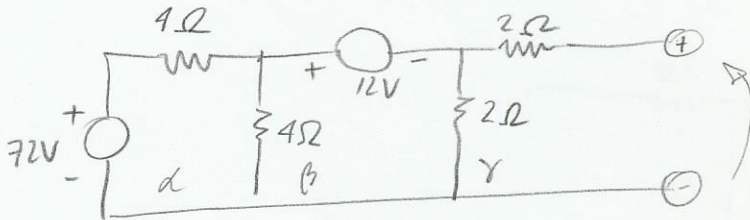
5.37

Determinação do R_{th}



$R_{th} = 3\Omega$

Determinação do E_{th}



$$\begin{cases} 8\alpha - 4\beta = 72 \\ 6\beta - 4\alpha - 2\gamma = -12 \\ 4\gamma - 2\beta = -E_{th} \end{cases} \quad \gamma = 0$$

$$\begin{aligned} 8\alpha - 4\beta = 72 & \sim 2\alpha - \beta = 18 \\ 6\beta - 4\alpha = -12 & \sim -2\alpha + 3\beta = -6 \end{aligned}$$

$$\sim \begin{cases} 2\alpha - \beta = 18 \\ -2\alpha + 3\beta = -6 \end{cases}$$

$2\beta = 12 \therefore \beta = 6$

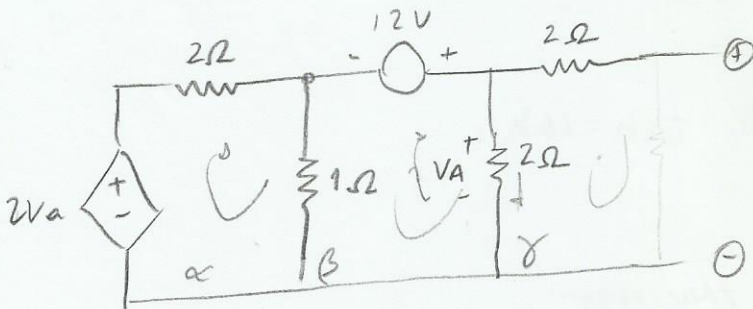
$E_{th} = -2 \cdot \beta = -2 \cdot 6 = -12V$

Gerador equivalente de Thévenin



$V_0 = \frac{1}{3+1} \cdot 12 = 3V$

5.38-



$$\begin{cases} 3\alpha - \beta = 2V_a \\ 3\beta - \alpha - 2\gamma = 12 \\ 4\gamma - 2\beta = -V_0 \end{cases}$$

$V_a = 2(\beta - \gamma)$

$$\begin{cases} 3\alpha - \beta = 4\beta - 4\gamma \\ 3\beta - \alpha = 12 \end{cases} \sim \begin{cases} 3\alpha - 5\beta = 0 \\ -\alpha + 3\beta = 12 \end{cases}$$

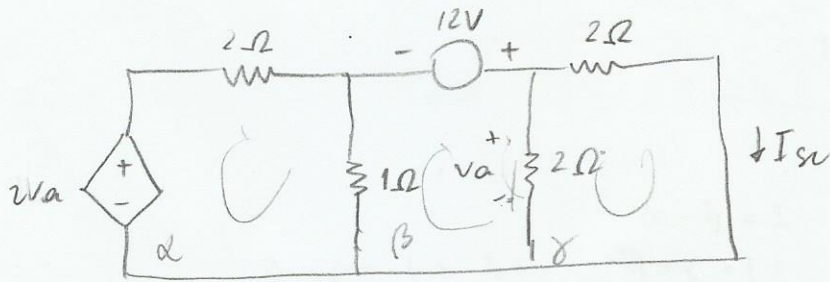
$$\begin{cases} 3\alpha - 5\beta = 0 \\ 4\beta = 36 \end{cases}$$

$\beta = 9 \quad \alpha = 3\beta - 12 = 3 \cdot 9 - 12$

$\therefore \alpha = 15$

$$V_0 = 29$$

$$= 1.611 \approx 1.6V$$

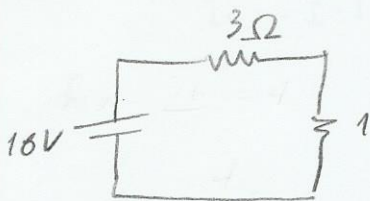


$$\begin{cases} 3\alpha - \beta = 2v_a & ; v_a = 2(\beta - \gamma) \\ 3\beta - \alpha - 2\gamma = 12 \\ 4\gamma - 2\beta = 0 \end{cases}$$

$$\begin{cases} 3\alpha - \beta = 4\beta - 4\gamma \\ -\alpha + 3\beta - 2\gamma = 12 \\ -2\beta + 4\gamma = 0 \end{cases} \sim \begin{cases} 3\alpha - 5\beta + 4\gamma = 0 \\ 4\beta - 2\gamma = 36 \\ 6\gamma = 36 \end{cases} \therefore \gamma = 6$$

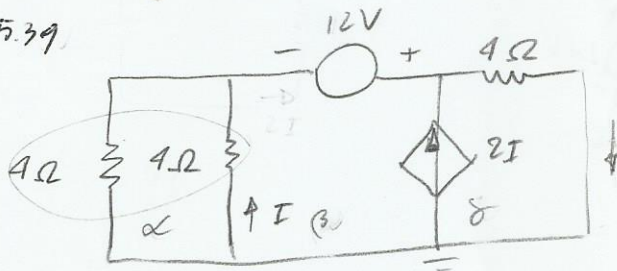
$$I_{sc} = 6 \text{ A}$$

$$R_{th} = \frac{18}{6} = 3$$



$$V_0 = \frac{1}{3+1} \cdot 16 = \frac{16}{4} = \frac{4}{1} = 4 \text{ V}$$

5.39



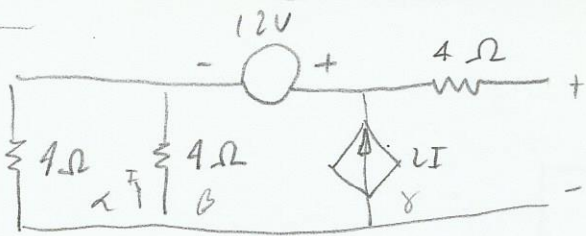
$$\begin{cases} 8\alpha - 4\beta = 0 \\ 4\beta + 4\gamma - 4\alpha = 12 \end{cases} \quad \gamma - \beta = 2I ; I = \beta - \alpha$$

$$\begin{cases} 8\alpha - 4\beta = 0 \\ 4\beta + 12\beta - 8\alpha - 4\alpha = 12 \end{cases} \quad \begin{aligned} \gamma - \beta &= 2\beta - 2\alpha \\ \gamma &= 3\beta - 2\alpha \end{aligned}$$

$$\begin{cases} 8\alpha - 4\beta = 0 \\ -12\alpha + 16\beta = 12 \end{cases} \sim \begin{cases} 8\alpha - 4\beta = 0 \\ 20\alpha = 12 \end{cases} \therefore \alpha = \frac{12}{20} = \frac{6}{10} = \frac{3}{5}$$

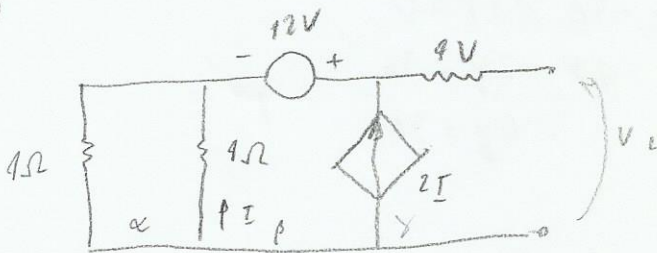
$$8\alpha - 4\beta = 0 \quad 2\alpha - \beta = 0 \quad \beta = 2\alpha = \frac{6}{5}$$

$$\gamma = 3 \cdot \frac{6}{5} - 2 \cdot \frac{3}{5} = \frac{18}{5} - \frac{6}{5} = \frac{12}{5}$$



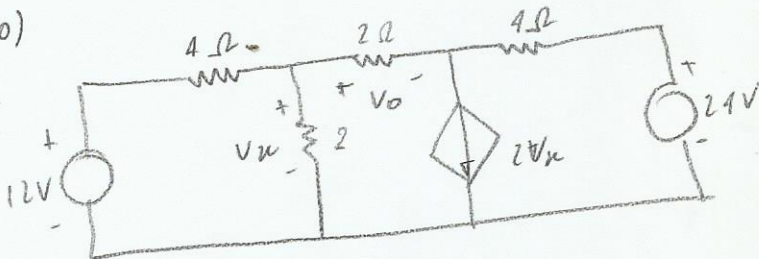
$$\begin{cases} 8\alpha - 4\beta = 0 & I = \beta - \alpha \\ 4\beta + 4\gamma - 4\alpha = 12 - E & 2I = \gamma - \beta \\ 4\beta + 12\beta - 8\alpha - 4\alpha = 12 - E & 2(\beta - \alpha) = \gamma - \beta \\ & 2\beta - 2\alpha = \gamma - \beta \\ & \gamma = 3\beta - 2\alpha \end{cases}$$

5.39)

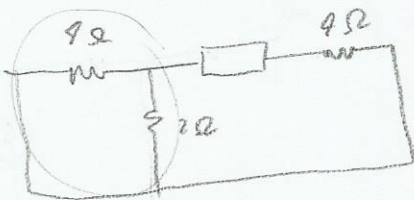


$$\begin{cases} 8\alpha - 4\beta = 0 & \beta - \alpha = I & \alpha = \beta - I = -2I - I = -3I \\ 4\beta + 4\gamma - 4\alpha = 12 - V_L & \gamma - \beta = 2I & \beta = -2I \end{cases}$$

5.40)

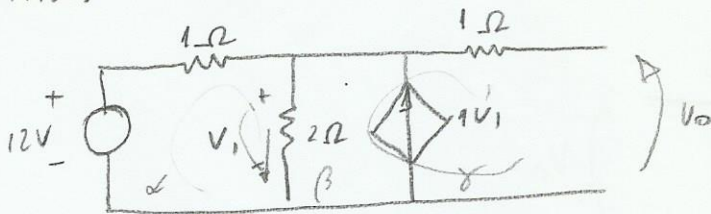


Determinação do RL



$$\frac{4 \cdot 2}{6} = \frac{8}{6} = \frac{4}{3} \quad R = \frac{4}{3} + 4 = \frac{16}{3}$$

5.45.)



$$3\alpha - 2\beta = 12$$

$$2\beta + \gamma - 2\alpha = -v_{oc}$$

$$3\alpha - 4\alpha = 12$$

$$-\alpha = 12 \Rightarrow \alpha = -12$$

$$\gamma - \beta = v_1 ; v_1 = 2(\alpha - \beta)$$

$$\beta = -2(\alpha - \beta)$$

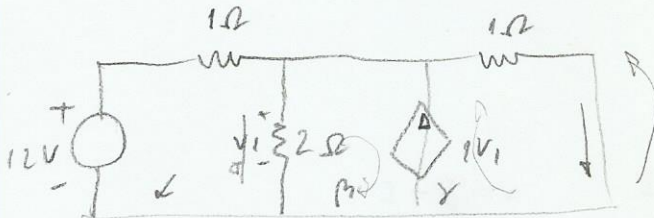
$$\beta = -2\alpha + 2\beta \quad -\beta = -2\alpha$$

$$\beta = 2\alpha$$

$$v_{oc} = -(2\beta - 2\alpha)$$

$$= -(4\alpha - 2\alpha) = -(-12 \cdot 4 - 2 \cdot (-12)) \therefore v_{oc} = \underline{24V}$$

$$-48 + 24 = -24$$



$$3\alpha - 2\beta = 12$$

$$2\beta + \gamma - 2\alpha = 0$$

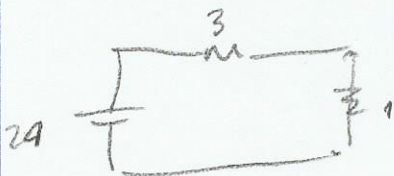
$$3\alpha - 2\beta = 12$$

$$-2\alpha + 2\beta + 2\alpha - \beta = 0$$

$$\left\{ \begin{array}{l} 3\alpha - 2\beta = 12 \\ \beta = 0 \end{array} \right. \Rightarrow 3\alpha = 12 \therefore \alpha = 4$$

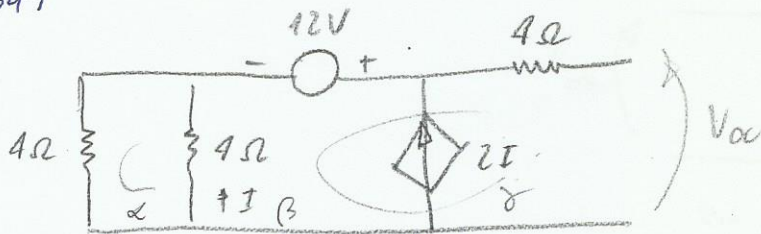
$$\gamma = 2\alpha - \beta \therefore \gamma = \beta = 8A$$

$$R_{th} = \frac{24}{8} = \frac{12}{4} = 3$$



$$v_o = \frac{1}{1+3} \cdot 24 = \frac{24}{4} = \underline{6V}$$

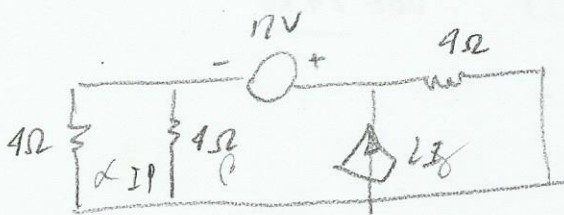
5.39-1)



$$\begin{cases} 0\alpha - 4\beta = 0 & \gamma - \beta = 2I & \beta - \alpha = I \\ 4\beta + 4\gamma - 4\alpha = 12 - V_{oc} & \beta = -2I & \alpha = \beta - I \\ & & \alpha = -3I \end{cases}$$

$$-12I + 8I = 0 \implies I = 0, \beta = 0, \alpha = 0$$

$$V_{oc} = 12$$



$$\begin{cases} 0\alpha - 4\beta = 0 & \beta - \alpha = I & \alpha = \beta - I \\ 4\beta + 4\gamma - 4\alpha = 12 & \gamma - \beta = 2I & \gamma = 2I + \beta \end{cases}$$

$$0\alpha - 4\beta = 0$$

$$\gamma = 2I + \beta$$

$$4\beta + 12\beta - 4\alpha - 4\alpha = 12$$

$$\gamma = 2\beta - 2\alpha + \beta = 3\beta - 2\alpha$$

$$16\beta - 6\alpha = 12$$

$$\gamma = 2(0\beta) = 12 \implies \beta = \frac{12}{10} = \frac{6}{5}, \alpha = \frac{6}{10} = \frac{3}{5}$$

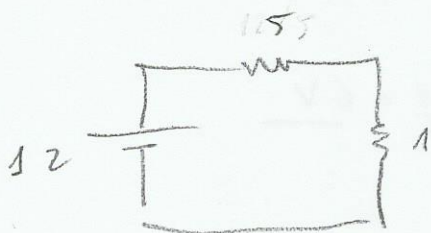
$$16\beta - 6\alpha = 0$$

$$\gamma = 2(\beta - \alpha) + \beta$$

$$R_{th} = 12 \cdot \frac{12}{5}$$

$$\gamma = 3\beta - 2\alpha = 3 \cdot \frac{6}{5} - \frac{6}{5} = \frac{18-6}{5} = \frac{12}{5}$$

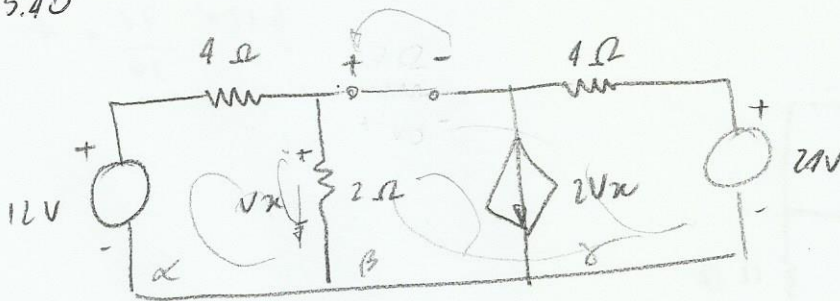
$$= 5$$



$$V_0 = \frac{1}{14.5} \cdot 12 = 2$$

$$I = 2A$$

5.40



$$6\alpha - 2\beta = 12$$

$$2\beta + 4\gamma - 2\alpha = -24$$

$$3\alpha - \beta = 12$$

$$2\beta + 10\gamma - 16\alpha - 2\alpha = -24$$

$$\beta - \gamma = 2Vx$$

$$\beta - \gamma = 2(2(\alpha - \beta))$$

$$\beta - \gamma = 4\alpha - 4\beta$$

$$\gamma = 5\beta - 4\alpha$$

$$3\alpha - \beta = 12$$

$$22\beta - 18\alpha = -24$$

$$18\alpha - 6\beta = 36$$

$$-18\alpha + 22\beta = -24$$

$$16\beta = 12$$

$$\beta = \frac{12}{16} = \frac{6}{8} = \frac{3}{4}$$

$$I_{NL} = \frac{3}{4}$$

Determinasi V_{oc}

$$6\alpha - 2\beta = 12$$

$$2\beta + 4\gamma - 2\alpha = -V_{oc} - 24$$

$$\alpha = 2$$

$$-16\alpha - 2\alpha = -V - 24$$

$$V = -24 + 18 \cdot 2 \quad \therefore \quad V = \underline{12V}$$

$$R_{th} = \frac{12 + \frac{3}{4}}{\frac{3}{4}} = \frac{12.4}{\frac{3}{4}} = 4.4 \approx 16$$

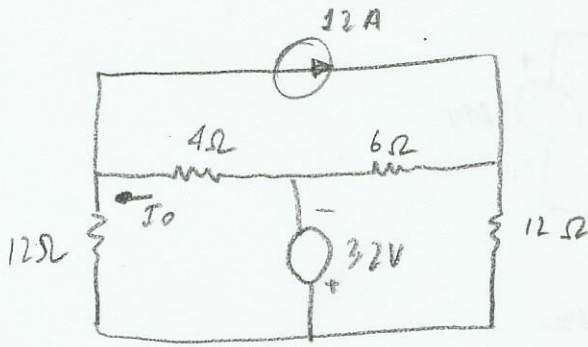


$$V = \frac{2}{2+16} \cdot 12 = \frac{24}{18} = \frac{12}{9} = \frac{4}{3} V = 1.33$$

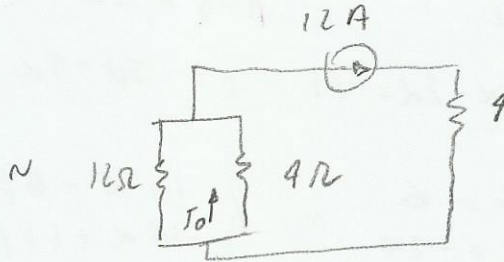
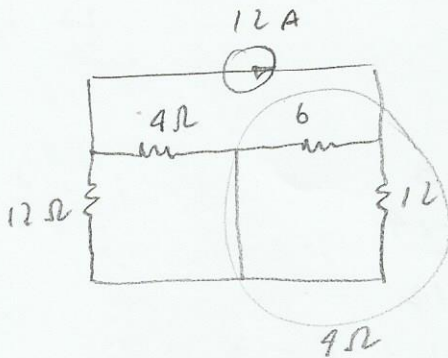
$$V = \underline{4V}$$

5.9

$$6-12 = \frac{72}{16} = 4$$



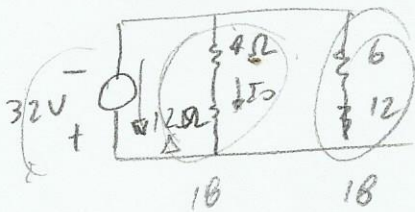
Influência de 12A



$$I_0 = \frac{12}{12+4} \cdot 12 = \frac{12 \cdot 12}{16} = \frac{12 \cdot 6}{8} = \frac{12 \cdot 3}{4}$$

$$I_0' = \frac{3 \cdot 3}{3+3} = 9$$

Influência de 32V

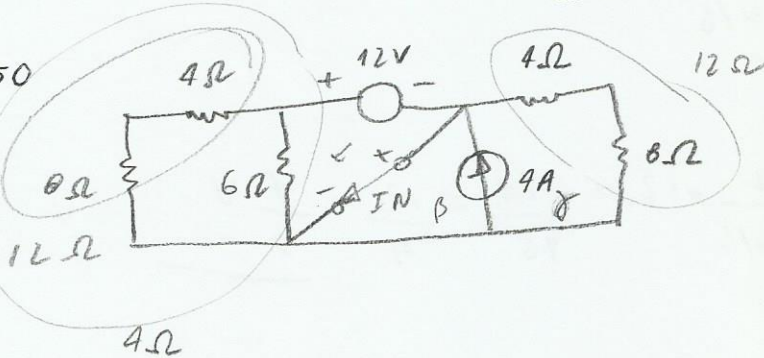


$$\therefore I_T = \frac{32}{9} = 4$$

$$I_0' = -2$$

$$I = 4 - 2 = 2 \text{ A}$$

5.50



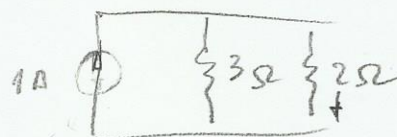
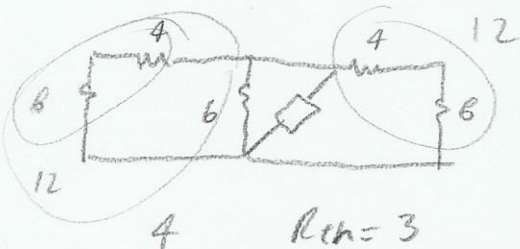
$$4 \alpha = -12 \quad 12 \gamma = 0$$

$$\alpha = -3 \quad \gamma = 0$$

$$X_1^0 - \beta = 4 \quad \therefore \beta = -4$$

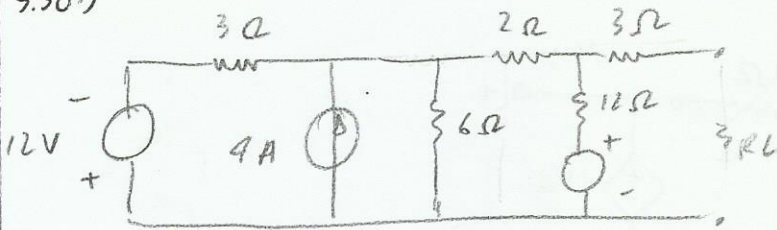
$$\alpha - \beta = I_N$$

$$I_N = -3 - (-4) = 1 \text{ A}$$

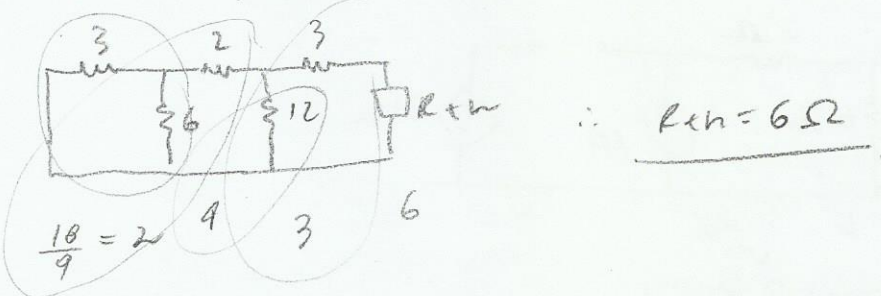


$$I_0 = \frac{3}{2+3} \cdot 1 = \frac{3}{5} \text{ A}$$

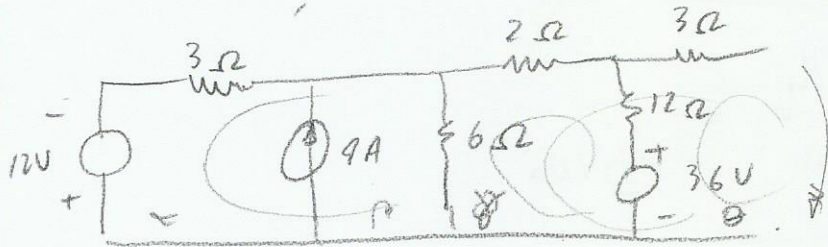
5.58.)



Determinação do R_{th}



Determinação do E_{th}



$$\begin{cases} 3\alpha + 6\beta - 6\gamma = -12 \\ 8\gamma - 6\beta - 12\theta = -36 \\ 15\theta - 12\gamma = -V + 36 \end{cases} \quad \begin{cases} \beta - \alpha = 4 \\ \beta = 4 + \alpha \end{cases}$$

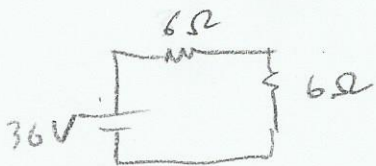
$$\begin{cases} 3\alpha + 24 + 6\alpha - 6\gamma = -12 \\ 8\gamma - 24 - 6\gamma = -36 \end{cases} \sim \begin{cases} 9\alpha - 6\gamma = 12 \\ 2\gamma = -12 \end{cases}$$

$$\gamma = -6$$

$$9\alpha - 6\gamma = 12$$

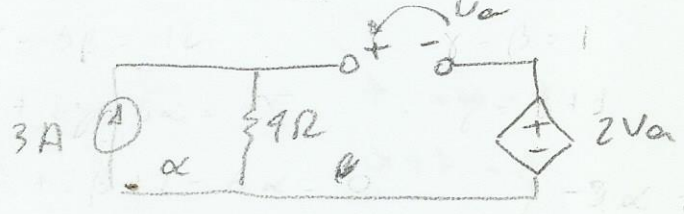
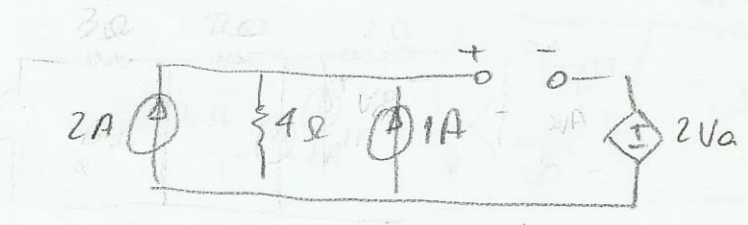
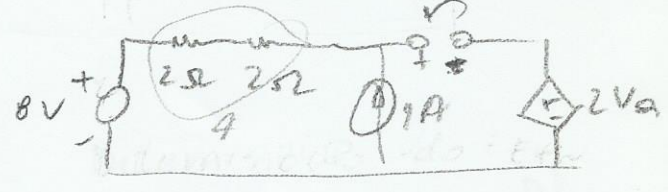
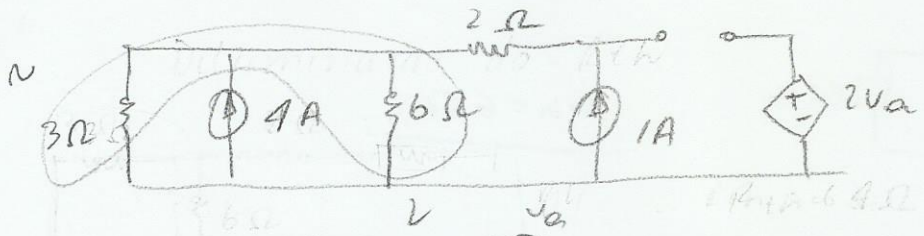
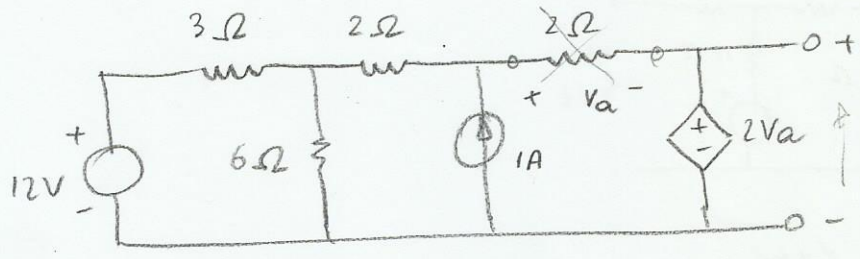
$$3\alpha - 2\gamma = 4 \quad \alpha = \frac{4 + 2 \cdot (-6)}{3} = \frac{4 - 12}{3} = -3$$

$$V = -12 \cdot (-6) - 36 = 72 - 36 = 36$$



$$P = V \cdot I = V \cdot \frac{V}{R} = \frac{V^2}{R} = \frac{36^2}{6} = \frac{36 \cdot 36}{6} = 36 \cdot 6 = 216$$

$\therefore P = 216W$



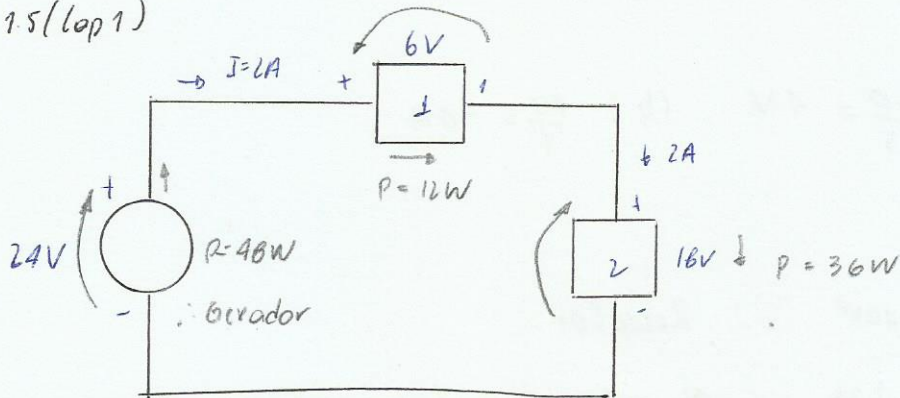
$$\begin{aligned}
 4\alpha - \beta &= 10 \\
 6\alpha - \beta &= 12 \\
 4\alpha - 6\beta &= -12 \\
 4\beta - 4\alpha &= -Va - 2Va \quad ; \quad \alpha = 3 \quad \beta = 2 \\
 \beta &= \frac{2}{3}
 \end{aligned}$$

$I_N = -8 - (5)$

$I_N = 5$

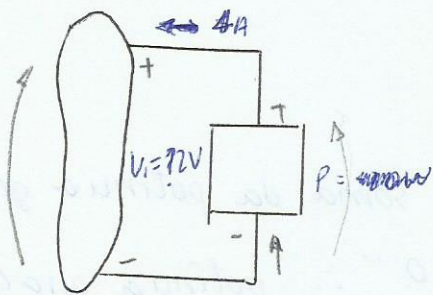
Fontes dependentes e independentes

Exemplo 1.5 (lap 1)

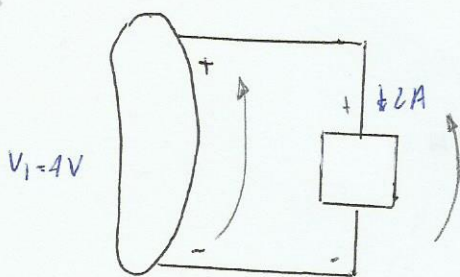


Exercício 1.1

Determine a quan. de potência absorvida ou fornecida pelos componentes



∴ Gerador $P = 12 \cdot 4 = -48W$



∴ Receptor $P = 2 \cdot 4 = 8W$

Conclusão:

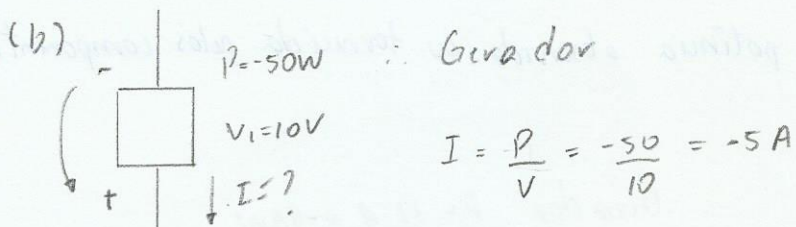
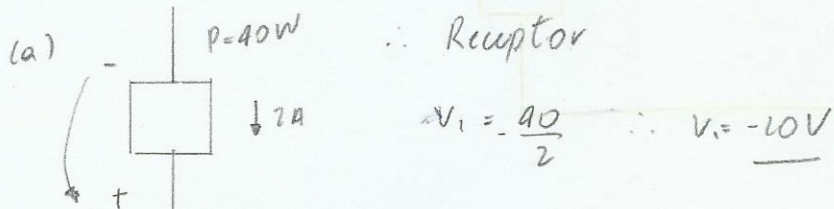
- Gerador, a $v(t)$ e $i(t)$ possuem o mesmo sentido
 $p(t) = v(t) \cdot i(t)$; $p(t) < 0$
- Receptor, a $v(t)$ e $i(t)$ possuem sentidos opostos
 $p(t) = v(t) \cdot i(t)$; $p(t) > 0$

Determinar as variáveis faltantes:

Ex. 1.4

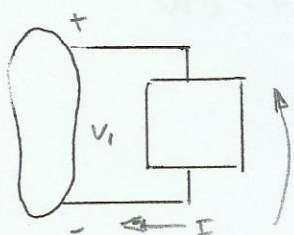
(a) $V = \frac{P}{I} = \frac{20}{5} = 4V$ (b) $\frac{40}{5} = -8A$

E.1.2



*Obs.: Balanço energético, significa que a soma da potência gerada + potência recebida é igual a "0" \therefore potência gerada igual a potência recebida

1.8



(a) $V_1 = 10$ e $I = 3A$

\therefore Receptor

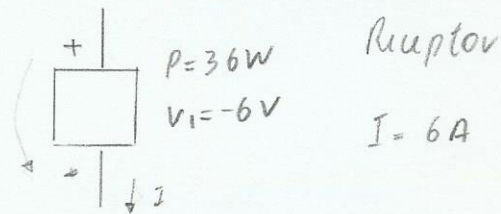
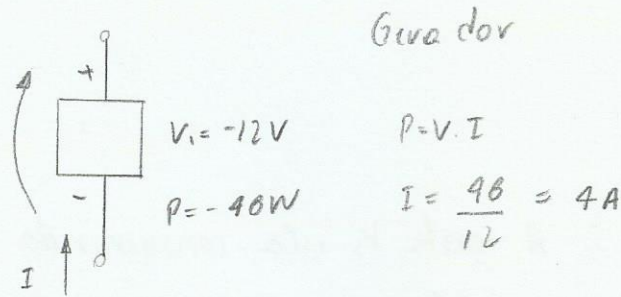
$P = 10 \cdot 3 = 30W$

(b) $V_1 = 4$ e $I = -4A$

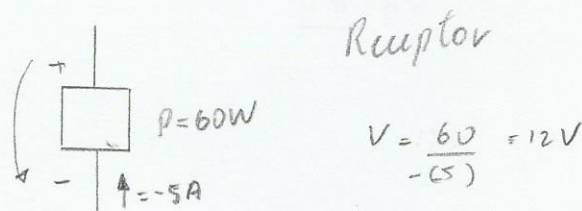
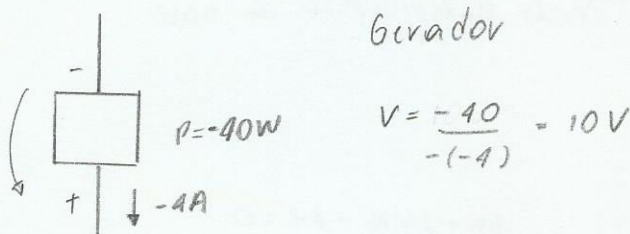
\therefore Gerador

$P = 4 \cdot -4 = -16W$

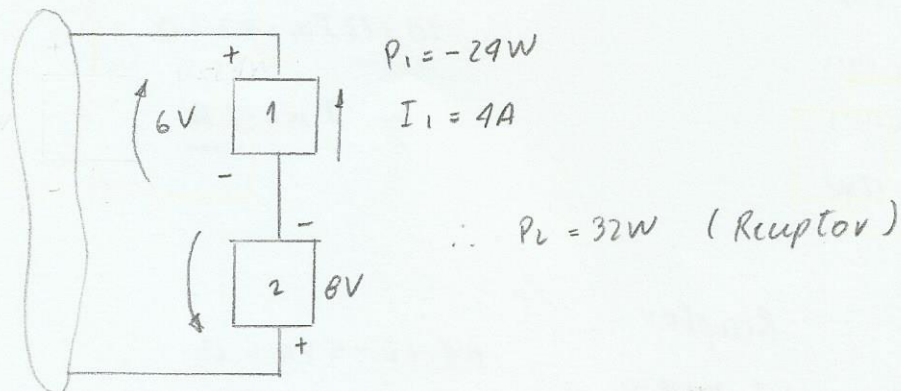
1.9



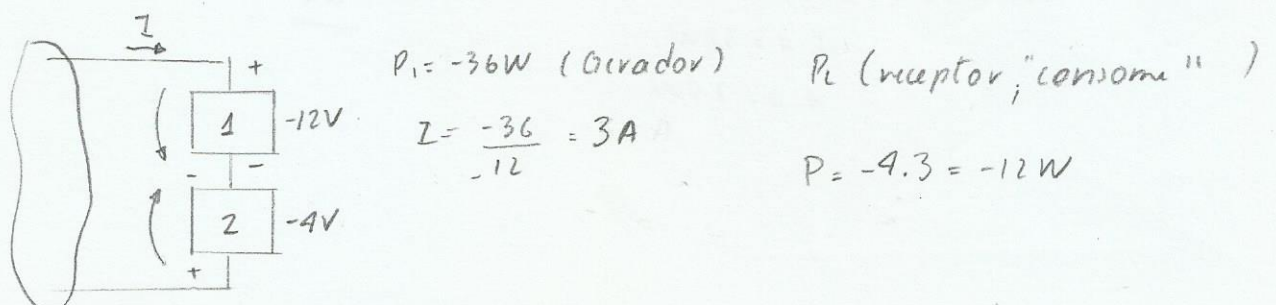
1.10



1.11



1.12



1.13

Geradores: $-144W$

Receptores: $30 + 18 + 96 = 96W$

$$G + R = 0$$

$$-144 + 96 + x = 0$$

$$\therefore x = \underline{48W}$$

\therefore A fonte V_s esta consumindo potência de $96W$.

1.14

Potências consumidas:

$$P_1 = 12W; P_2 = 12W; 36W; P_3 = 8W$$

Potências fornecidas: $12W$ e fonte dependente de $56V$

1.15

Consumidos	Fornecidos
$2 \cdot 6 = 12W$	$2 \cdot 24 = 48W$
$2 \cdot 12 = 24W$	$2 \cdot 18 = 36W$
$2Vx = 2Vx$	
$2 \cdot 16 = 32W$	

$$\therefore 68 + 2Vx - 84 = 0$$

$$\therefore Vx = \underline{8V}$$

1.16

Consumidas	Fornecida
$2 \times 12 = 24W$	$12 \cdot 6 = 72$
$1 \times 12 = 12W$	
$4I_x (W)$	
$8I_x (W)$	
$1 \cdot 12 = 12W$	

$$\therefore 48 + 12I_x - 72 = 0$$

$$\therefore I_x = \underline{2A}$$

1.17

Gerador	Receptor
$2 \times 6 = 12W$	$2 \cdot 2 = 4W$
$4V_x (W)$	$6 \cdot 4 = 24W$
	$8 \cdot 4 = 32W$
	$4 \cdot 6 = 24W$

$$84 - 12 - 4V_x = 0$$

$$\therefore V_x = \underline{18V}$$

1.16 Consumidos fornecida

$12 \cdot 8 = 96W$	$6Vx (W)$
$18 \cdot 2 = 36W$	$12 \cdot 6 = 72W$
$6 \cdot 6 = 36W$	
$4 \cdot 6 = 24W$	
$18 \cdot 4 = 72W$	

$$264 - 72 - 6Vx = 0$$

$$Vx = \underline{24V}$$

1.19 Gerador Receptor

$3 \cdot 10 = 30W$	$6I_0 (W)$
$6 \cdot 2 = 12W$	$11 \cdot 16 = 176W$
$12 \cdot 4 = 108W$	
$8 \cdot 4 = 32W$	

$$-182 + 176 + 6I_0 = 0$$

$$\therefore I_0 = \underline{1A}$$

1.20 Gerador Receptor

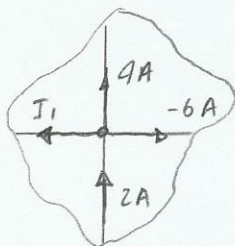
$24 \cdot 6 = 144W$	$8 \cdot 6 = 48W$
$8 \cdot 3 = 24W$	$10 \cdot 4 = 40W$
	$6I_0 (W)$
	$2 \cdot 16 = 32W$
	$1 \cdot 6 = 6W$
	$8 \cdot 3 = 24W$

$$150 + 6I_0 - 168 = 0$$

$$\therefore I_0 = \underline{3A}$$

Capítulo 2 - Circuitos Resistivos

E2.3



$$I + 4 - 6 - 2 = 0$$

$$I = 4A$$

E2.4 nó 1: $3 - 2 - 4 - I_1 = 0 \quad \therefore I_1 = -3A$

nós 2: $I_2 + 3 + 1 - 2 = 0 \quad \therefore I_2 = -2A$

nó 3: $I_2 - 4 + 4 + 2 = 0 \quad \therefore I_2 = -2A$

nó 4: $I_3 - 1 - 4 + 2 = 0 \quad \therefore I_3 = 3A$

Resumo:

$$v(t) = R i(t)$$

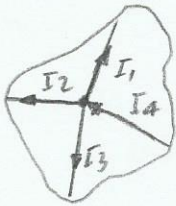
$$G = \frac{1}{R}$$

$$p(t) = R i^2(t) = \frac{v^2(t)}{R}$$

Leis de Kirchhoff

"A soma algébrica das correntes entrando em qualquer nó é zero".

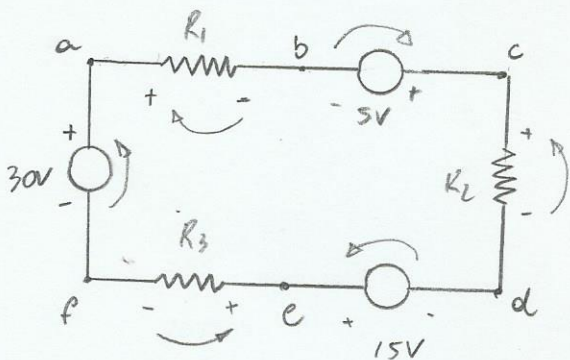
"A soma algébrica das tensões ao longo de qualquer laço é zero".



$$I_1 + I_2 + I_3 - I_4 = 0$$

Obs.: Quando a corrente sai do nó, ela é positiva, caso contrário é negativa.

Ex:



$$-V_{R1} + 5V - V_{R2} + 15 - V_{R3} + 30 = 0$$

Admitindo $V_{R1} = 18V - V_{R2} = 12V$

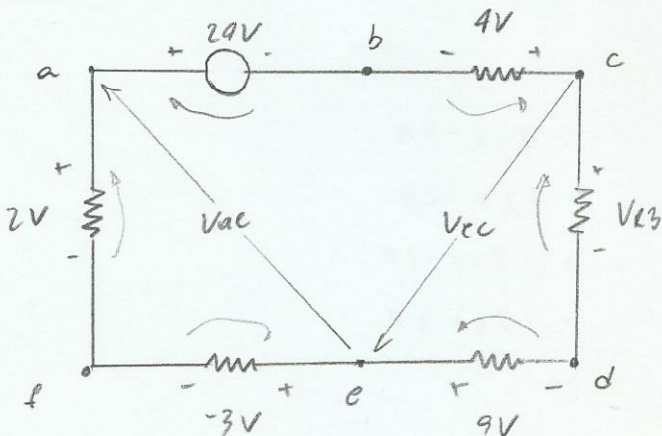
$$V_{R3} = 20V$$

$$-V_{R1} + V_{R2} + V_{R3} = 5 + 15 + 30$$

$$V_{R1} + V_{R2} + V_{R3} = 50$$

$$18 + 12 + 20 = 50$$

Exemplo 2.9



Determine

V_{ae}, V_{ec} e V_{R3}

$$-24 + 4V - V_{R3} + 9 + 3 + 2 = 0 \quad \therefore V_{R3} = \underline{-6V}$$

$$-V_{ac} + 3 + 2 = 0 \quad \therefore V_{ac} = 5V$$

$$V_{ec} - 9 - 6 = 0 \quad \therefore V_{ec} = \underline{15V}$$

E2.5

$$-4 - V_{R2} + 6 + 12 = 0 \quad \therefore V_{R2} = \underline{14V}$$

$$V - 14 + 6 = 0 \quad \therefore V = 8 \quad V_{bd} = -V$$

$$V_{bd} = \underline{-8V}$$

E2.6 $12 + 1 + 4 + 2 - 24 - V_{r4} = 0 \quad \therefore V_{r4} = \underline{-5V}$

$$V_{bt} - 1 - 12 = 0 \quad \therefore V_{bt} = \underline{13V}$$

$$V_{ec} + 24 - 2 = 0 \quad \therefore V_{ec} = \underline{-22V}$$

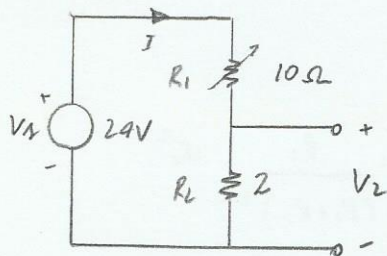
Divisor de tensão

Divisor de corrente

$$V_{R2}(t) = \frac{R_2}{R_1 + R_2} v(t)$$

$$i_2(t) = \frac{R_1}{R_1 + R_2} i(t)$$

Exemplo:



$$V_s = V_{R1} + V_{R2}$$

$$V_s = R_1 \cdot I + R_2 \cdot I$$

$$V_s = I(R_1 + R_2)$$

$$I = \frac{V_s}{R_1 + R_2}$$

$$V_{R1} = R_1 \cdot I$$

$$V_{R2} = R_2 \cdot I$$

$$\frac{V_{R1}}{R_1} = \frac{V_s}{R_1 + R_2} \sim V_{R1} = \frac{R_1}{R_1 + R_2} V_s$$

$$\frac{V_{R2}}{R_2} = \frac{V_s}{R_1 + R_2} \sim V_{R2} = \frac{R_2}{R_1 + R_2} V_s$$

$$V_2 = \frac{2}{2 + 10} \cdot 24 \quad \therefore V_2 = \underline{4V}$$

Problemas

2.1 nó 1: $16 - I_0 - 3 - 4 - 2 = 0 \quad \therefore I_0 = 7A$

nó 2: $-16 + I_1 + 7 = 0 \quad \therefore I_1 = 9A$

nó 3: $I_2 - 9 + 3 = 0 \quad \therefore I_2 = 6A$

2.2 nó A: $I_1 + 4 - 12 = 0 \quad \therefore I_1 = 12A$

nó D: $I_3 - 4 - 2 = 0 \quad \therefore I_3 = 6A$

nó C: $9 - I_2 - 6 - 12 = 0 \quad \therefore I_2 = -9A$

nó B: $I_4 - 9 + 12 = 0 \quad \therefore I_4 = -3A$

2.3 nó E: $2 - 9 - I_4 = 0 \quad \therefore I_4 = -7A$

nó B: $I_2 + 12 - 7 = 0 \quad \therefore I_2 = -5A$

nó D: $I_3 - 4 - 2 = 0 \quad \therefore I_3 = 6A$

nó C: $9 + 5 - 6 - I_1 = 0 \quad \therefore I_1 = 8A$

2.4 Observação:

$$P_1(t) = v_1(t) \cdot i_1(t) = \frac{v_1^2(t)}{R}$$

$$P_1(t) = \frac{v_1^2}{R_1} = \frac{R_1^2 \cdot v_1^2}{(R_1 + R_2)^2} \cdot R_1 \quad \therefore P_1(t) = \frac{R_1}{(R_1 + R_2)^2} \cdot v_1^2$$

$$P = \frac{2}{(2+10)^2} \cdot 12^2 \quad \therefore P = 2W$$

2.5 $R^1 = \frac{(3+1) \cdot 4}{(3+1+4)} = 2 \quad V^1 = 12V$

$$P = \frac{1}{(1+3)^2} \cdot 12^2 \quad \therefore P = 9W$$

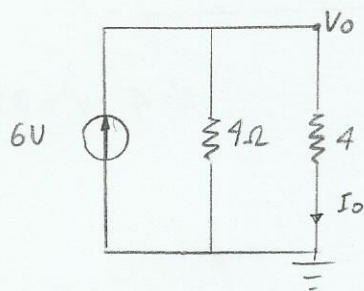
2.6

Usando as somas das tensões, e igualando a "0".

$$12 - 6I_1 + 12 = 0 \quad \therefore$$

$$I_1 = \underline{4A}$$

2.7



$$V_0 = \underline{6V}$$

$$I_T = \frac{6}{2} = 3A$$

$$I_0 = \frac{4}{8} \cdot 3 = \underline{1,5A}$$

2.8

$$R_1 = \left(\frac{1}{7,5} \right) \div \left(\frac{1}{7} + \frac{1}{5} \right) = 0,0833$$

$$R_2 = \frac{1}{12} + \frac{1}{4} + \frac{1}{6} = 0,5$$

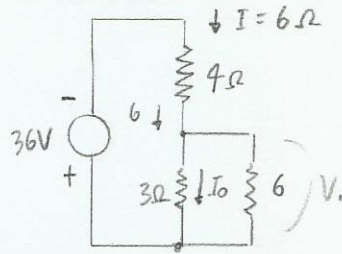
$$R_3 = \frac{0,5 \cdot 0,5}{1} = 0,25$$

$$R = \frac{1}{12} + \frac{1}{6} + \frac{1}{4} \quad \therefore R = 0,5 \Omega$$

$$\therefore G = 2N$$

2.9 $12,5 \Omega$

2.10
 $R_{eq} = 6 \Omega$
 $I_T = 6 A$



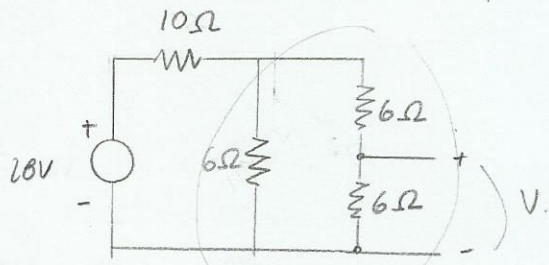
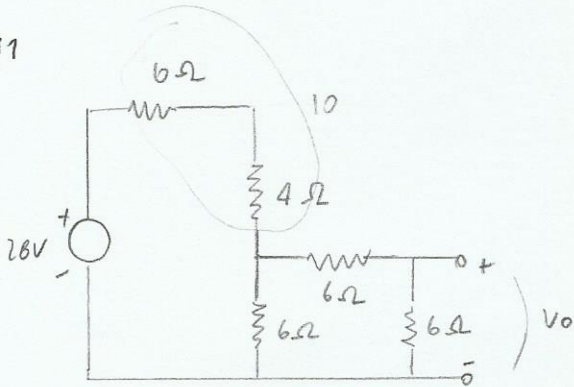
$$3I_0 = 6I'$$

$$I' = \frac{3I_0}{6} = \frac{I_0}{2}$$

$$I = \frac{I_0}{2} + I_0 = \frac{3I_0}{2}$$

$$I_0 = \frac{2I}{3} = \frac{2 \cdot 6}{3} = 4 A$$

2.11



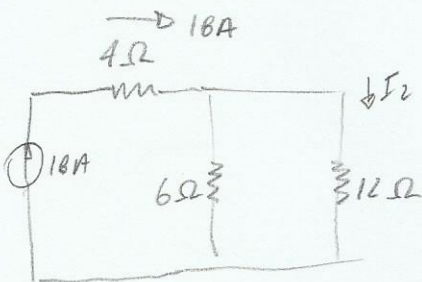
$R' = 4 \quad V' = 8V$

$$V' = \frac{4}{14} \cdot 28 = 8V$$

$$V = \frac{6}{12} \cdot 8 = 4V$$

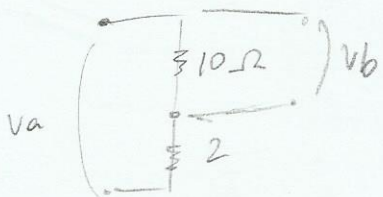
2.12

$V_a = 18 \cdot 4 = 72V$



$$I_2 = \frac{6}{6+12} \cdot 18 \therefore I_2 = 6A \therefore I_1 = 12A$$

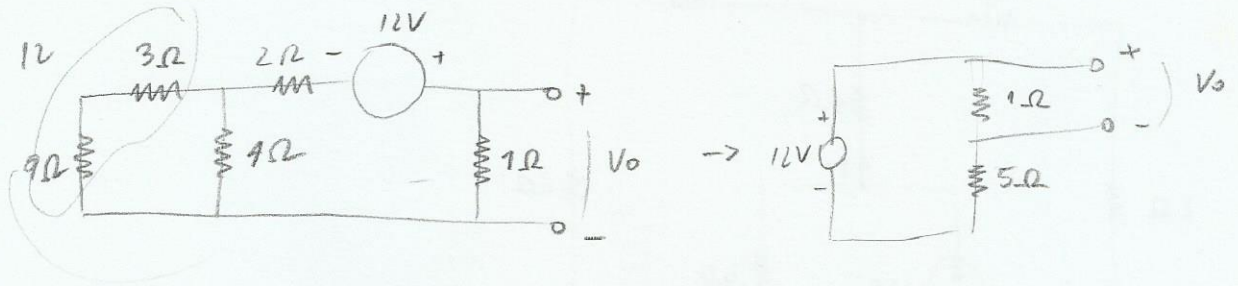
$V_2 = 72V = V_a$



$$\therefore V_b = \frac{10}{10+2} \cdot 72 \therefore V_b = 60V$$

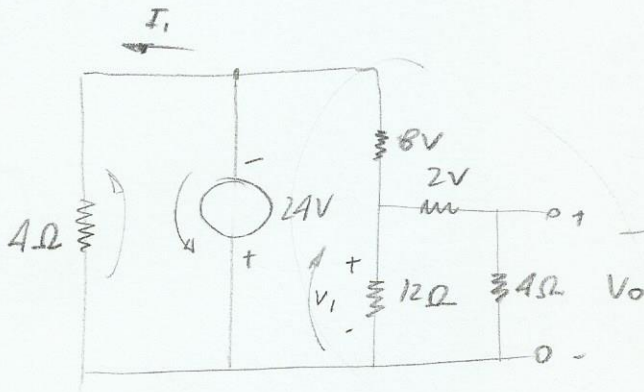
$2.12 - 60 - V_c = 0 \therefore V_c = -36V$

2.13.) Determine V_0



$$V_0 = \frac{1}{5+1} \cdot 12 = \underline{2V}$$

2.14.) Determine I_1 & V_0

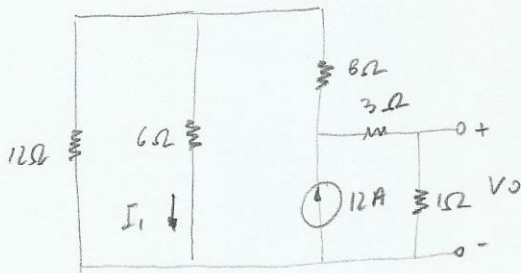


$$I_1 = \frac{24}{4} = \underline{6A}$$

$$V_1 = \frac{4}{4+8} \cdot 24 \therefore V_1 = 8V$$

$$V_0 = \frac{4}{2+4} \cdot 8 \therefore V_0 = \underline{\underline{-\frac{16}{3}V}}$$

215



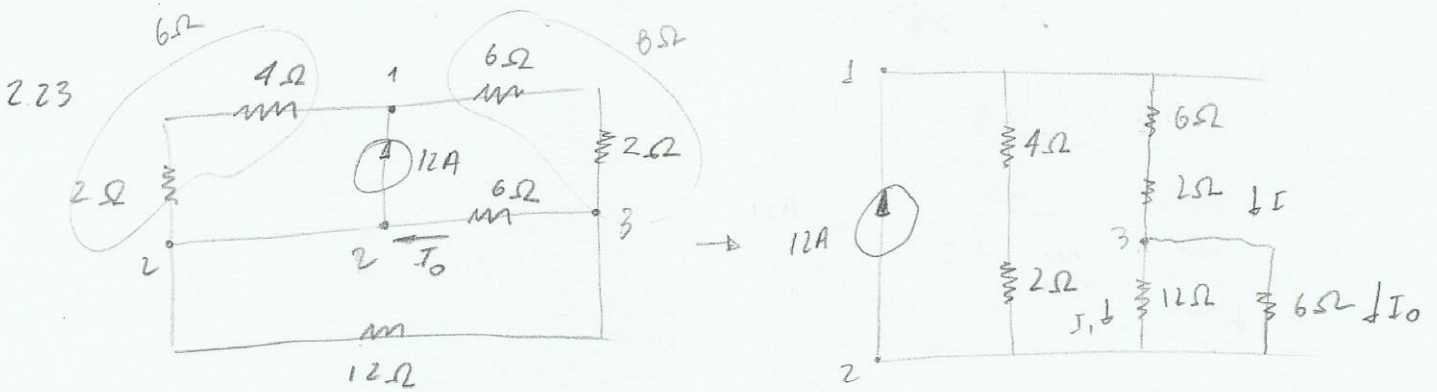
Determine I_1 & V_0

$$V = 12 \cdot 12 = 144V$$

$$I_1 = \frac{144}{6} \therefore I_1 = \underline{24A}$$

$$V' = 12 \cdot 4 = 48V$$

$$V_0 = \frac{1}{3+1} \cdot 48 \therefore V_0 = \underline{12V}$$



$$R_{eq} = 4 \quad V_{12} = 96V$$

$$V_{32} = \frac{4}{12} \cdot 96 = 16V$$

$$\therefore I_0 = \frac{16}{6} = \frac{8}{3} A$$

0V

$$12I_1 = 6I_0$$

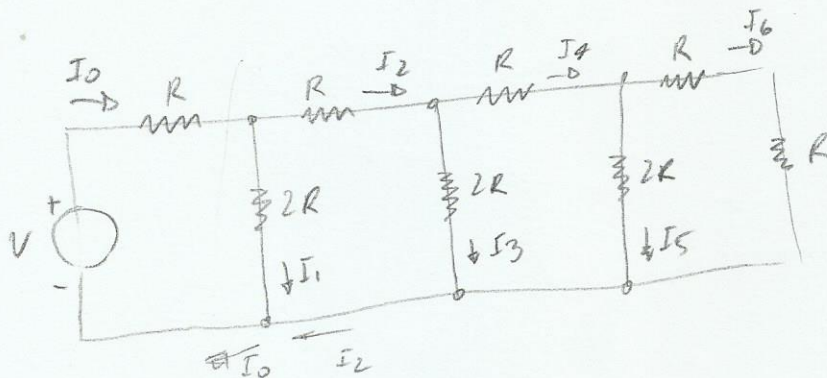
$$I_1 = \frac{6I_0}{12} = \frac{I_0}{2}$$

$$\therefore I = \frac{I_0}{2} + I_0 = \frac{3I_0}{2}$$

$$I = \frac{96}{12} = 8$$

$$\therefore I_0 = \frac{2 \cdot 8}{3} = \frac{16}{3} A$$

2.24



$$R_{eq} = 2R$$

$$I_1 = \frac{2R}{2R+2R} \cdot I_0 = \frac{2R I_0}{4R} \quad \therefore I_1 = \frac{I_0}{2} A$$

$$I_0 = \frac{V}{2R}$$

$$I_L + I_1 = I_0$$

$$I_L = I_0 - \frac{I_0}{2} = \frac{I_0}{2} A$$

$$I_3 = \frac{2R'}{4R'} \cdot \frac{I_0}{2} = \frac{I_0}{4}$$

$$I_5 = \frac{2R}{4R} \cdot \frac{I_0}{4} = \frac{I_0}{8} \text{ A}$$

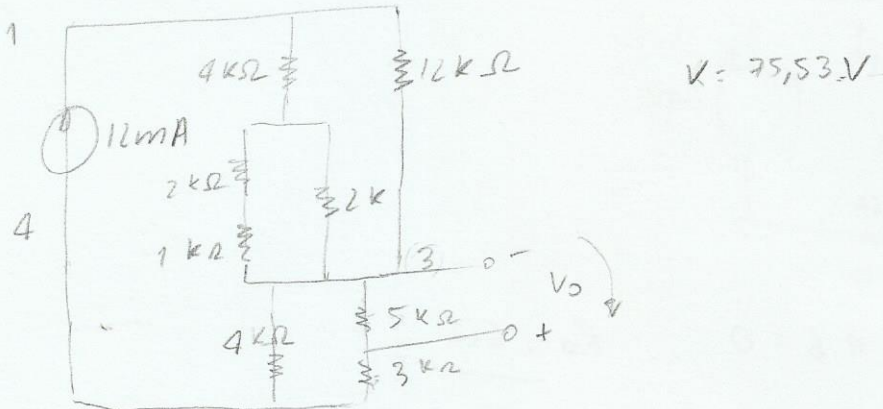
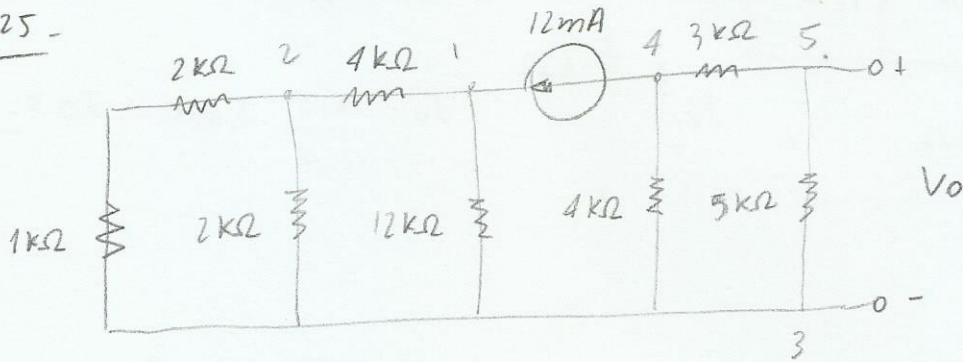
$$I_4 = I_2 - I_3$$

$$= \frac{I_0}{2} - \frac{I_0}{4} \therefore I_4 = \frac{I_0}{4}$$

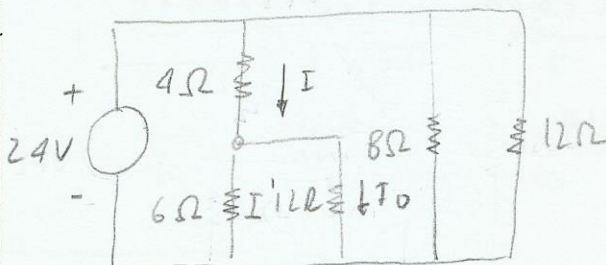
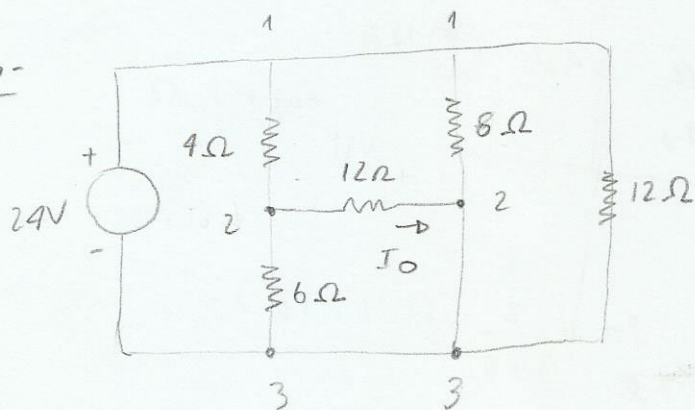
$$I_6 = I_4 - I_5$$

$$= \frac{I_0}{4} - \frac{I_0}{8} \therefore I_6 = \frac{I_0}{8} \text{ A}$$

225-



226-



$$6I' = 12I_0$$

$$I' = 2I_0$$

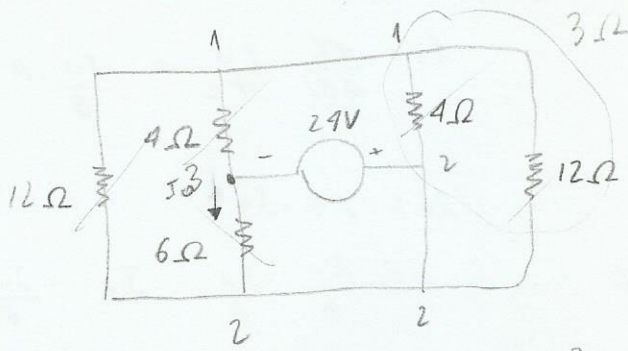
$$I = 3I_0$$

$$I = \frac{4,8 \cdot 24}{8+4,8} \cdot \frac{24}{3}$$

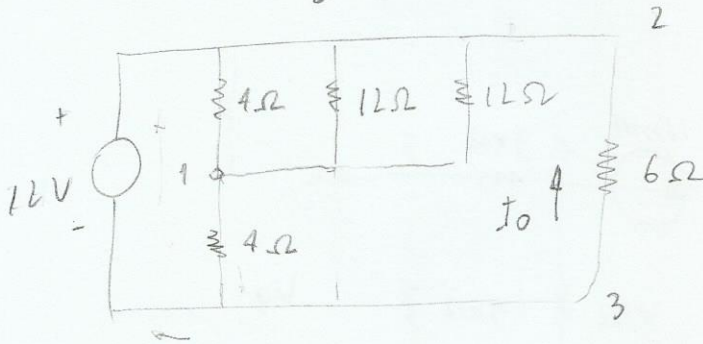
$$\therefore I = 3$$

$$I_0 = \underline{1 \text{ A}}$$

2.27



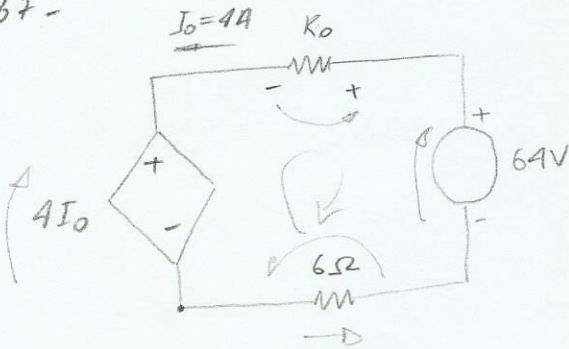
Determinare I_0



$$I_T = 3,875 \text{ A}$$

$$I_0 = \frac{6,4}{12,4} \cdot 3,875 \therefore I_0 = \underline{-2 \text{ A}}$$

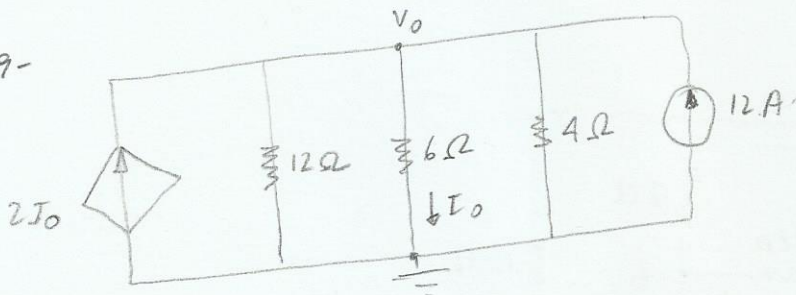
2.67-



Calculare R_0 :

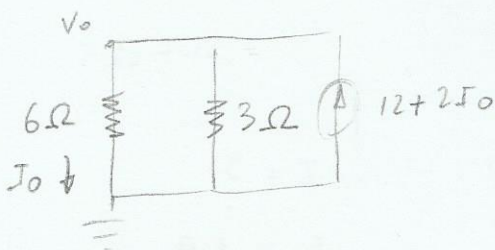
$$4 \cdot 4 + 4R_0 - 64 + 4 \cdot 6 = 0 \therefore R_0 = \underline{6 \Omega}$$

2.69-



Calcula V_0 :

$$R_{eq} = 2 \Omega$$



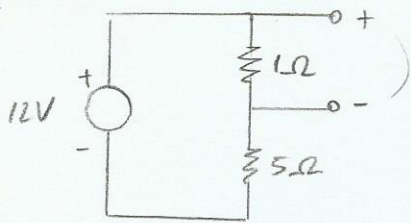
$$I_0 = \frac{3}{3+6} \cdot (12 + 2I_0)$$

$$I_0 = \frac{36 + 6I_0}{9} \rightarrow 9I_0 - 6I_0 = 36$$

$$\therefore I_0 = \underline{12 \text{ A}}$$

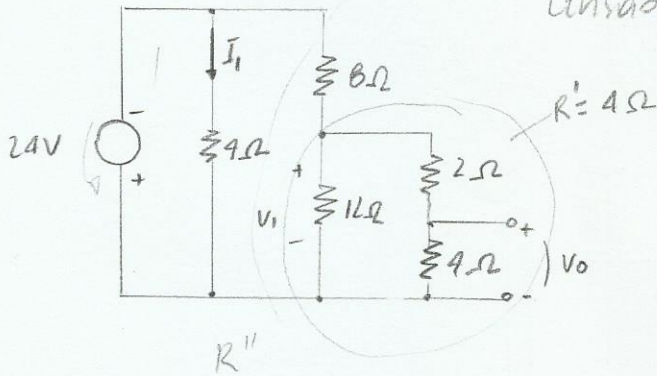
$$V_0 = 12 \cdot 6 \therefore V_0 = \underline{72 \text{ V}}$$

2.13



$$V = \frac{1}{6} \cdot 12 = \underline{2V}$$

2.14



Como determinar o sinal da minha tensão, quando eu uso um divisor.

$$V' = \frac{4}{12} \cdot 24$$

$$V' = 8V$$

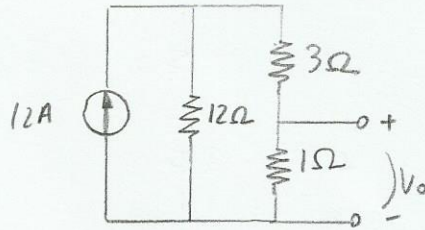
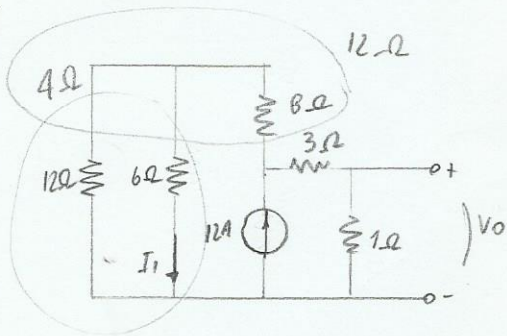
$$V_0 = \frac{4}{6} \cdot 8 = \underline{\frac{16}{3}V}$$

$$R_T = 3$$

$$I_T = 8A$$

$$I_1 = \frac{12}{16} \cdot 8 = \underline{6A}$$

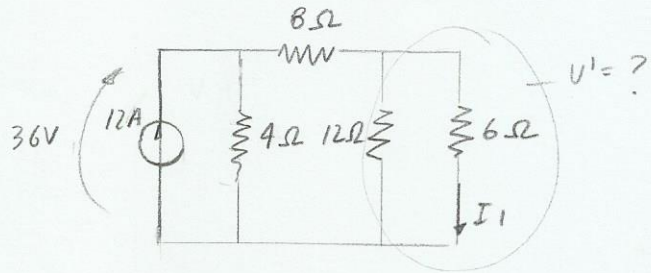
2.15



$$R_T = 3\Omega$$

$$V_T = 36V$$

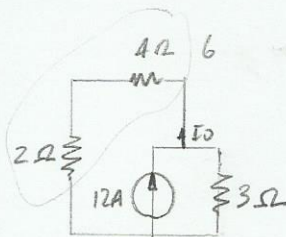
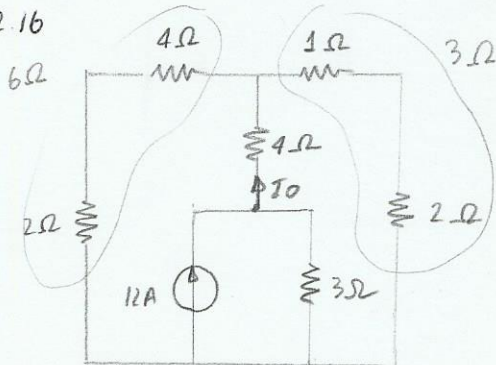
$$V_0 = \frac{1}{4} \cdot 36 = 9V$$



$$V' = \frac{4}{12} \cdot 36 = 12$$

$$I_1 = \frac{12}{6} = \underline{2A}$$

2.16



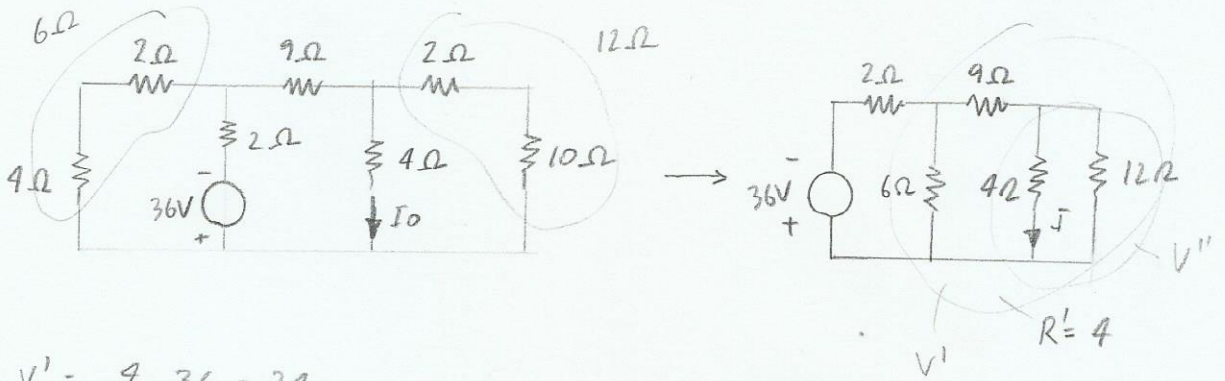
$$I_1 = \frac{R_2}{R_1 + R_2} \cdot I_T$$

$$12 = \frac{3}{3} \cdot I_0$$

2.17

$$R = [(10 + 2) \parallel (2 + (6 \parallel 3))] + 8 \quad \therefore R_T = 11 \quad \therefore V = 60V$$

2.18

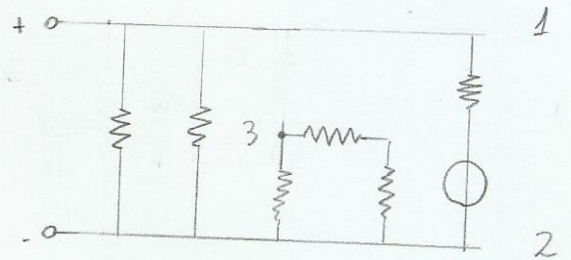
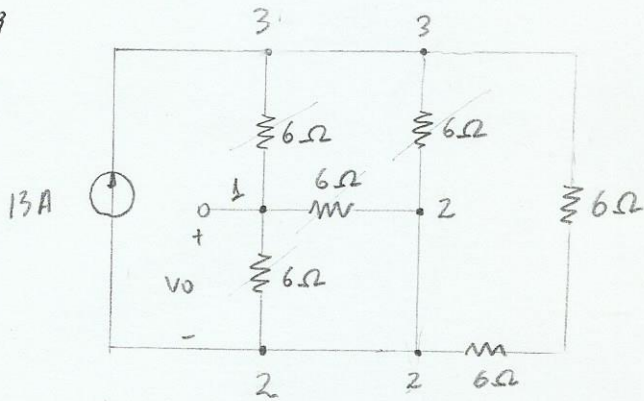


$$V' = \frac{4}{6} \cdot 36 = 24$$

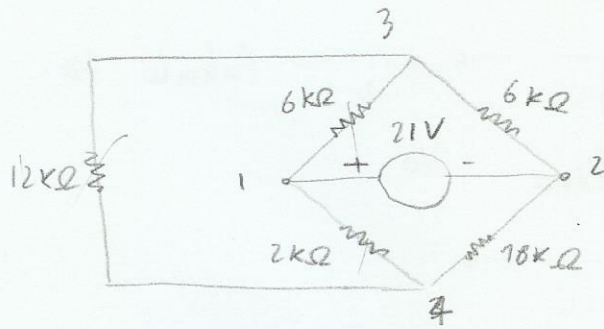
$$I_0 = \frac{6}{4} = 1.5A$$

$$V'' = \frac{3}{12} \cdot 24 = 6V$$

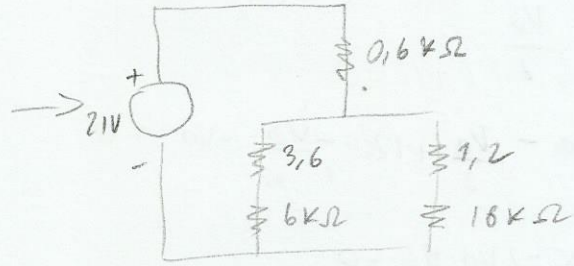
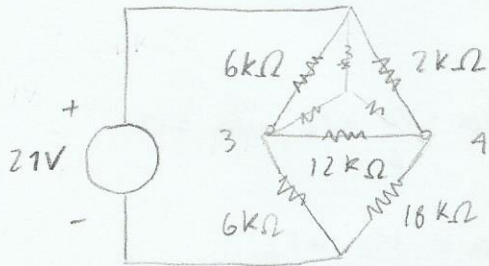
2.19



2.58



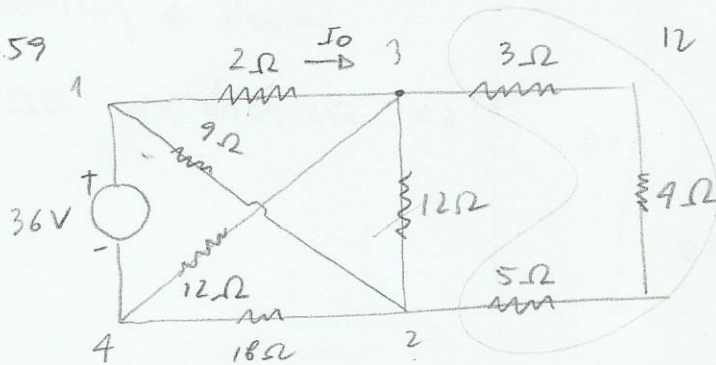
Encontre o potência dissipada no circuito total.



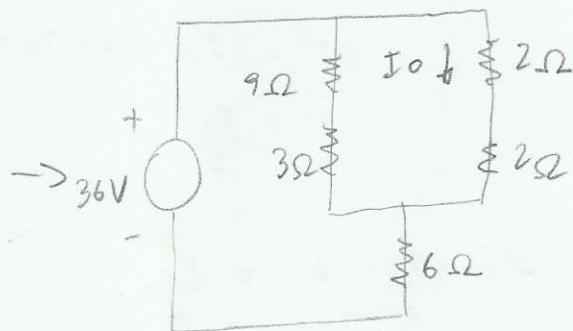
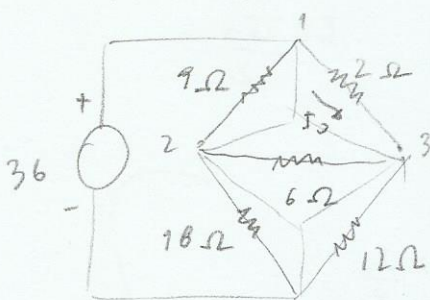
$$R_{eq} = 7$$

$$P = VI = V \cdot \frac{V}{R} = \frac{V^2}{R} = \frac{21^2}{7} \therefore P = \underline{63 \text{ mW}}$$

259



Calcule I_0 .



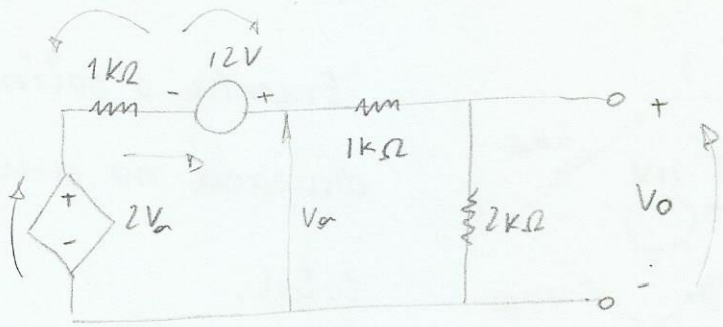
$$R_{eq} = 9$$

$$I_0 = \frac{12}{12+4} \cdot 4$$

$$I_T = \frac{36}{9} = 4A$$

$$\therefore I_0 = \underline{3A}$$

2.68 -



Calcule V_o

$$I = \frac{V_o}{2k\Omega}$$

$$2Va - 2I + 12 = 0$$

$$2Va - \frac{V_o}{2} + 12 = 0 \quad \frac{V_o}{2} - V_o = 0$$

$$2Va - \frac{V_o}{2} + 12 - Va = 0$$

$$Va = I + 12 \rightarrow I = Va - 12$$

$$Va = \frac{V_o}{2} - 12$$

$$2Va - 2Vo + 12 = 0$$

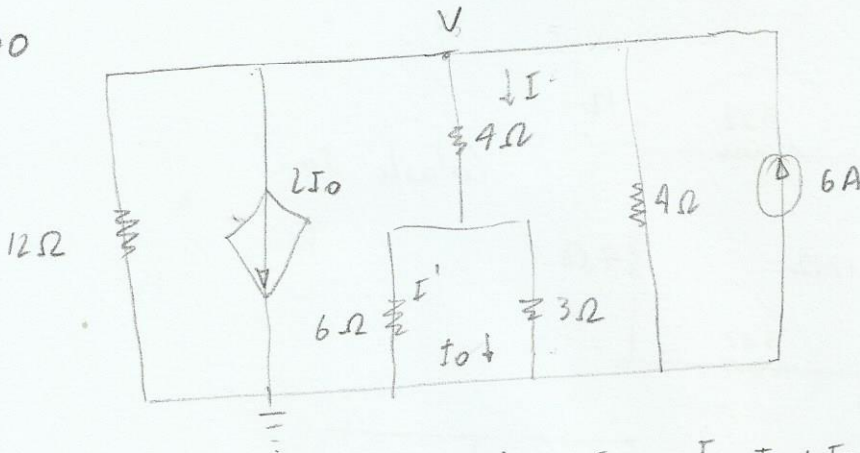
$$Va - Vo + 6 = 0$$

$$Vo - 6 = \frac{Vo}{2} - 12$$

$$Va = Vo - 6$$

$$\frac{Vo}{2} = -6 \quad \therefore \underline{Vo = -12V}$$

2.70



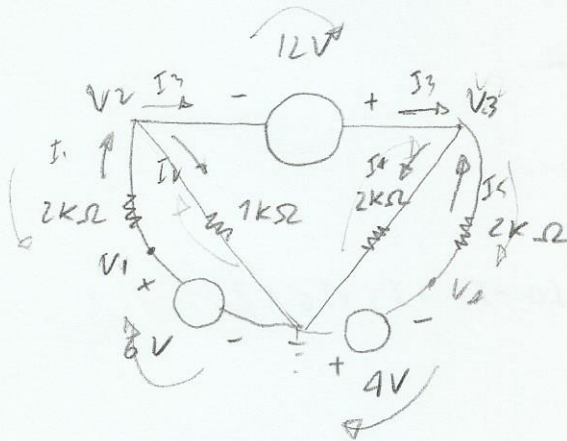
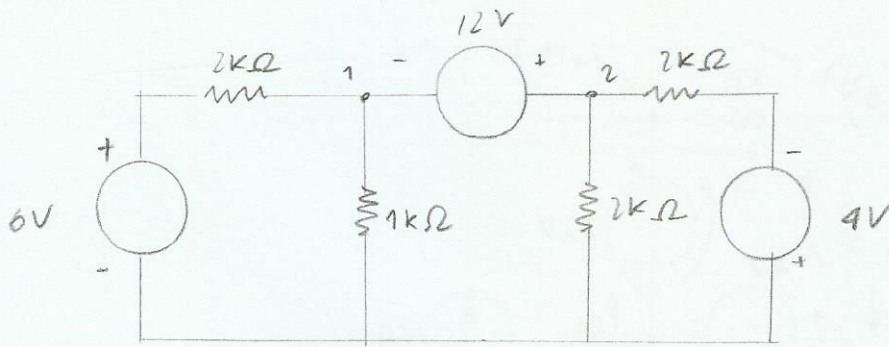
Calcule a potência dissipada em 12Ω

$$R_{eq} = 2\Omega$$

$$6I' = 3I_0 \quad I = I_0 + \frac{I_0}{2} \quad \therefore I = \frac{3I_0}{2}$$

$$I' = \frac{I_0}{2}$$

$$V = \frac{I}{6} \quad V = \frac{3I_0}{2} : 6 = \frac{I_0}{4} \quad \therefore V = \frac{I_0}{4}$$



$$\text{nó 1: } I_3 + I_2 - I_1 = 0$$

$$\text{nó 2: } I_4 - I_3 - I_5 = 0$$

$$-I_1 + I_2 + I_4 - I_5 = 0$$

$$- \left[\frac{6 - V_2}{2} \right] + \frac{V_2 - 0}{1} + \frac{V_3 - 0}{2} - \left[\frac{V_3 - 4}{2} \right] = 0$$

$$-6 + V_2 + 2V_2 + V_3 - V_3 - V_3 + 4 = 0$$

$$3V_2 - V_3 = 2$$

$$V_2 + 12 + \frac{V_3}{2} = 0 \Rightarrow 2V_2 + 24 + V_3 = 0$$

$$\begin{cases} 3V_2 - V_3 = 2 \\ 2V_2 + V_3 = -24 \end{cases}$$

$$V_3 = 3V_2 - 2$$

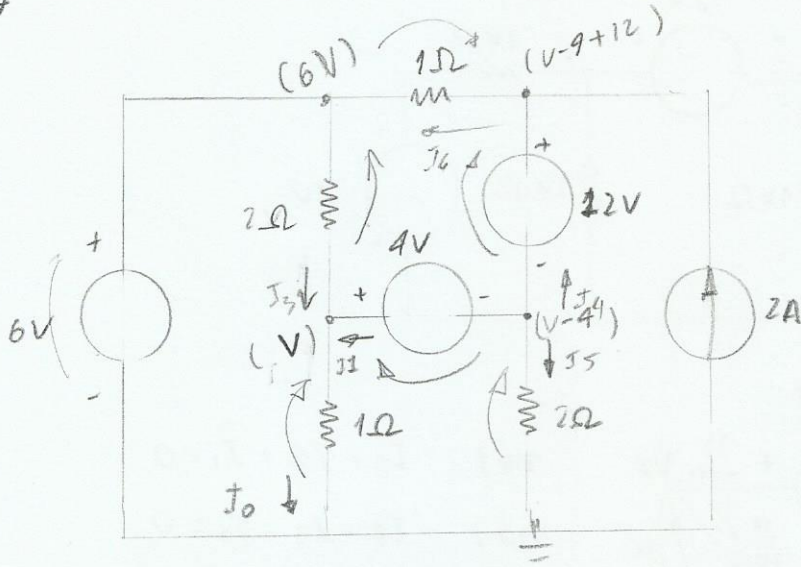
$$V_3 = 3 \cdot \left(\frac{-22}{5} \right) - 2$$

$$5V_2 = -22$$

$$V_2 = \frac{-22}{5}$$

$$\therefore V_3 = 15,02$$

3.27



nó 1: $I_0 - I_1 - I_3 = 0$

$I_0 - I_3 + I_5 + I_6 = 2$

nó 2: $I_1 + I_4 + I_5 = 0$

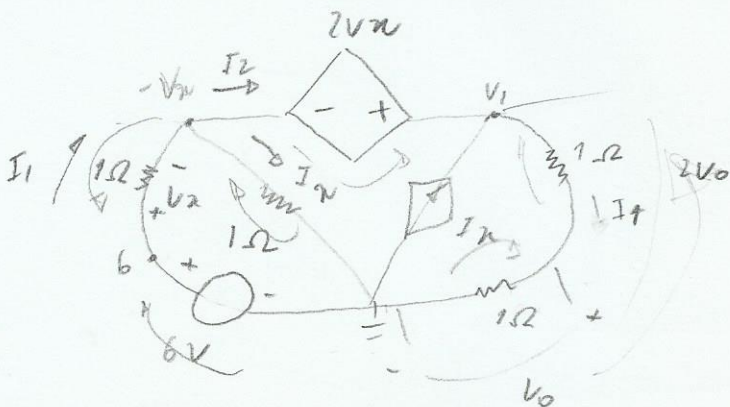
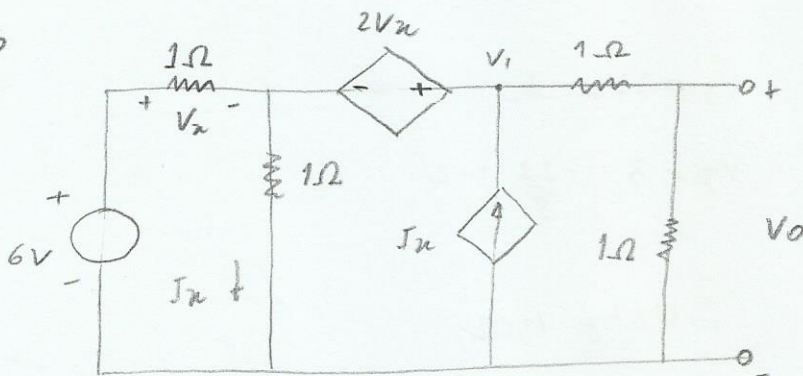
nó 3: $-I_4 + I_6 - 2 = 0$

$$\frac{V-0}{1} - \left(\frac{6-V}{2} \right) + \frac{V-4}{2} + \frac{V+6-6}{1} = 2$$

$$2V - 6 + V + V - 4 + 2V - A = A$$

$$6V = 10 \quad \therefore V = \frac{5}{3}$$

3.36



nó 1: $-I_1 + I_2 + I_3 = 0$

nó 2: $-I_2 - I_3 + I_4 = 0$

$-I_1 + I_4 = 0$

$I_1 = I_4$

$$\frac{6 - (2V_0 - 2V_x)}{1} = \frac{2V_0 - 0}{2}$$

$$6 - 2V_0 + 2V_x = V_0$$

$$V_x = 6 - (2V_0 - 2V_x) = 0$$

$$6 - 3V_0 + 2V_x = 0$$

$$V_x = 6 - 2V_0 + 2V_x$$

$$-3V_0 + 2V_x = -6$$

$$-V_x = 6 - 2V_0$$

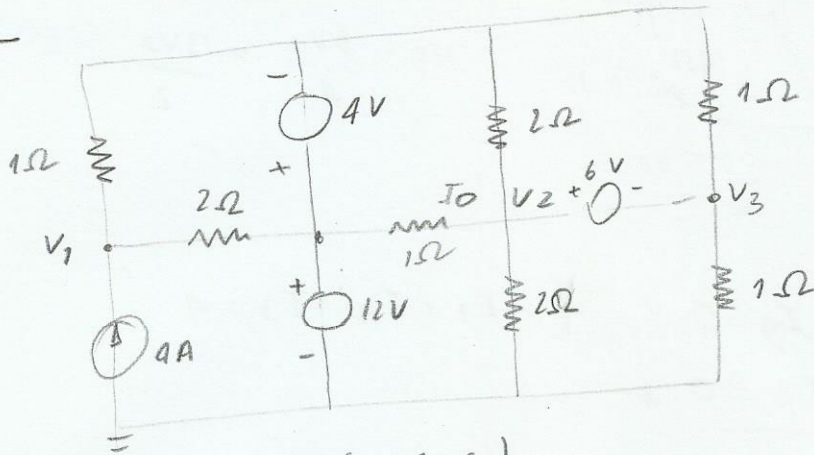
$$V_x = 2V_0 - 6$$

$$-3V_0 + 2(V_0 - 6) = -6$$

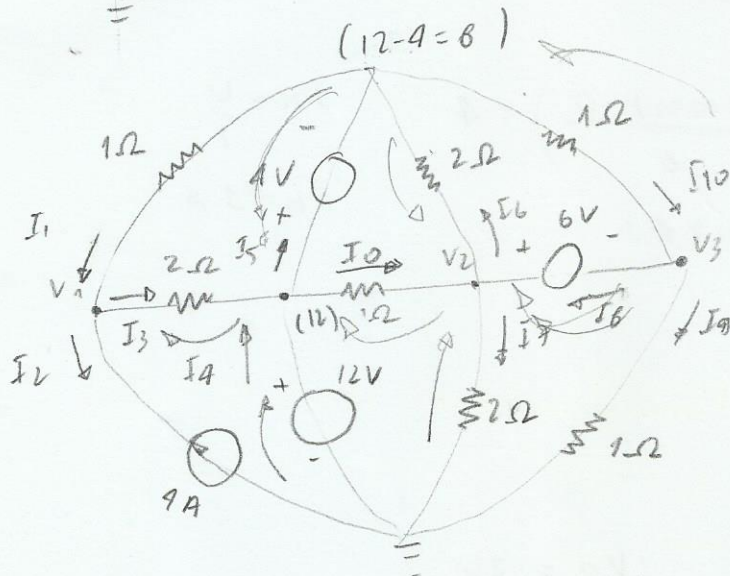
$$-3V_0 + 2V_0 - 12 = -6$$

$$-V_0 = 12 \quad \therefore \quad V_0 = -6V$$

3.30



Determine I_0



$$I_0 = \frac{12 - V}{1} = \frac{12 - 6}{1} = \underline{6V}$$

nos: $-I_0 - I_8 + I_6 + I_7 = 0$

$$I_8 + I_9 - I_{10} = 0$$

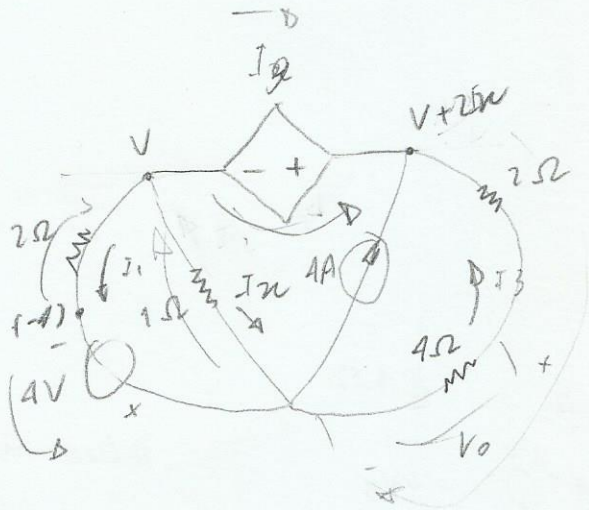
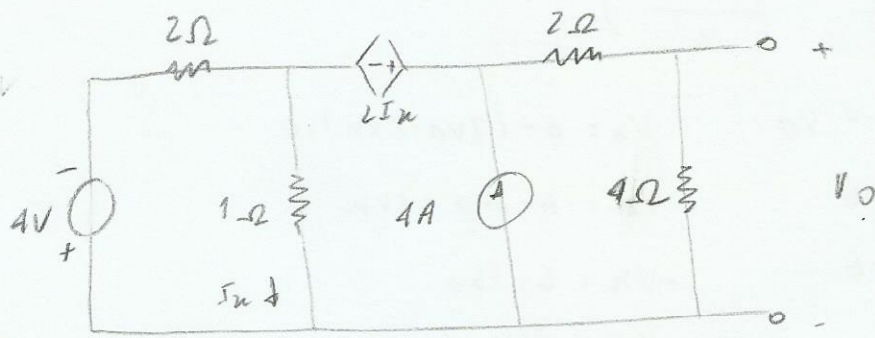
$$-I_0 + I_6 + I_7 + I_9 - I_{10} = 0$$

$$\frac{2 - V}{1}$$

$$-\left(\frac{12 - V}{1}\right) + \frac{V - 6}{2} + \frac{V}{2} + \frac{V - 6}{1} - \left(\frac{8 - (V - 6)}{1}\right) = 0$$

$$-24 + 2V + V - 6 + V + 2V - 12 + 2V - 4 = 0 \quad 8V = 46 \quad V = 6V$$

3.31



$$V_o = \frac{4}{2+4} V_c$$

$$V_c = \frac{6V_o}{4} = \frac{3V_o}{2}$$

nós: $I_1 + I_n + I_2 = 0$
 $-I_2 - 4 - I_3 = 0$

$$I_1 + I_n - I_3 = 4$$

$$\frac{V+4}{2} + \frac{V-0}{1} - \left(\frac{V+2I_n}{4} - 0 \right) = 4$$

$$I_n = \frac{V}{1}$$

$$I_n = 1A$$

$$3V + 12 + 6V + V + 2I_n = 24$$

$$10V + 2V = 12$$

$$12V = 12$$

$$V = 1$$

$$V_o = \frac{4}{2+4} (1+2) \therefore V_o = 2V$$